



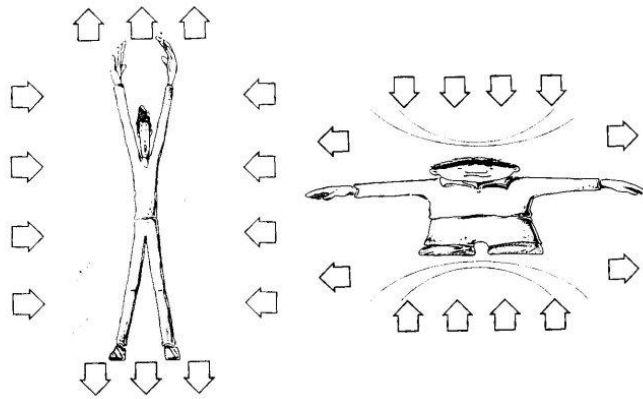
GRAN SASSO
SCIENCE
INSTITUTE



New technologies for sensitivity improvement of current and future gravitational-wave detectors

17th October 2019
Francesca Badaracco

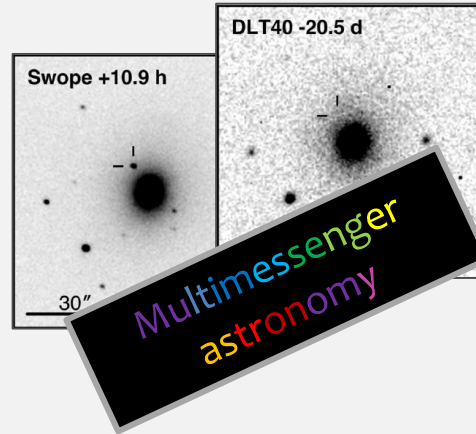
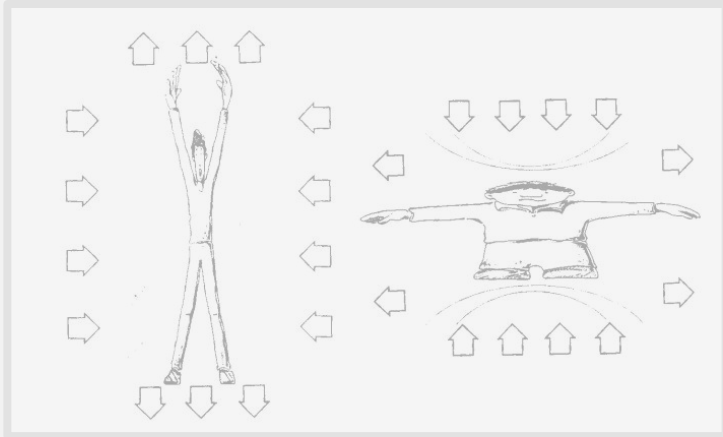
- What a gravitational wave is
- Why is it important to Astrophysics
- How does a gravitational wave detector work?



They are just like EM waves but they move in the 4D space-time modifying its structure.

$$\frac{\Delta L}{L} = 10^{-21}$$

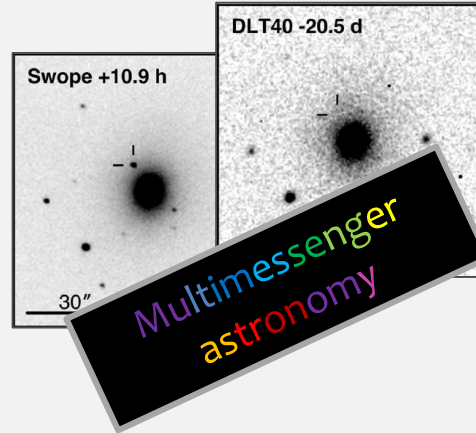
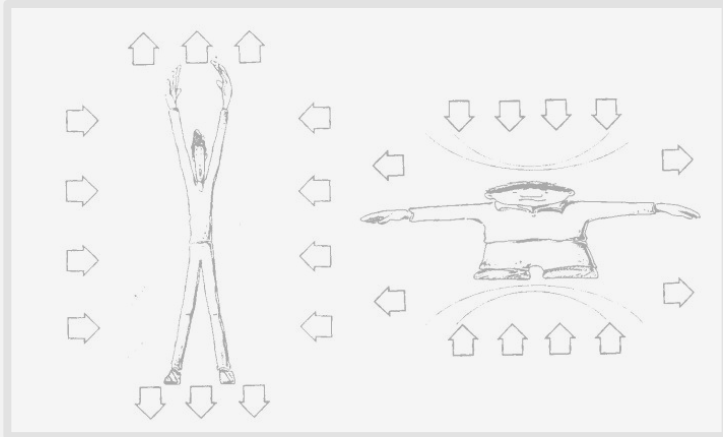
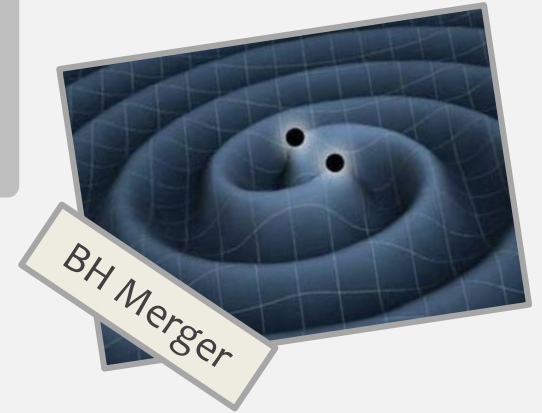
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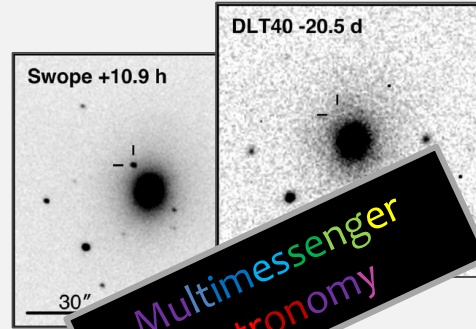
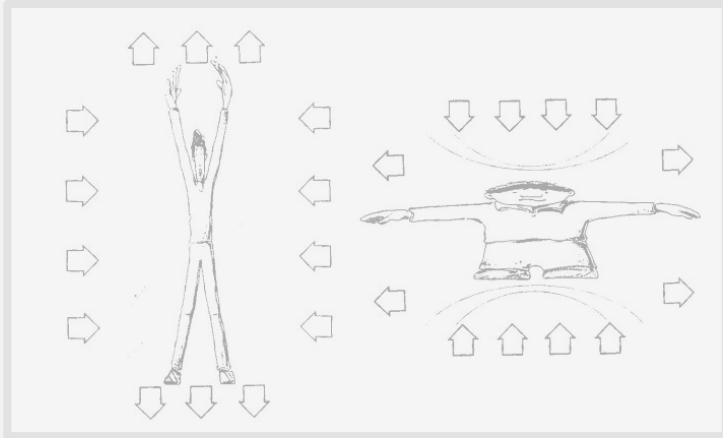
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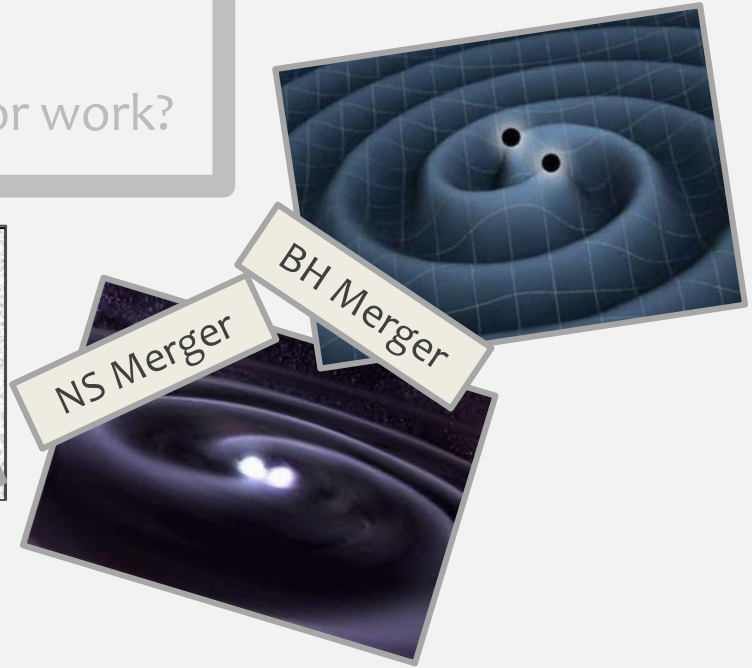
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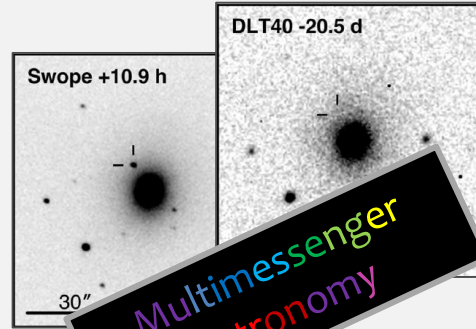
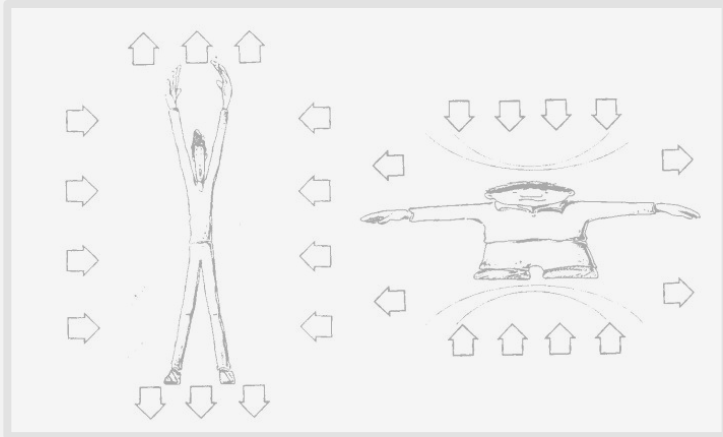
Multimessenger
astronomy



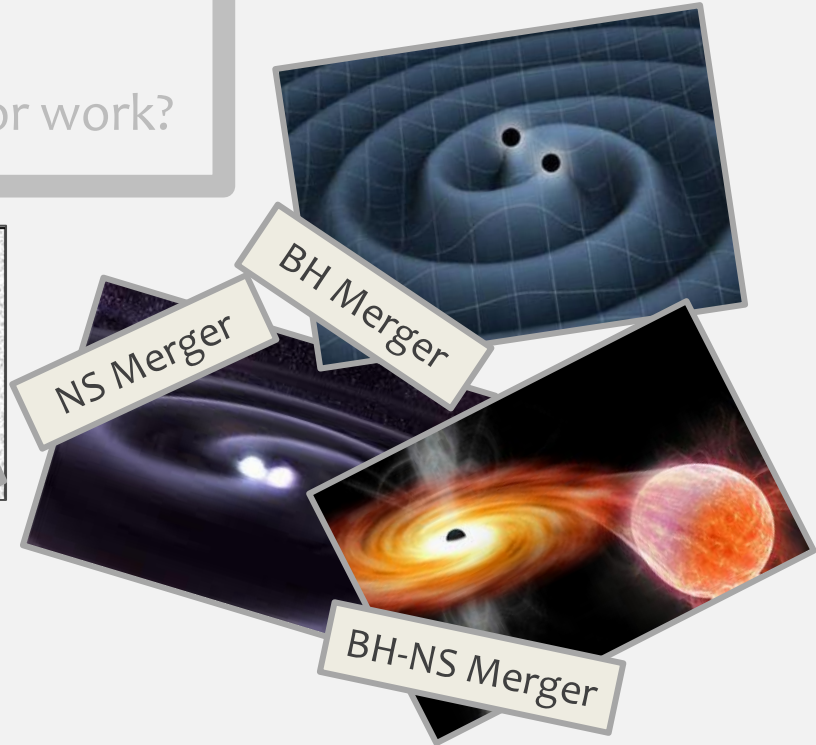
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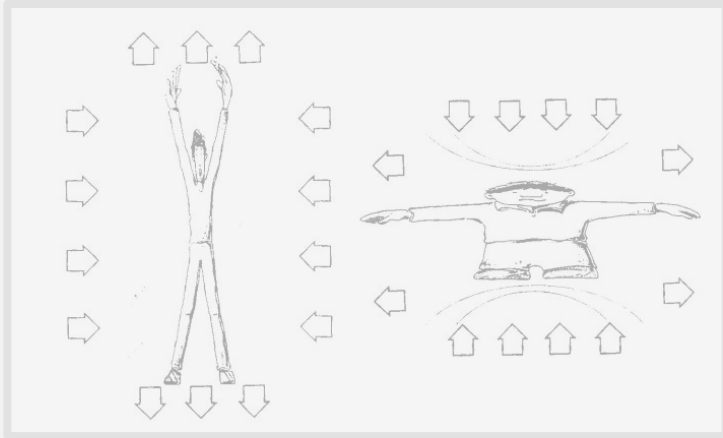
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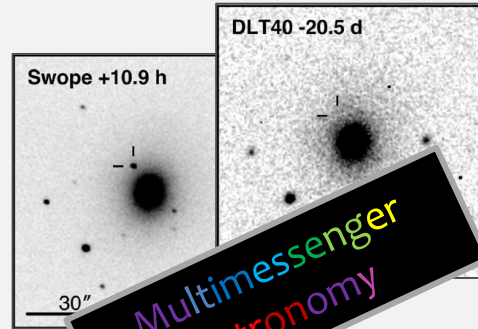
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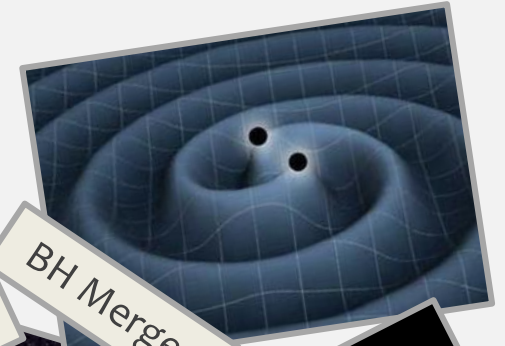


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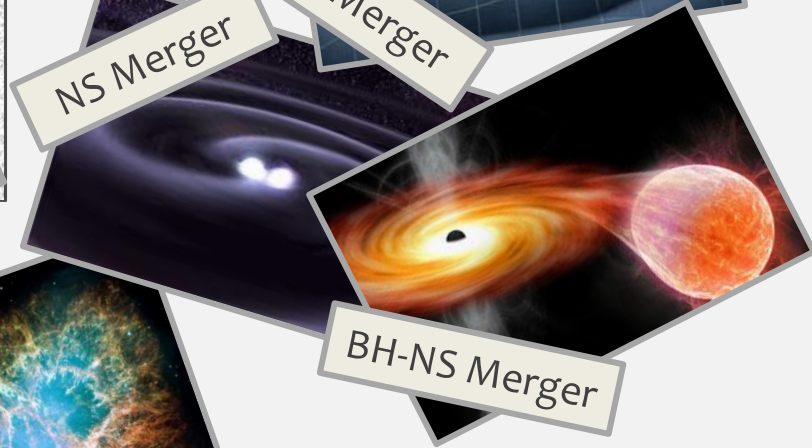


Multimessenger
astronomy



BH Merger

NS Merger

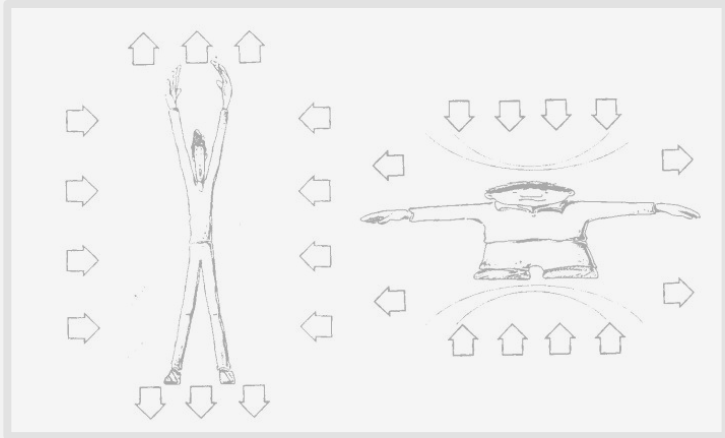


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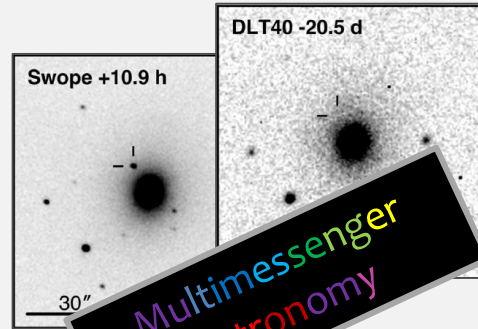
Supernovae

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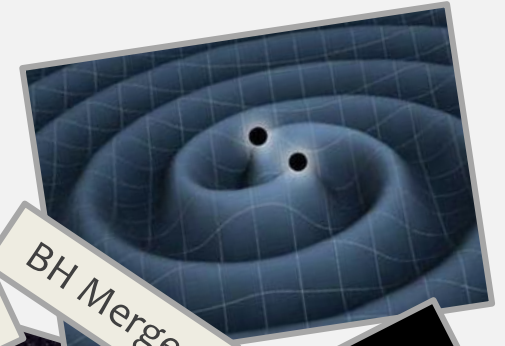


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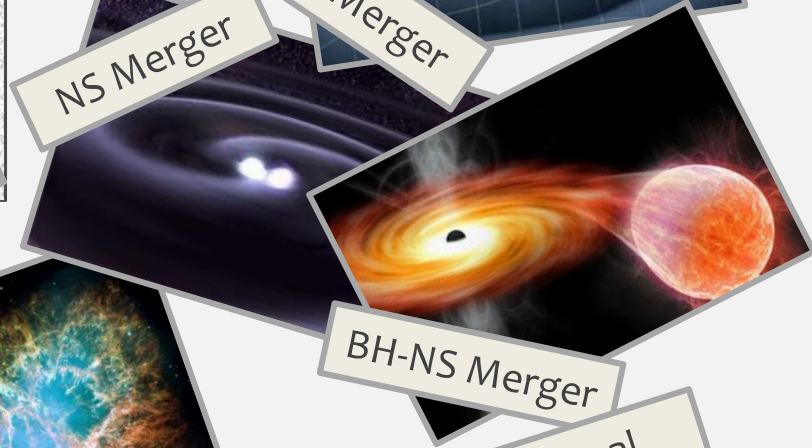


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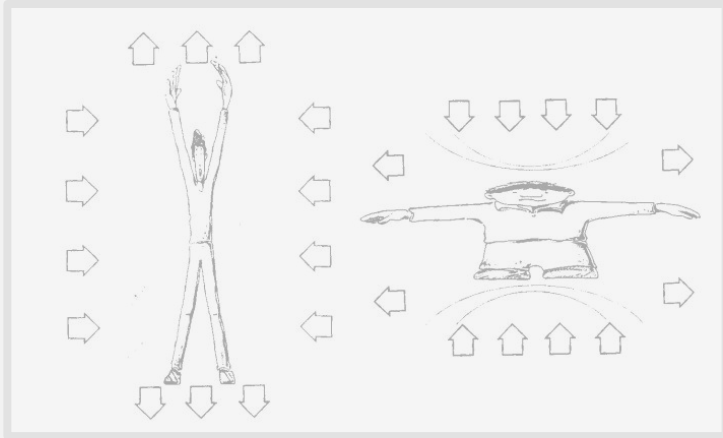
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Supernovae

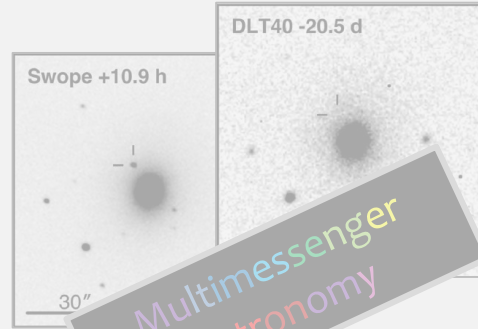
Stochastic gravitational
wave background
(unresolved sources)

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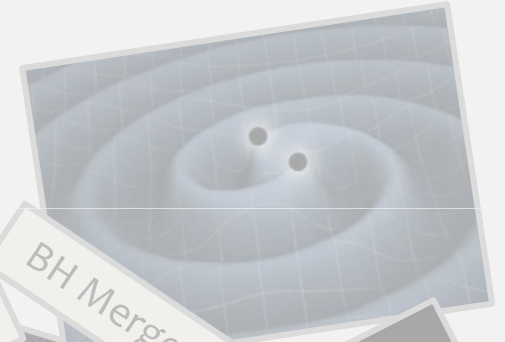


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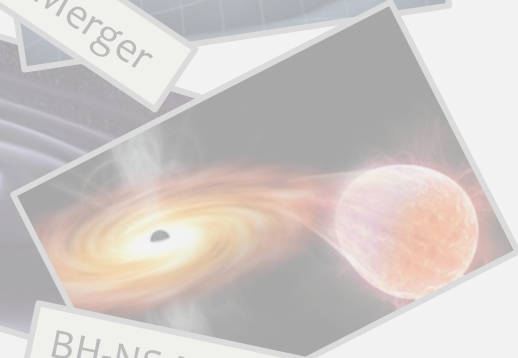
Multimessenger
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BH Merger



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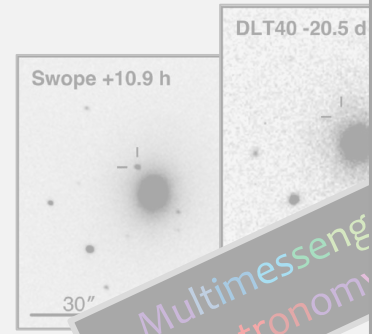
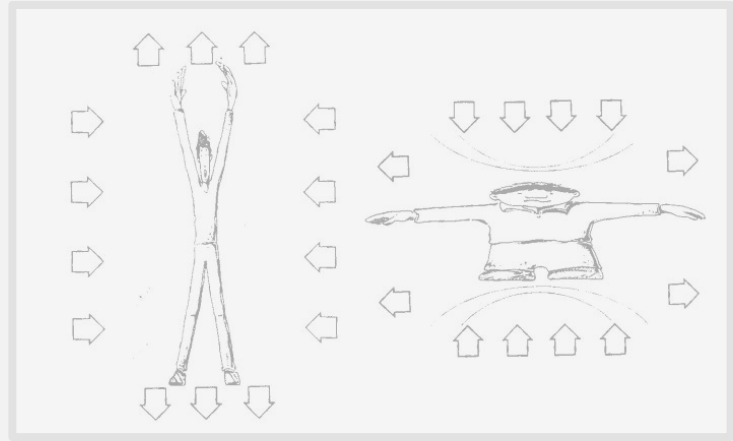
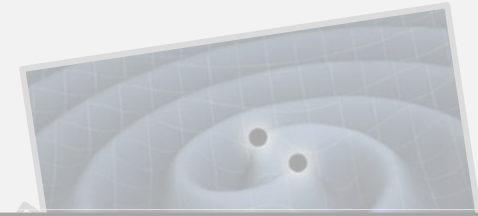
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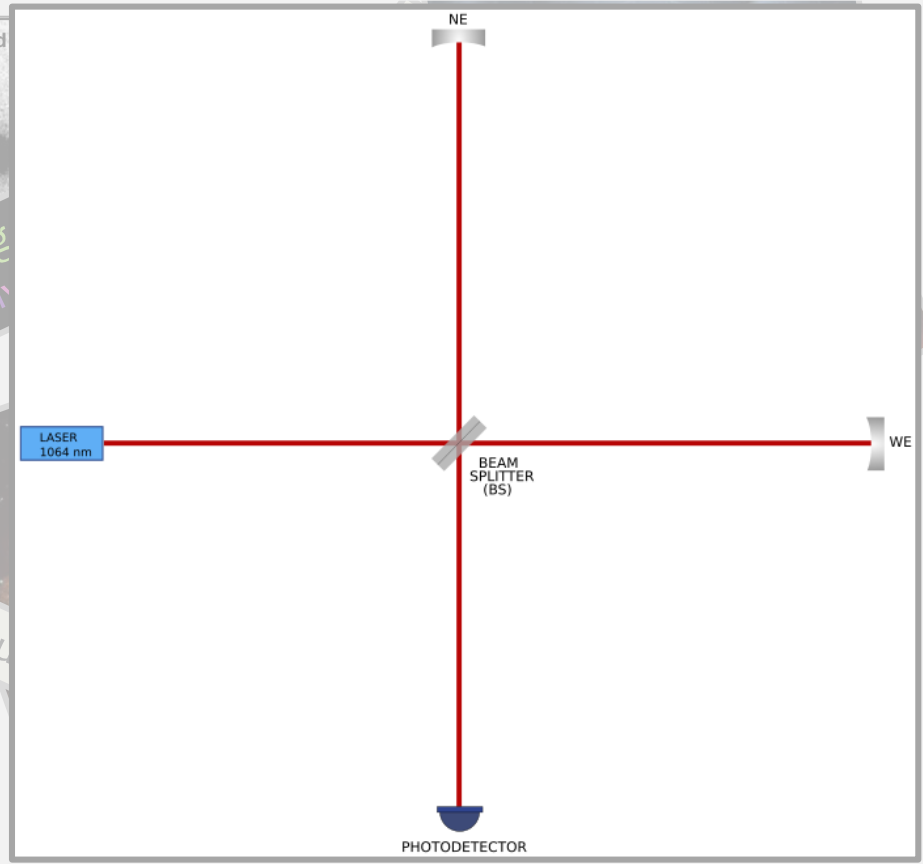
Supernovae

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- What a gravitational wave is
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Multimessenger
astronomy



Measure the change in length →
 Measure change in phase
 $\Delta L \propto hL$
 $\Delta\phi \propto hL$

- What a gravitational wave is
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Introduction of Fabry-Perot cavities (we indeed need interferometers 100 Km long)

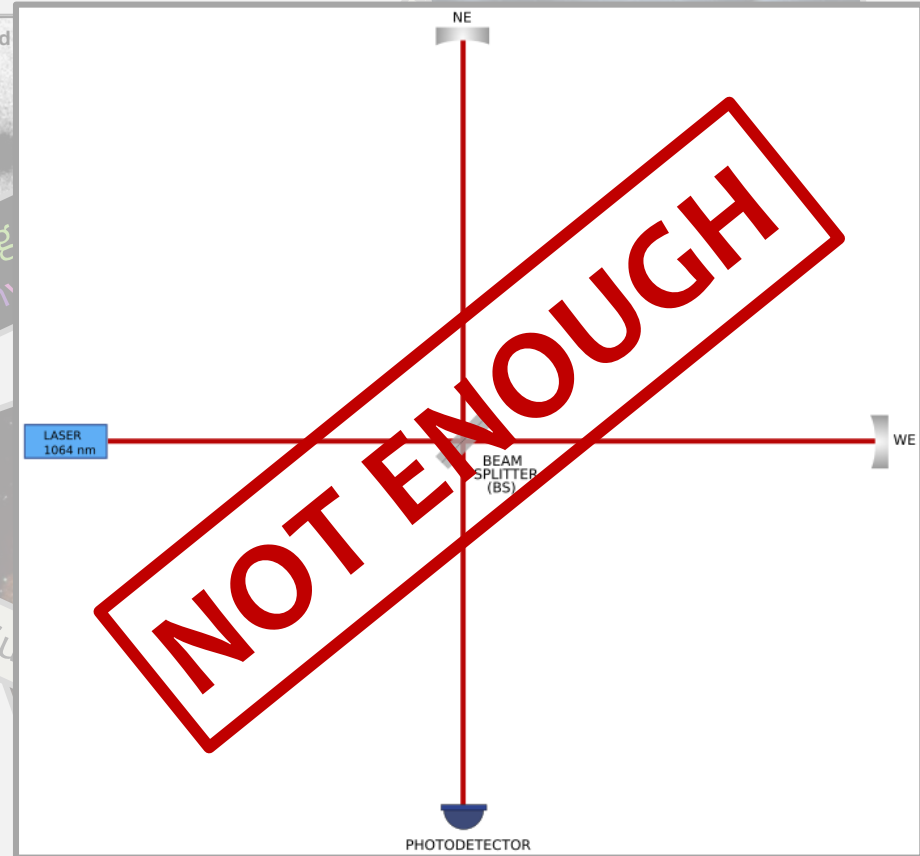
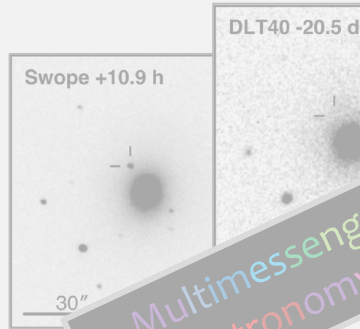
$$L \sim \frac{\lambda_{gw}}{2} = \frac{c}{2f_{gw}}$$

Measure the change in length →
Measure change in phase

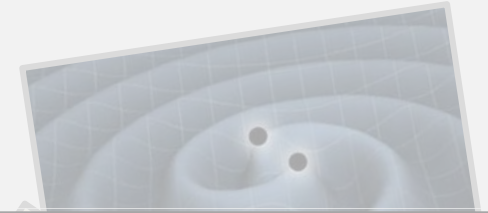
$$\Delta L \propto hL$$

$$\Delta \phi \propto hL$$

$$h \sim 10^{-21}$$

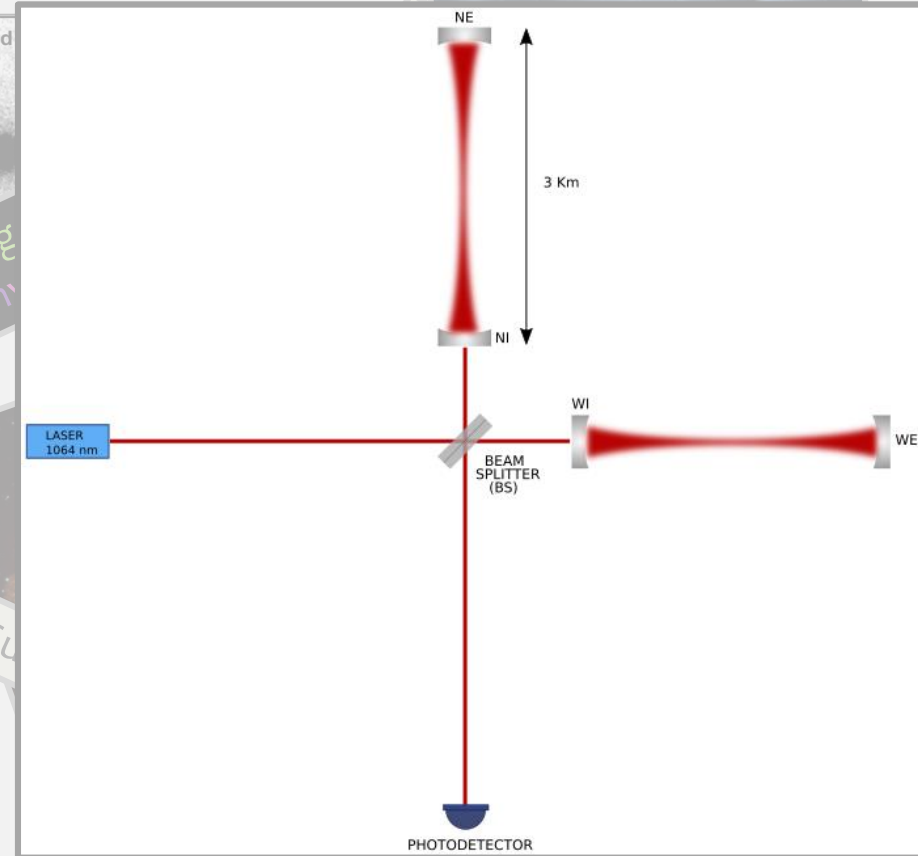
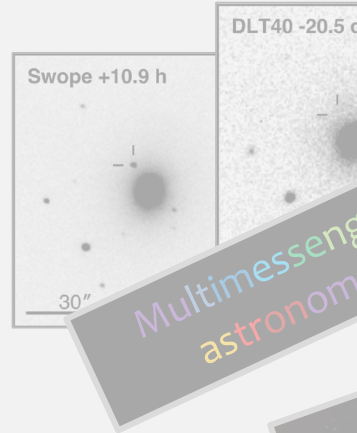


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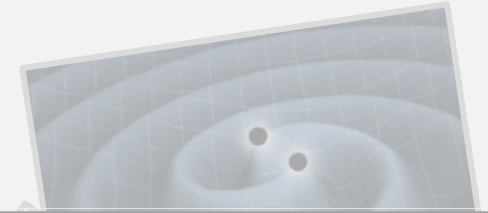
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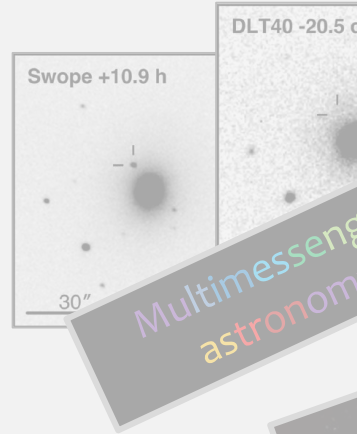
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Many different parts to reach the required sensitivity!!!

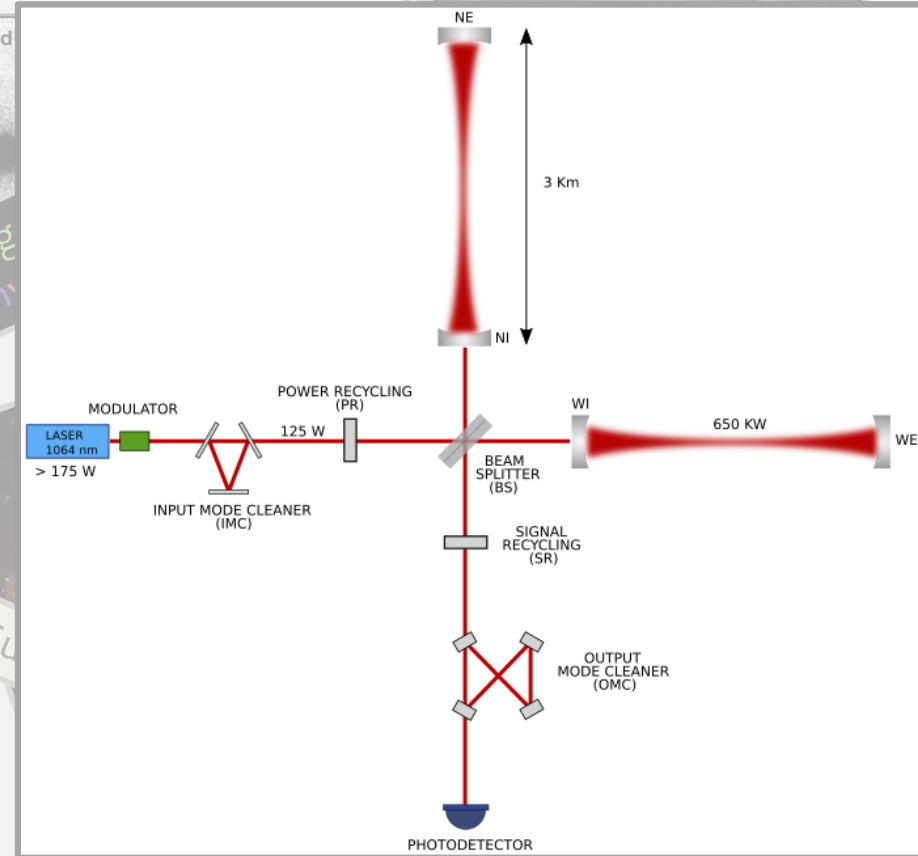


Measure the change in length →
Measure change in phase

$$\Delta L \propto hL$$

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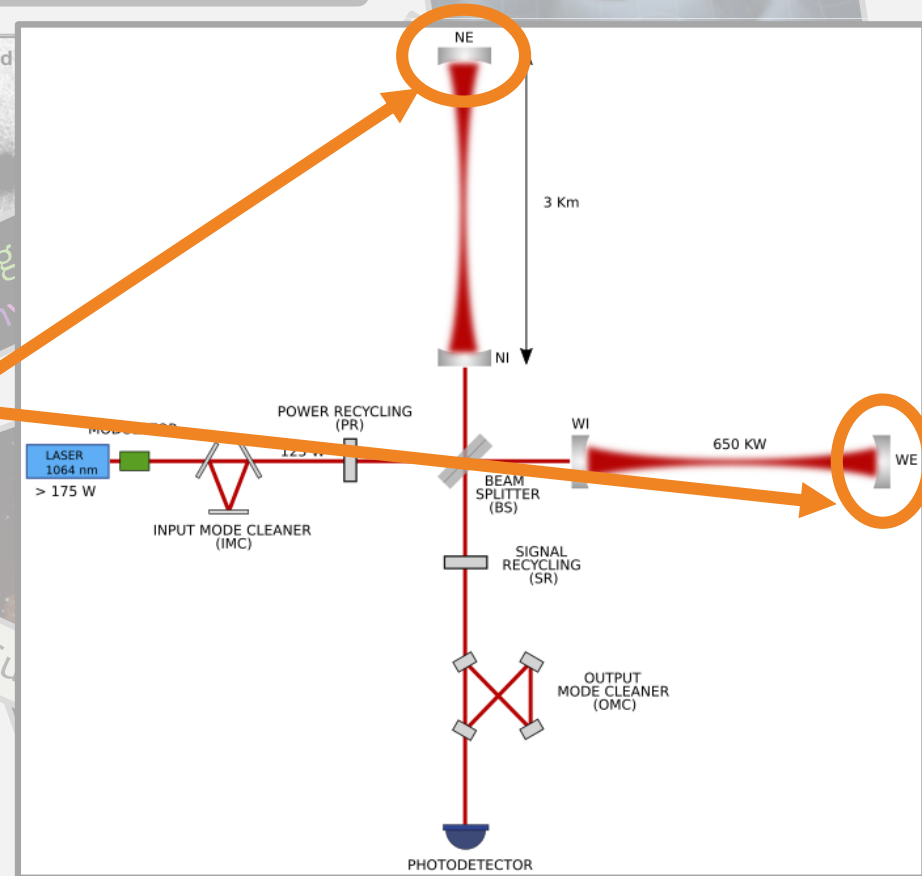
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To be kept in mind: when I will mention the 'TEST MASSES' I will refer to the **end mirrors** of the interferometer!!! Which are in **free fall** along the arms direction.

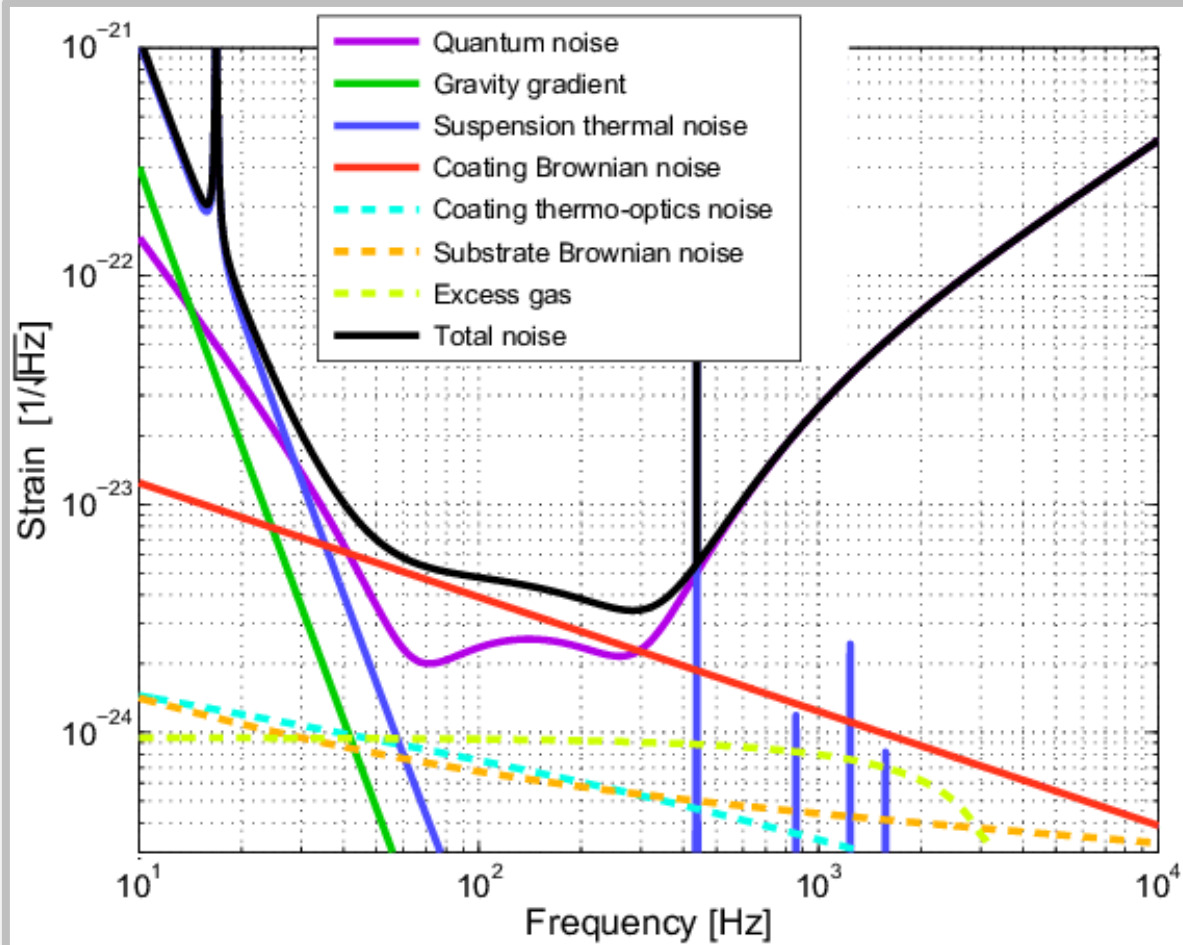
$$\Delta L \propto hL$$

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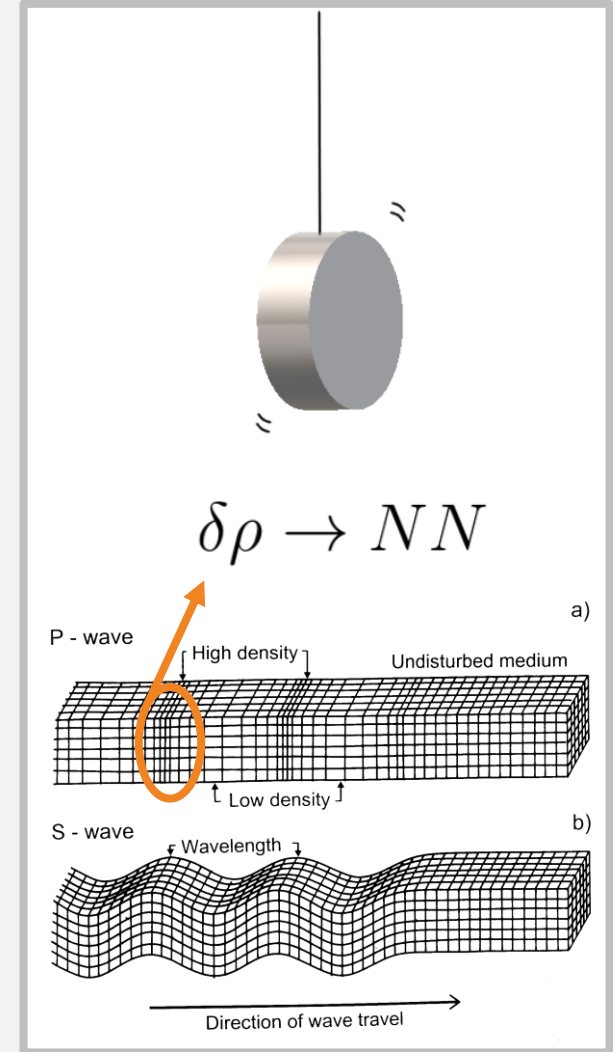
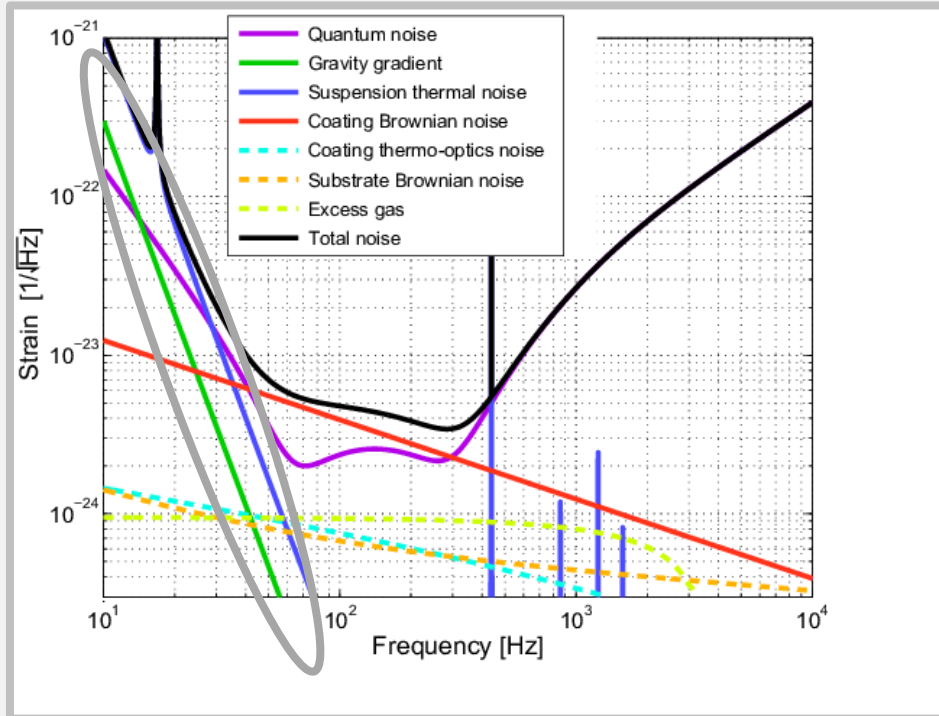
Plenty of different kinds of noises



What is Newtonian Noise (NN):

Perturbation of the gravity field due to a variation in the density ($\delta\rho$) of the surrounding media.

Example of NN in Virgo:

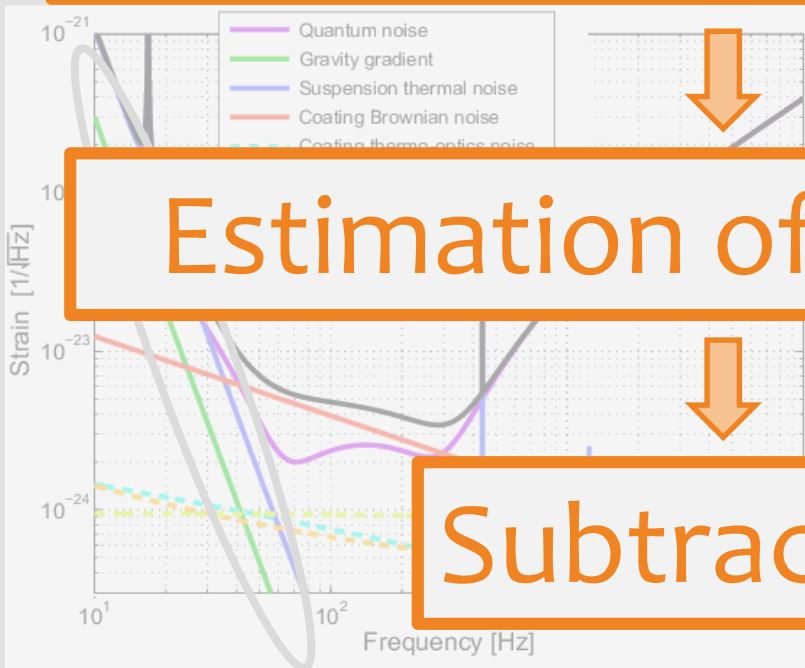


Virgo

Perturbat
the d

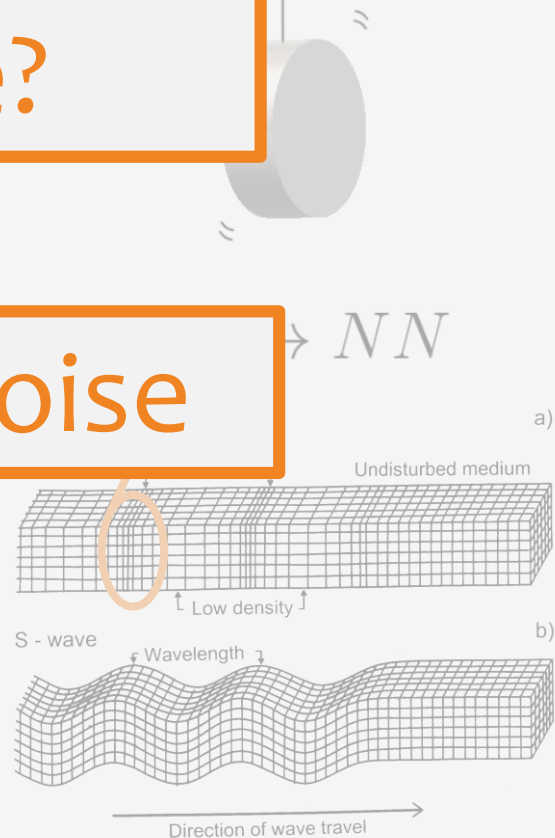
What can we do about Newtonian Noise?

Example of
NN in Virgo:



Estimation of the noise

Subtraction

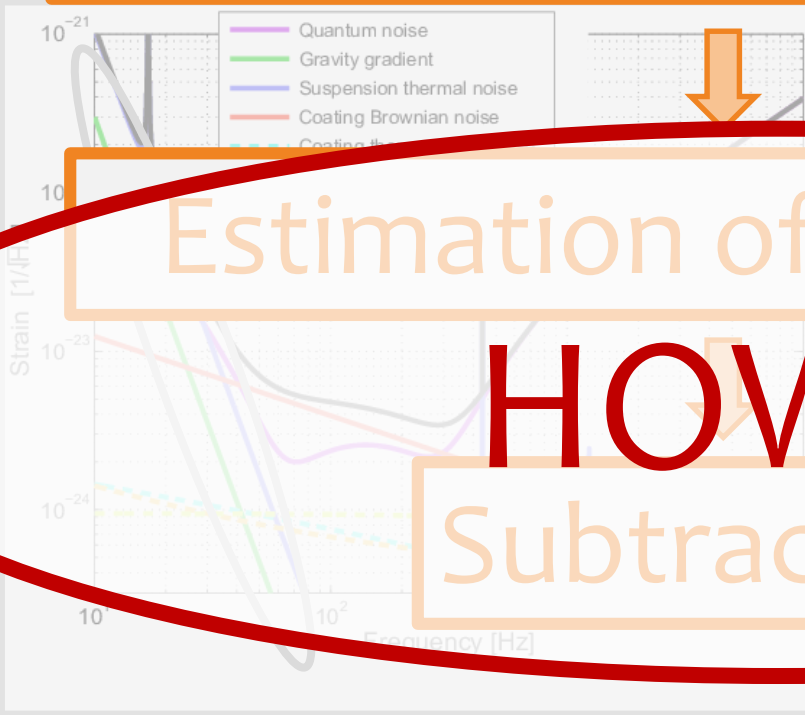


Virgo

Perturbat
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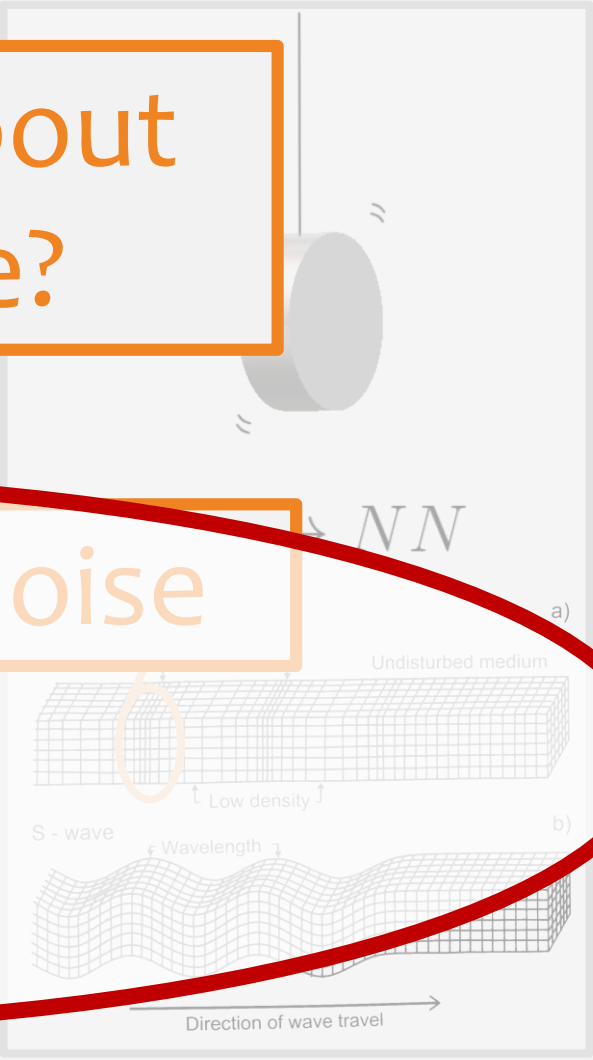
Example of
NN in Virgo:



Estimation of the noise

HOW?!?

Subtraction



Wiener filter is the way

Assumptions:

- Stationary signal
- Linear relationship: $x \propto y$

$$\hat{x}(m) = \sum_{k=0}^{P-1} w_k y(m-k)$$

Estimated value of the **Newtonian Noise**

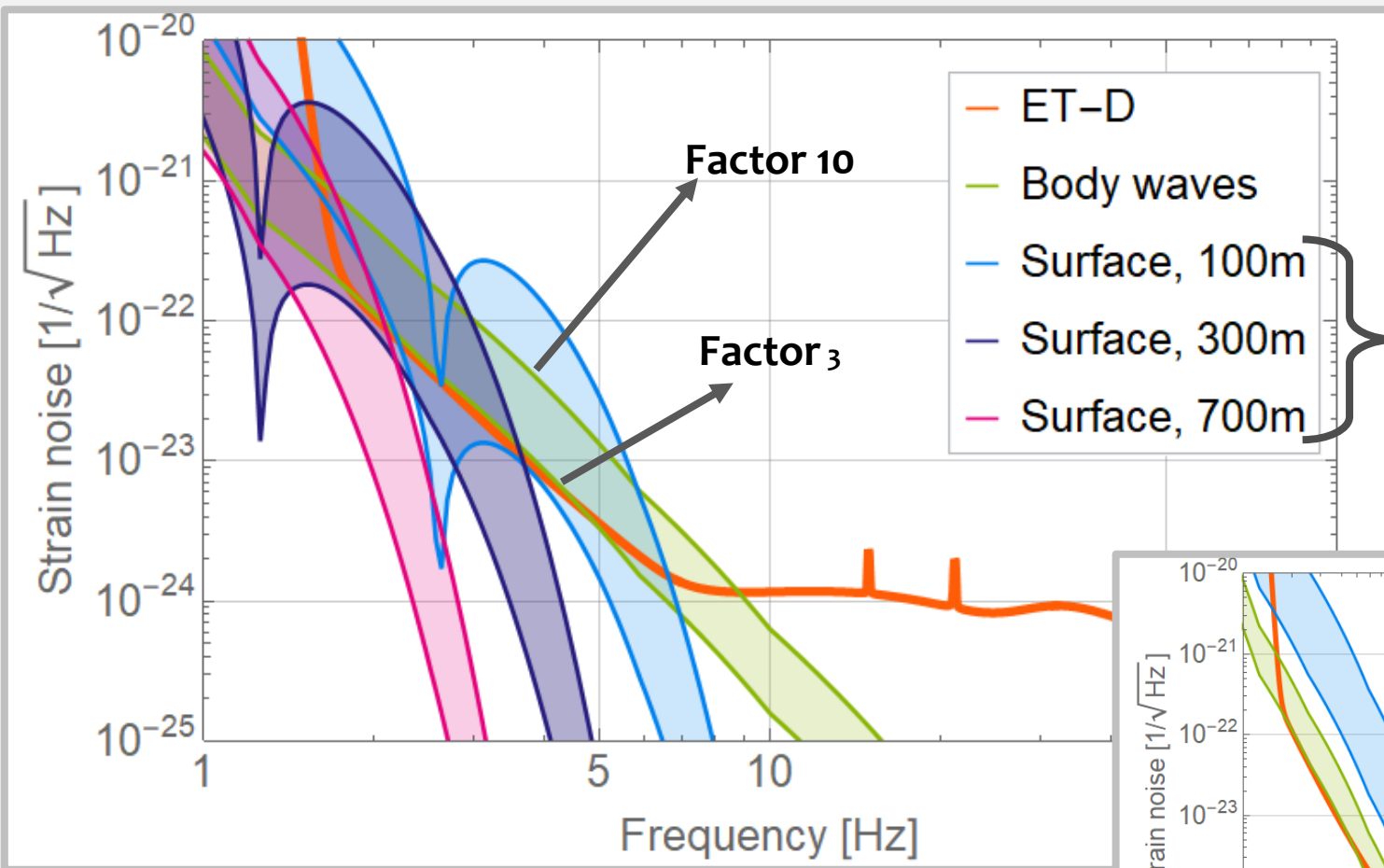
Wiener filter **coefficients**

Measured signal (**seismic displacement**)

Subtraction



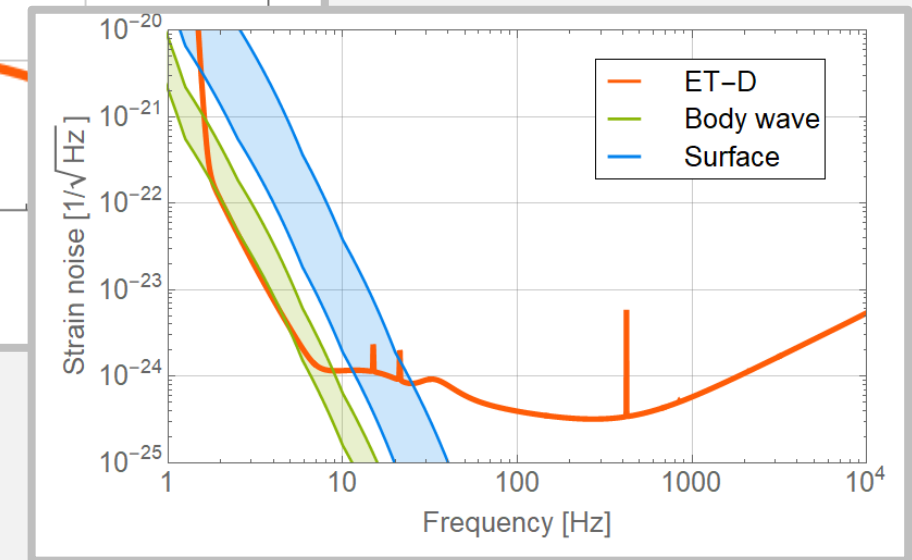
DATA - \hat{x}



How much deep?

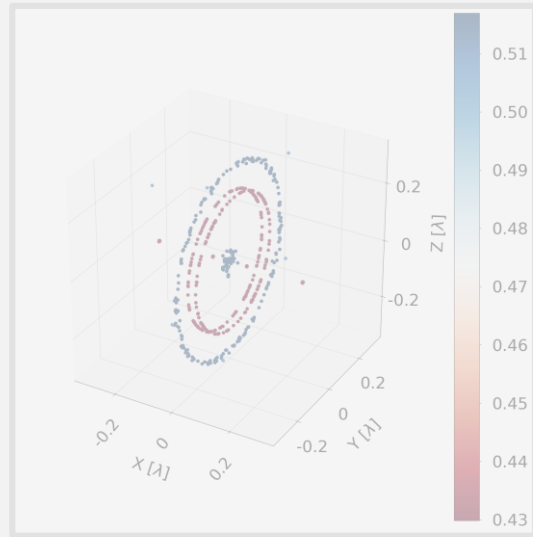
Surface

Underground
Suppression up to a
factor 10



OPTIMIZATION of:

$$R(\omega) = 1 - \frac{\vec{C}_{SN}^\dagger(\omega) \cdot \left(\vec{C}_{SS}(\omega)\right)^{-1} \cdot \vec{C}_{SN}(\omega)}{C_{NN}(\omega)}$$

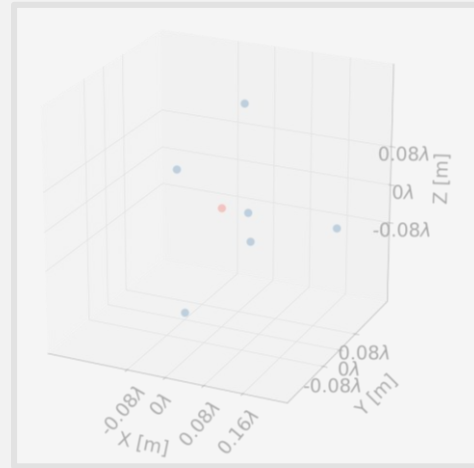


Cross Power Spectral Densities (CPSDs) between **seismometers**

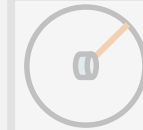
Power Spectral Density of **test mass**

CPSDs between **seismometers and test mass**

Single example



Isotropic & Homogeneous seismic field hypothesis



&

$k^{P,S} a \ll 1$

Gravitational coupling model: mirror ↔ field

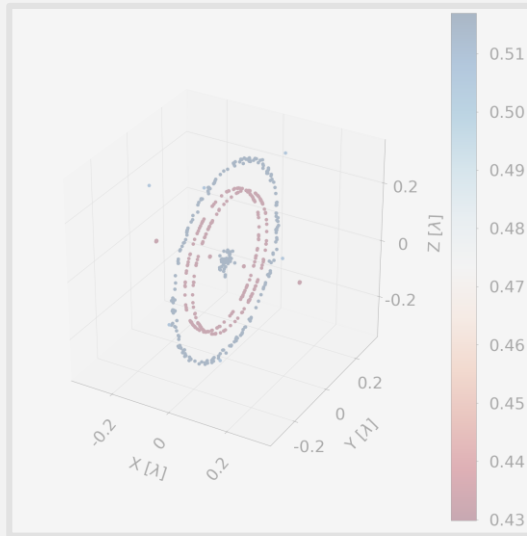
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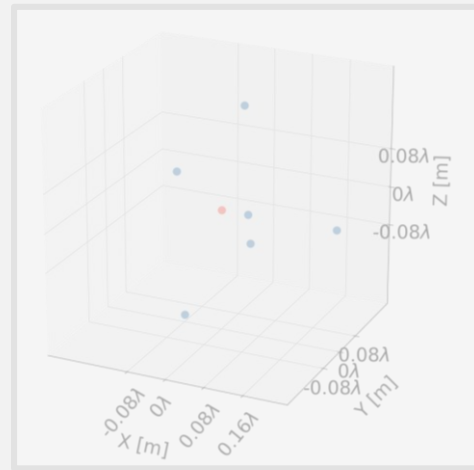
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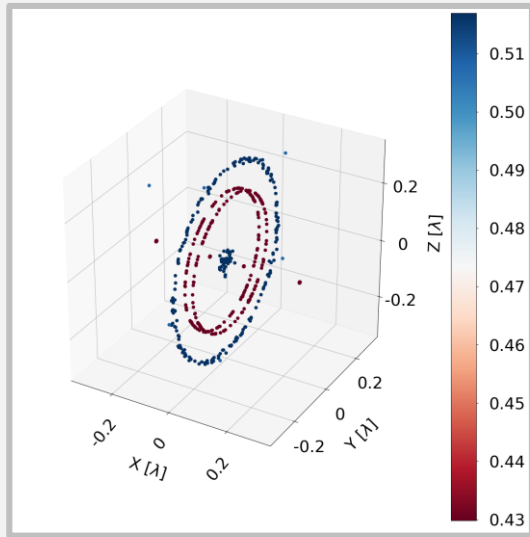
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Gravitational coupling model:
mirror \leftrightarrow field

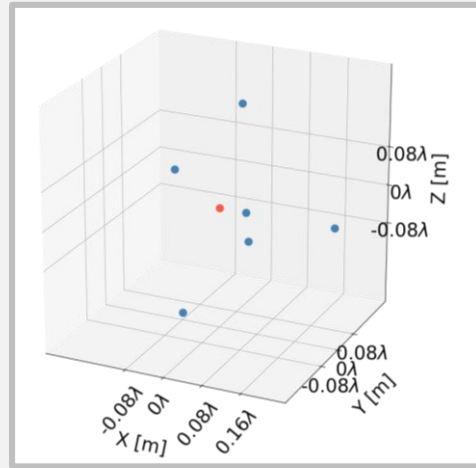
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Cross Power Spectral Densities (CPSDs) between seismometers

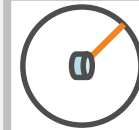
Single example



Power Spectral Density of test mass

CPSDs between seismometers and test mass

Isotropic & Homogeneous seismic field hypothesis

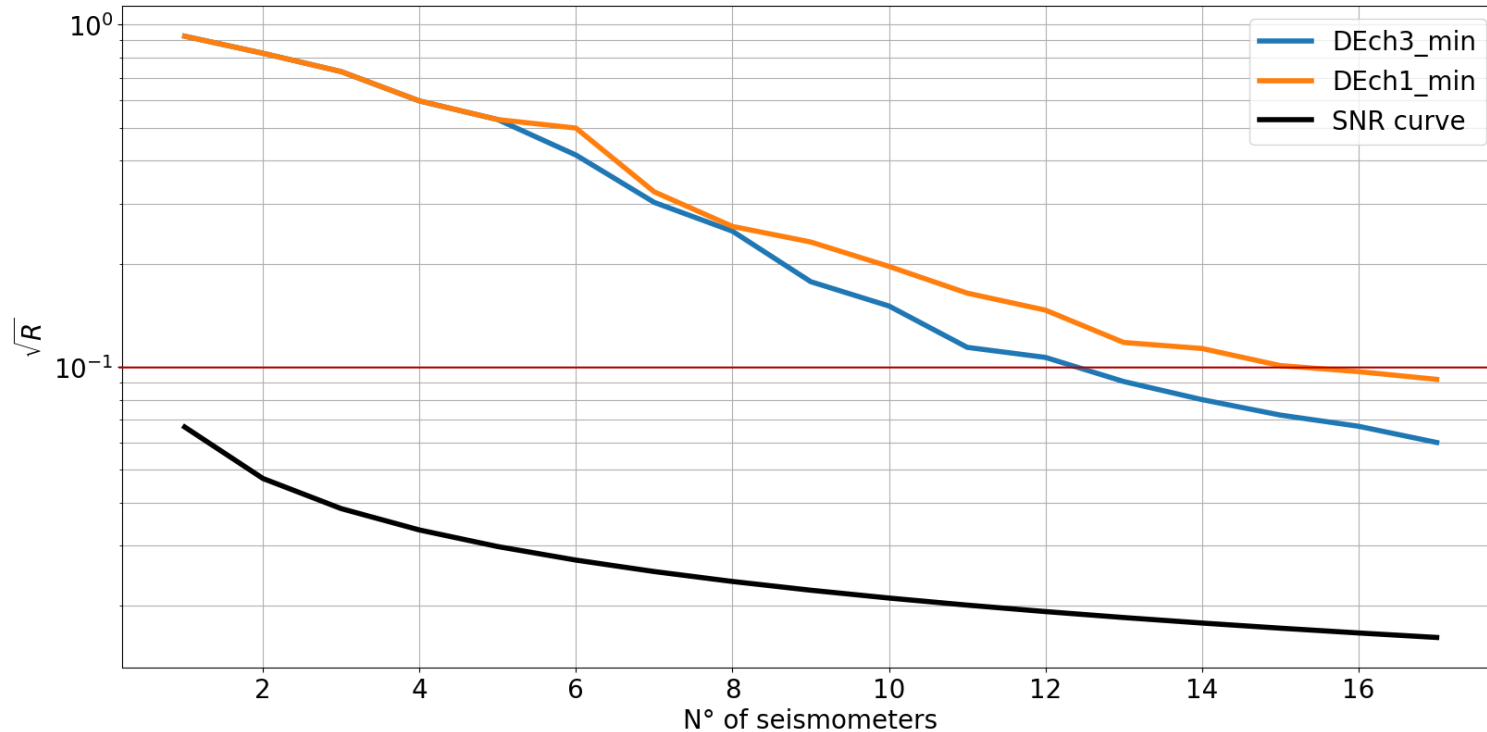


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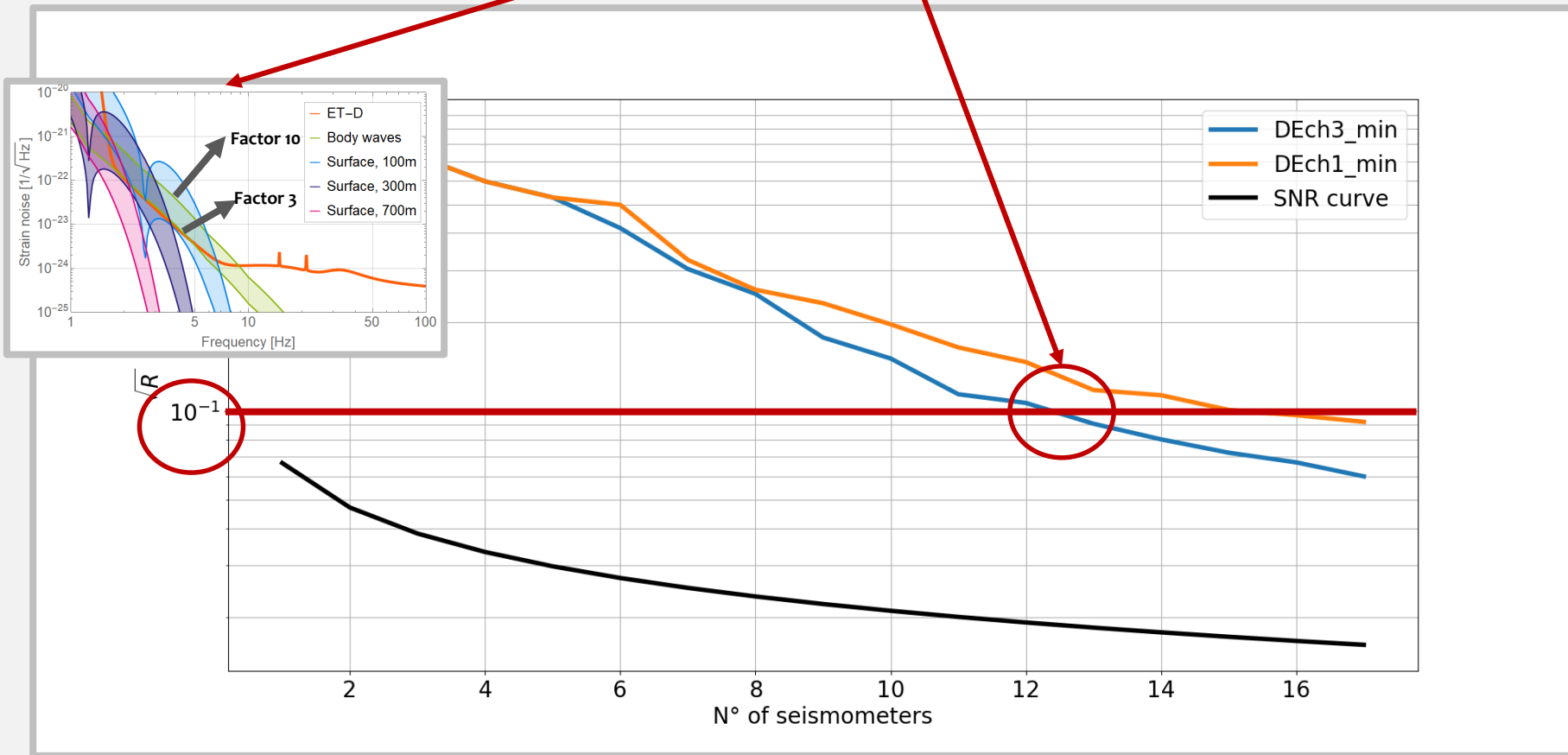
$$k^{P,S} a \ll 1$$

Gravitational coupling model: mirror <-> field

Successful mission: factor 10 of reduction already with 13 seismometers per test mass

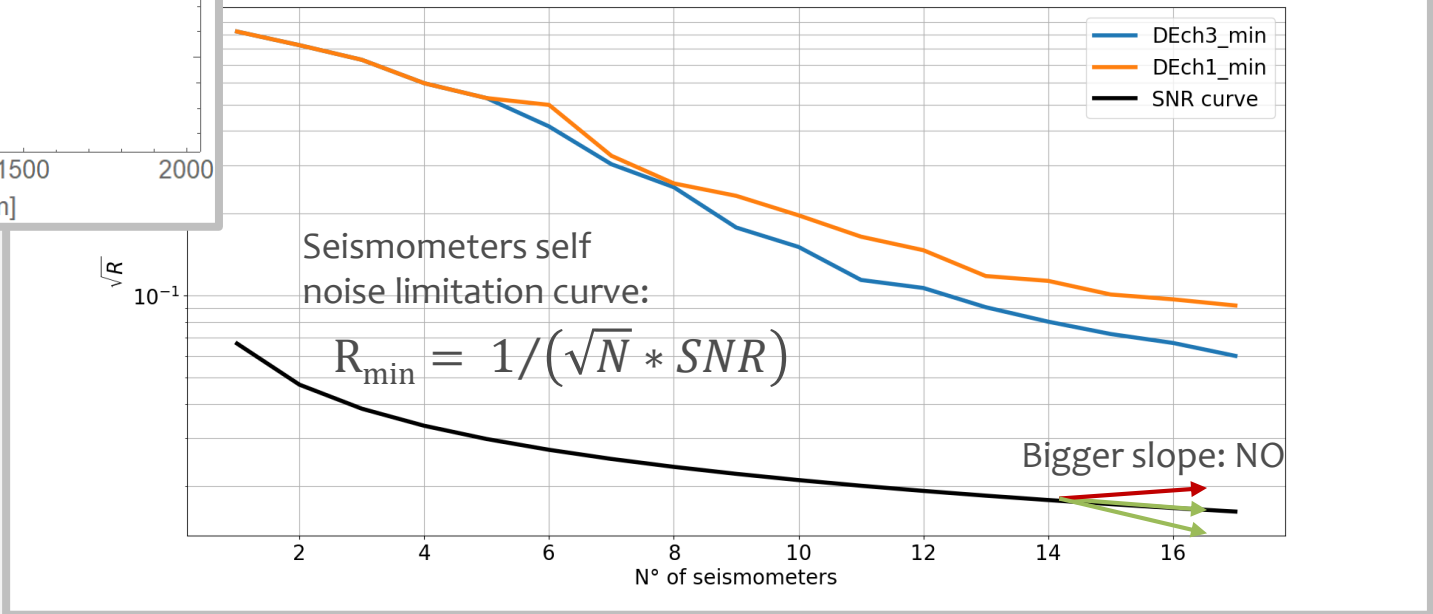
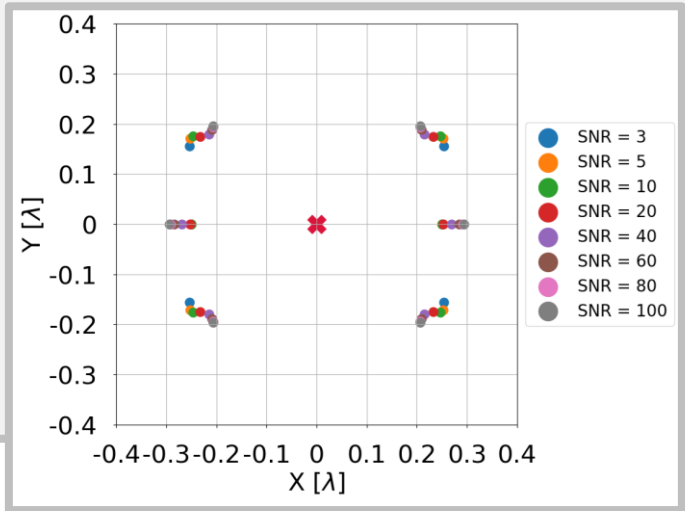
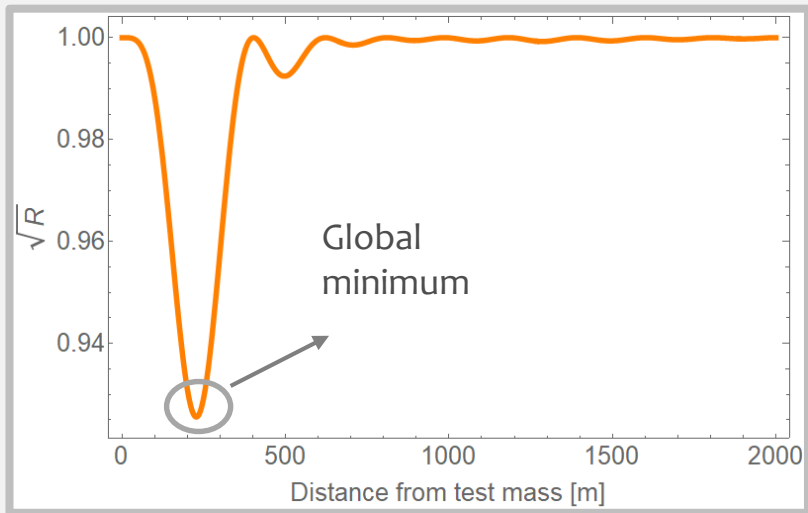


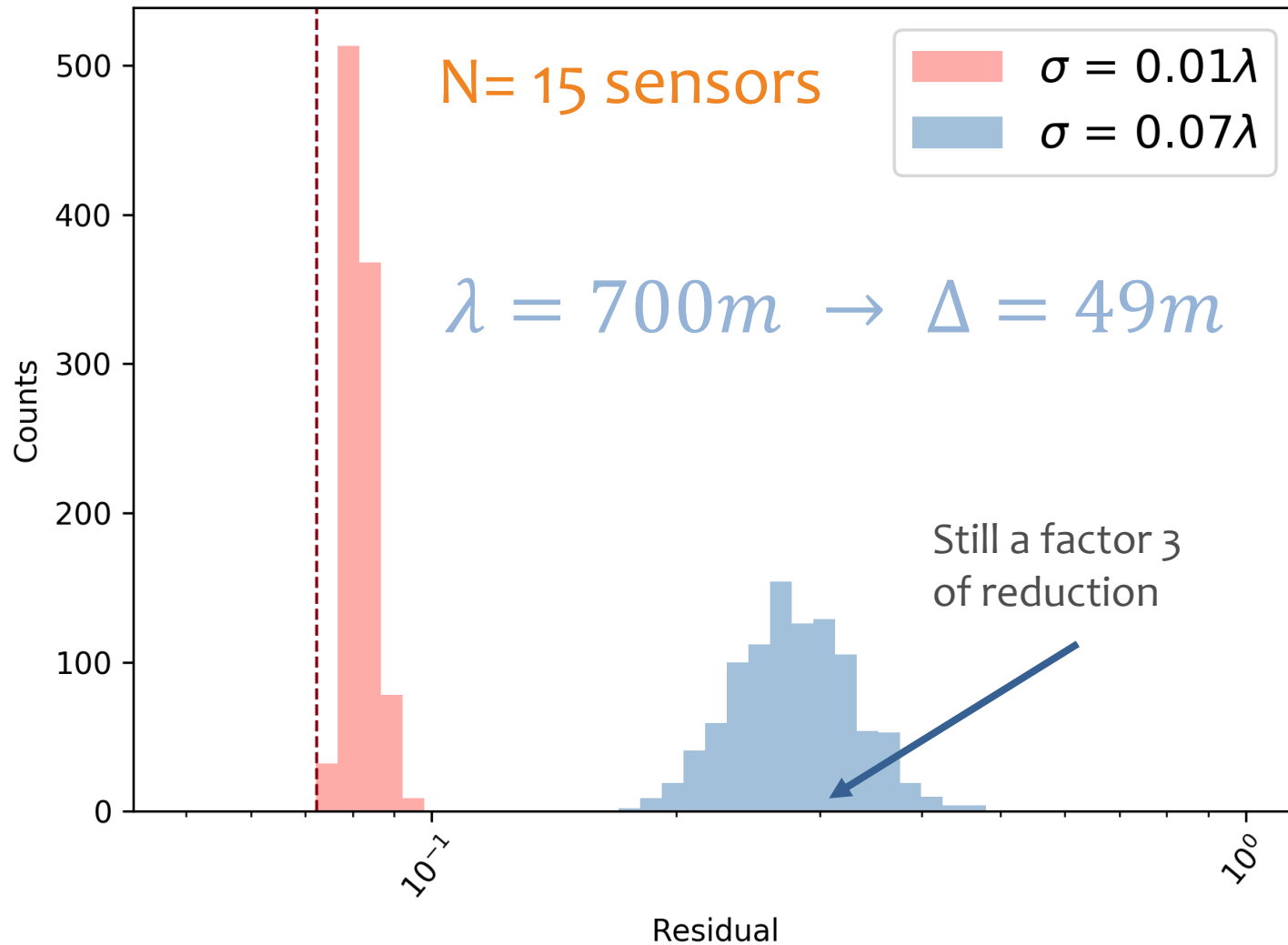
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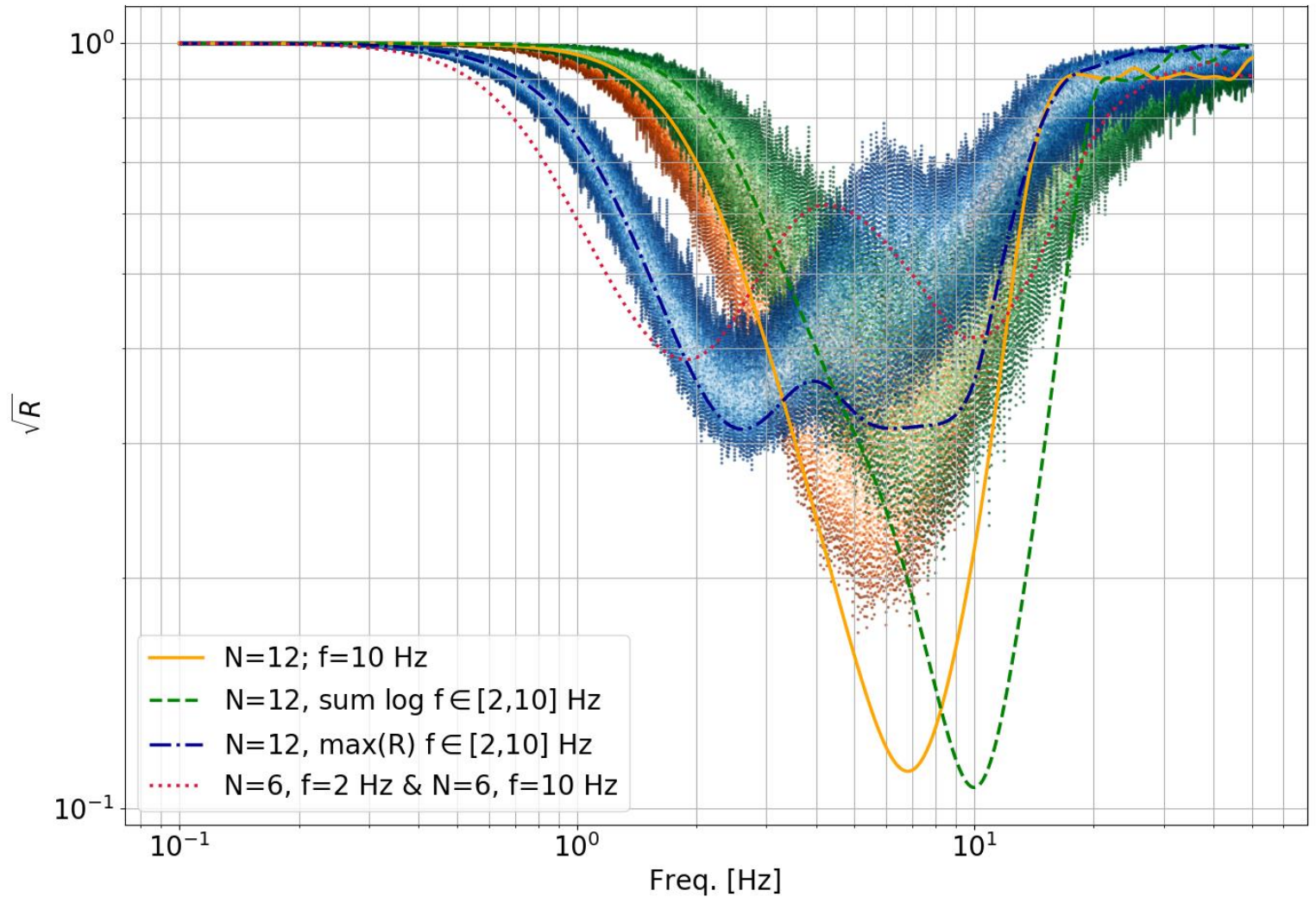
Validation:

Analytical solution for N = 1





Broadband optimization:



Optimization of seismometer arrays for the cancellation of Newtonian noise from seismic body waves

F Badaracco^{1,2} and J Harms^{1,2}

¹ Gran Sasso Science Institute (GSSI), I-67100 L'Aquila, Italy

² INFN, Laboratori Nazionali del Gran Sasso, I-67100 Assergi, Italy

E-mail: francesca.badaracco@gssi.it

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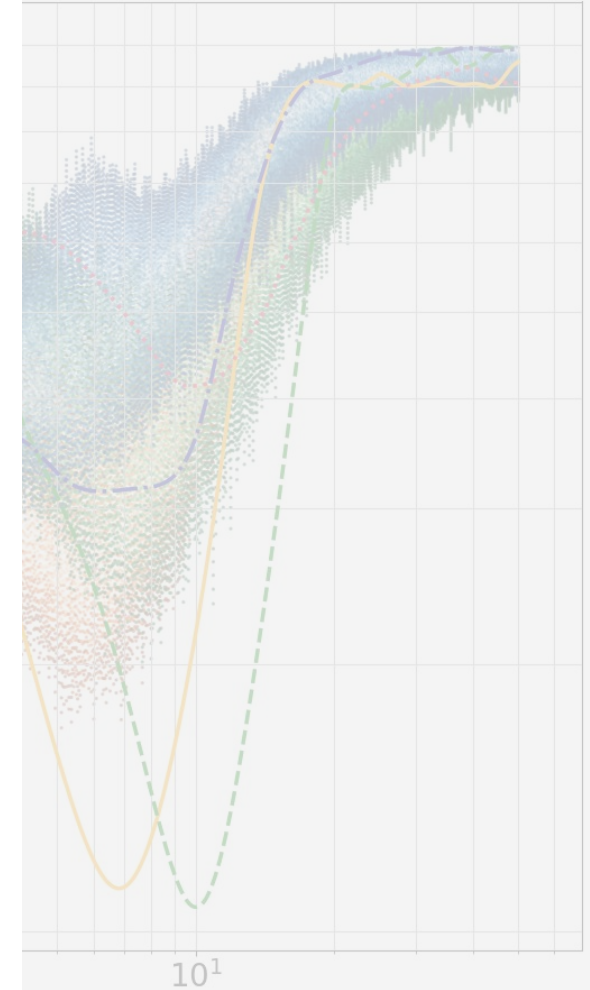
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Published 25 June 2019



Abstract

Newtonian noise (NN) from seismic fields is predicted to become a sensitivity limiting noise contribution of the gravitational-wave detectors Advanced LIGO and Virgo in the next few years. It also plays a major role in the planning of next-generation detectors, which might be constructed underground as planned for the Einstein telescope (ET) mostly to suppress NN. Coherent noise cancellation using Wiener filters provides a way to mitigate NN. So far, only the cancellation of NN produced by seismic surface waves has been studied in detail due to its relevance for Advanced LIGO and Virgo. However, seismic body waves can still contribute significantly to NN in surface detectors, and they might be the dominant source of gravity fluctuations in underground detectors. In this paper, we present the first detailed analysis of coherent cancellation of NN from body waves. While the required number of seismometers to achieve a certain level of noise suppression is higher than for seismic surface waves, we show that optimal seismometer arrays can greatly reduce body-wave NN. The optimal array configurations and achieved residuals depend strongly on the composition of the seismic field in terms of average compressional-wave and shear-wave content. We propose Newtonian-noise cancellation to achieve the ambitious low-frequency target of the ET.



Broadband
optimization:

\sqrt{R}

1

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!!!
WHAT ABOUT VIRGO?

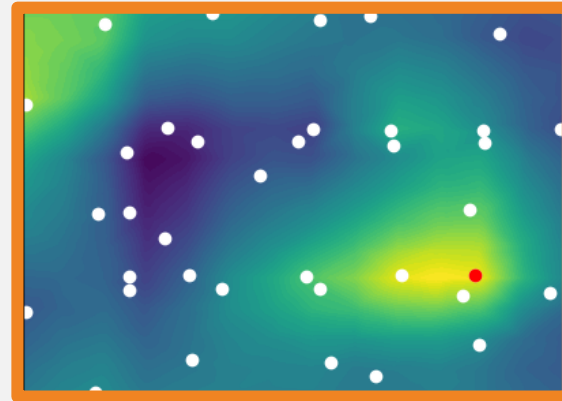
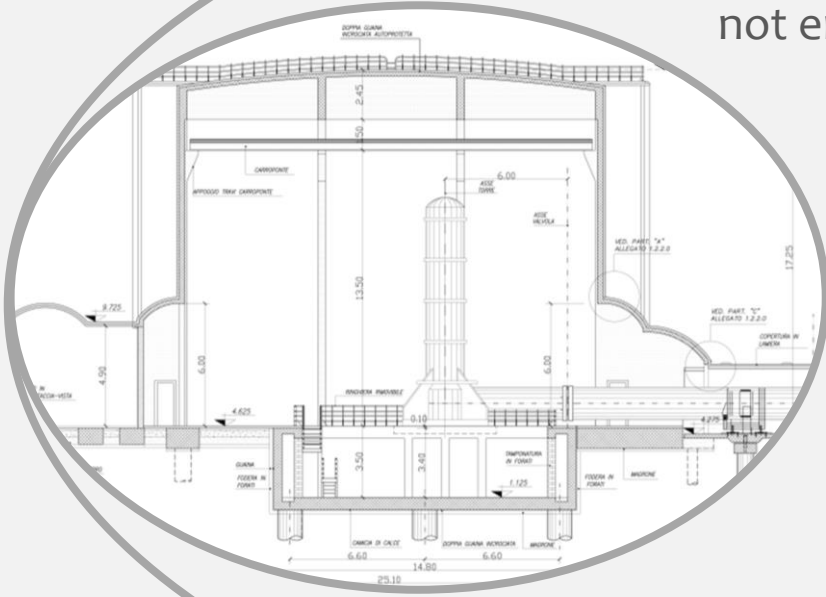


Broadband
optimization

Virgo: Newtonian Noise from **body AND** surface seismic waves

Virgo end buildings are **complex**. A fitted model is not enough.

We can base our optimization on **seismic data**

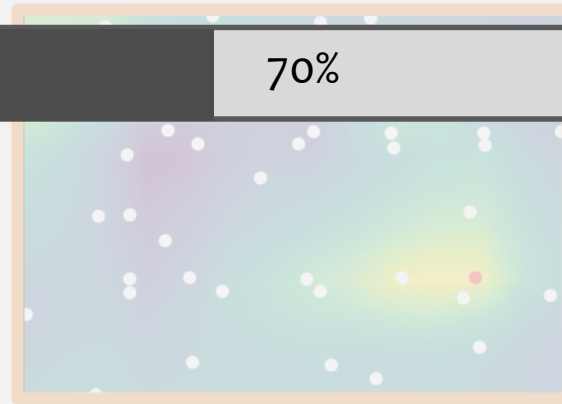


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Work in progress...

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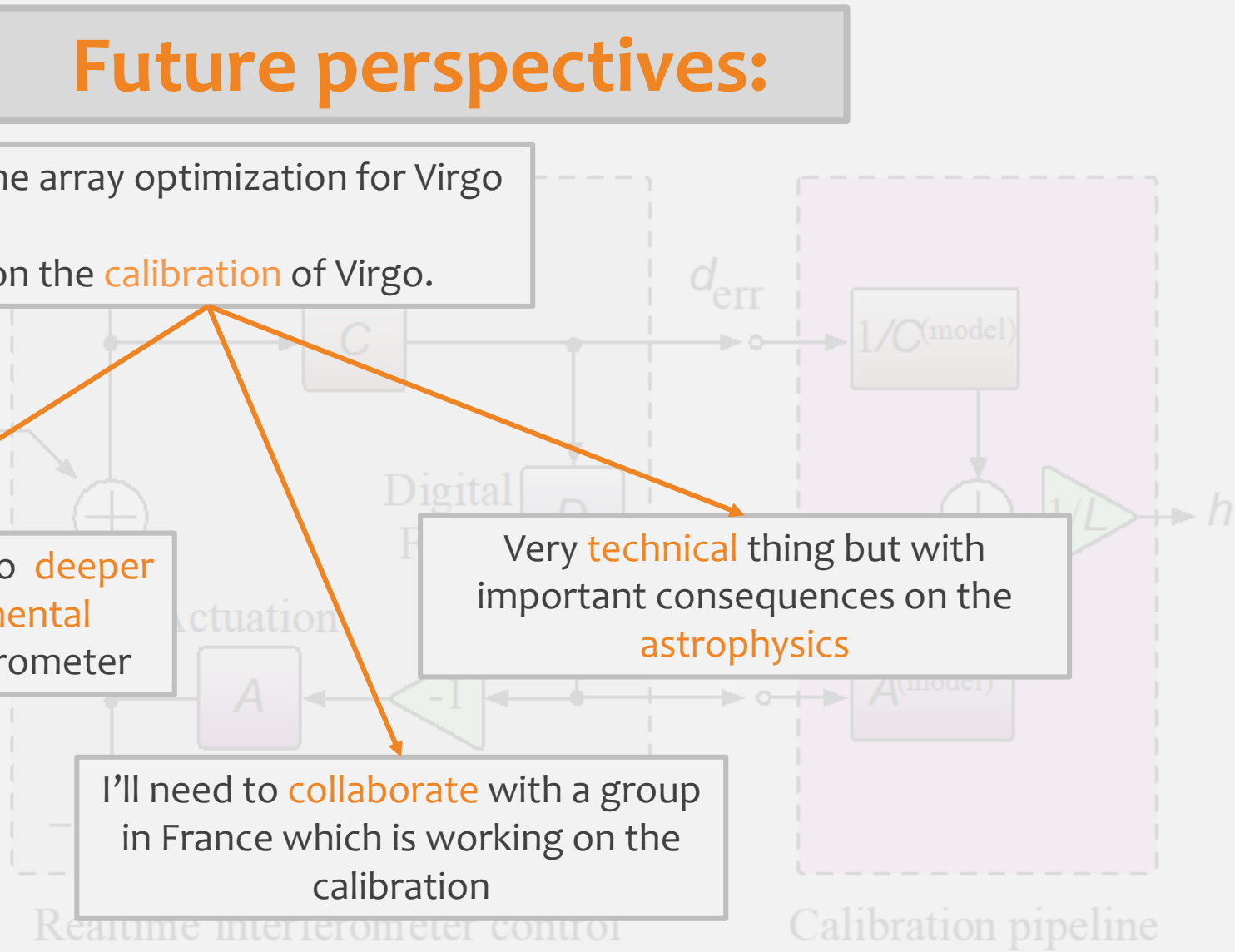
Future perspectives:

- Finishing the work on the array optimization for Virgo
- Starting a new project on the **calibration** of Virgo.

It will give me the chance to **deeper understand** the **fundamental** functioning of the interferometer

Very **technical** thing but with important consequences on the **astrophysics**

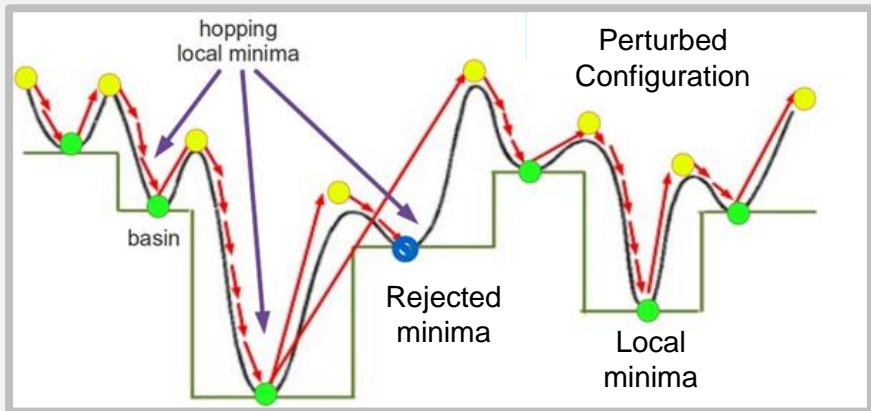
I'll need to **collaborate** with a group in France which is working on the calibration



*Thank you for
your attention*

Optimization algorithms:

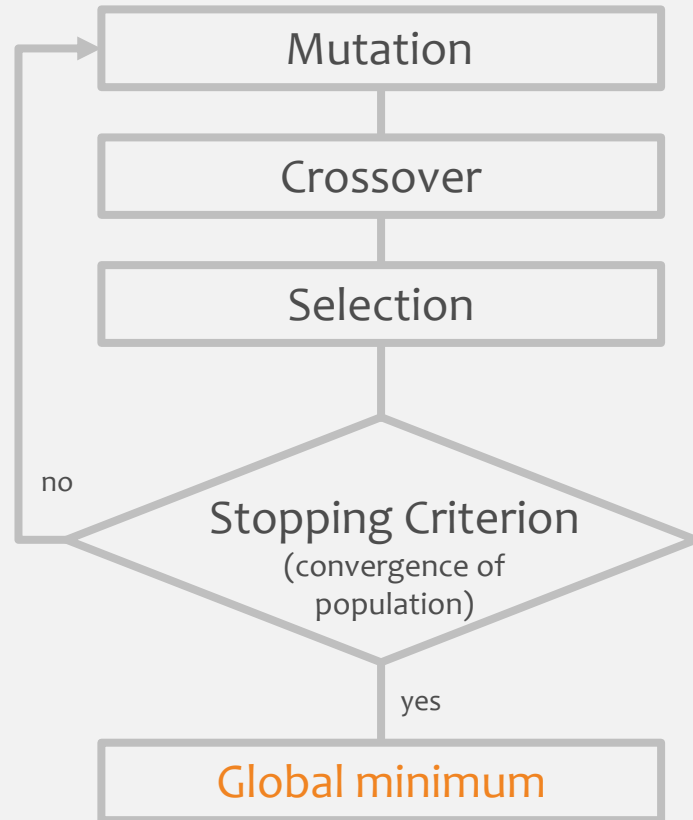
Basin Hopping:



- 1) Perturbation
- 2) Local minimization
- 3) Acceptance/Rejection

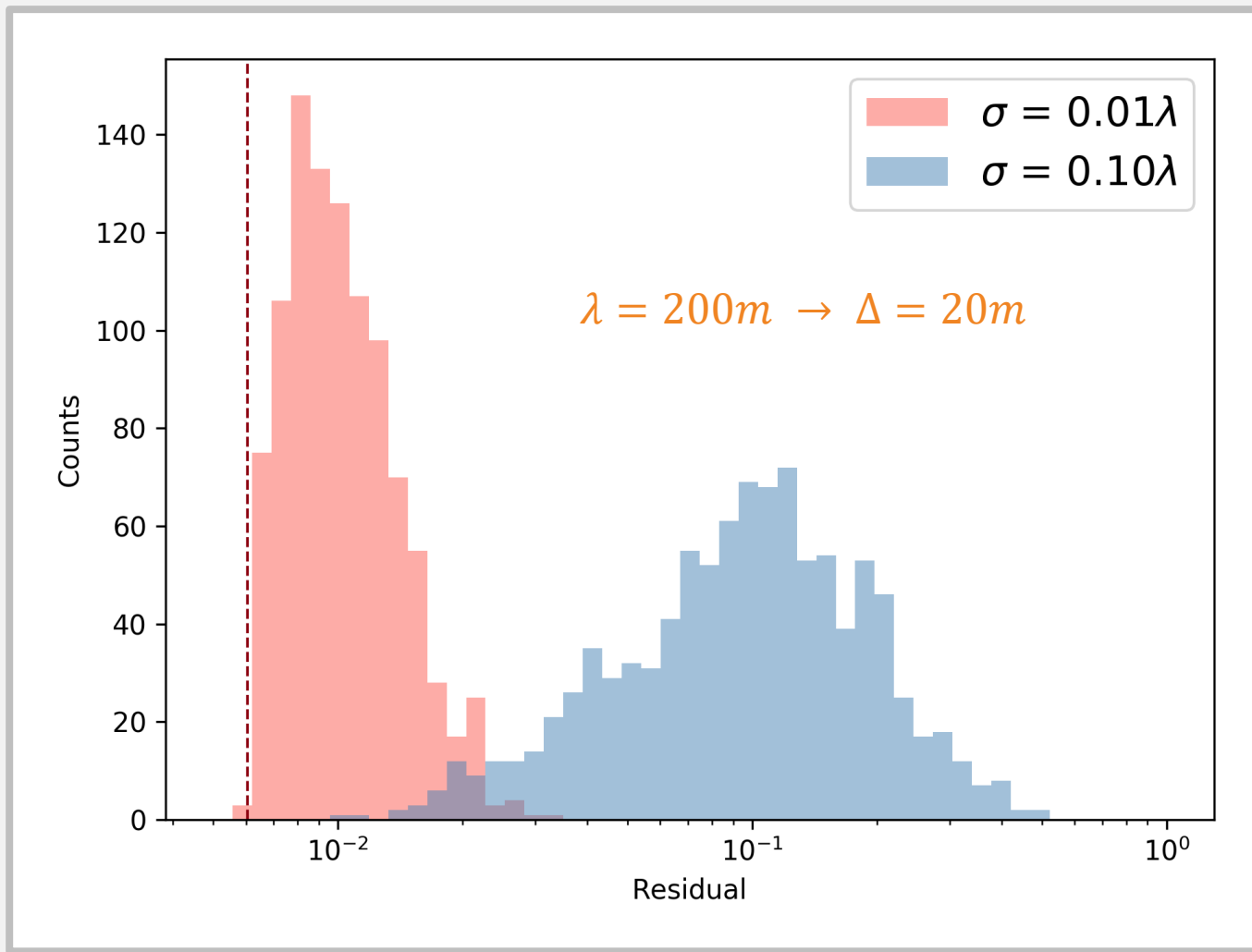
Metropolis

Differential Evolution:



Rayleigh, $N = 6$

Already limited by the self noise



↓
This entails a worse NN reduction for a degraded array configuration

What about 4d interpolation?

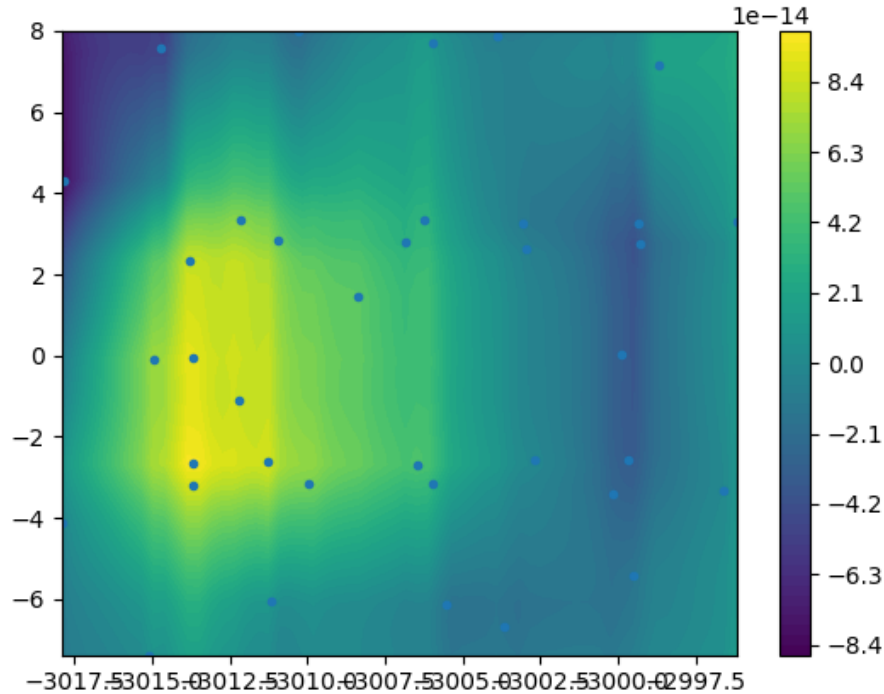
Convolution theorem:

$$\text{CPSD}(s_1, s_2) = \langle (F x_1(\omega) * F x_2(\omega)) \rangle$$

For each seismometer take N samples in the data \rightarrow FFT

For each sample period calculate the interpolation of the $\text{FFT}(\omega)$ in the 2D space

Calculate $\text{CPSD}(s_1, s_2) = \text{CPSD}(x_1, y_1, x_2, y_2)$ (just one element of the matrix)



CPSD of the 30° sensor