

2nd Year Report

Stefan Grimm

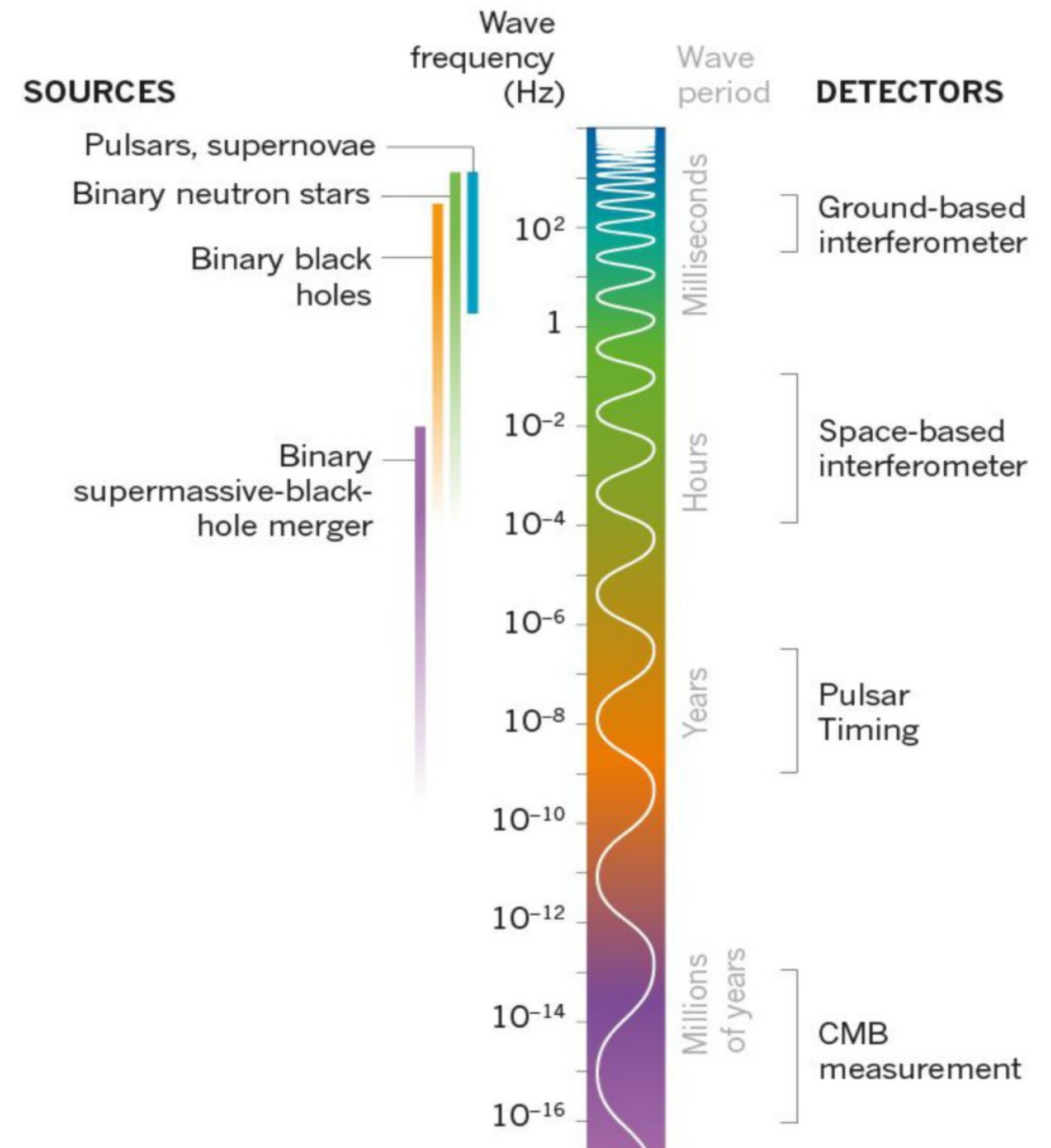
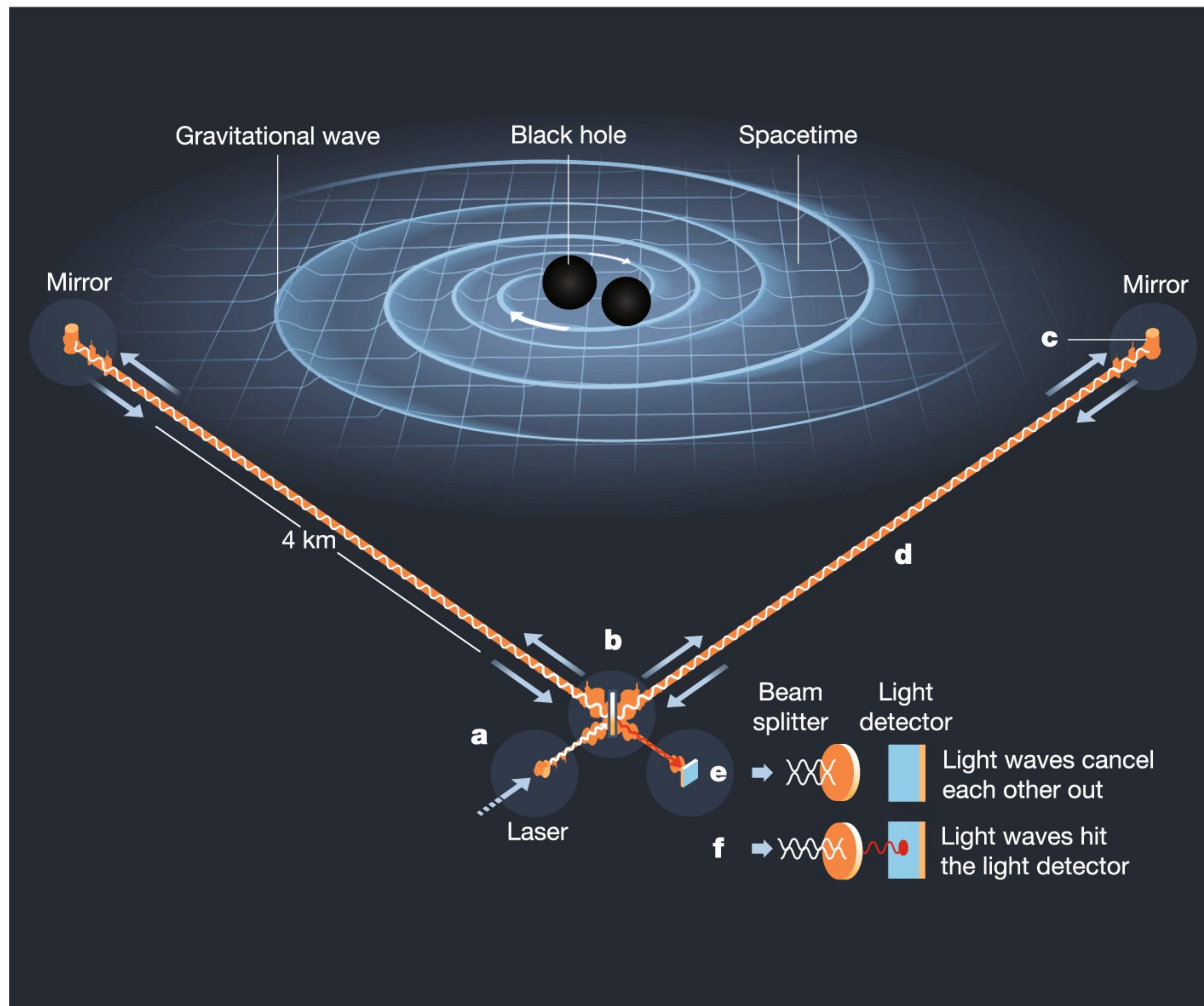


Istituto Nazionale di Fisica Nucleare

Structure

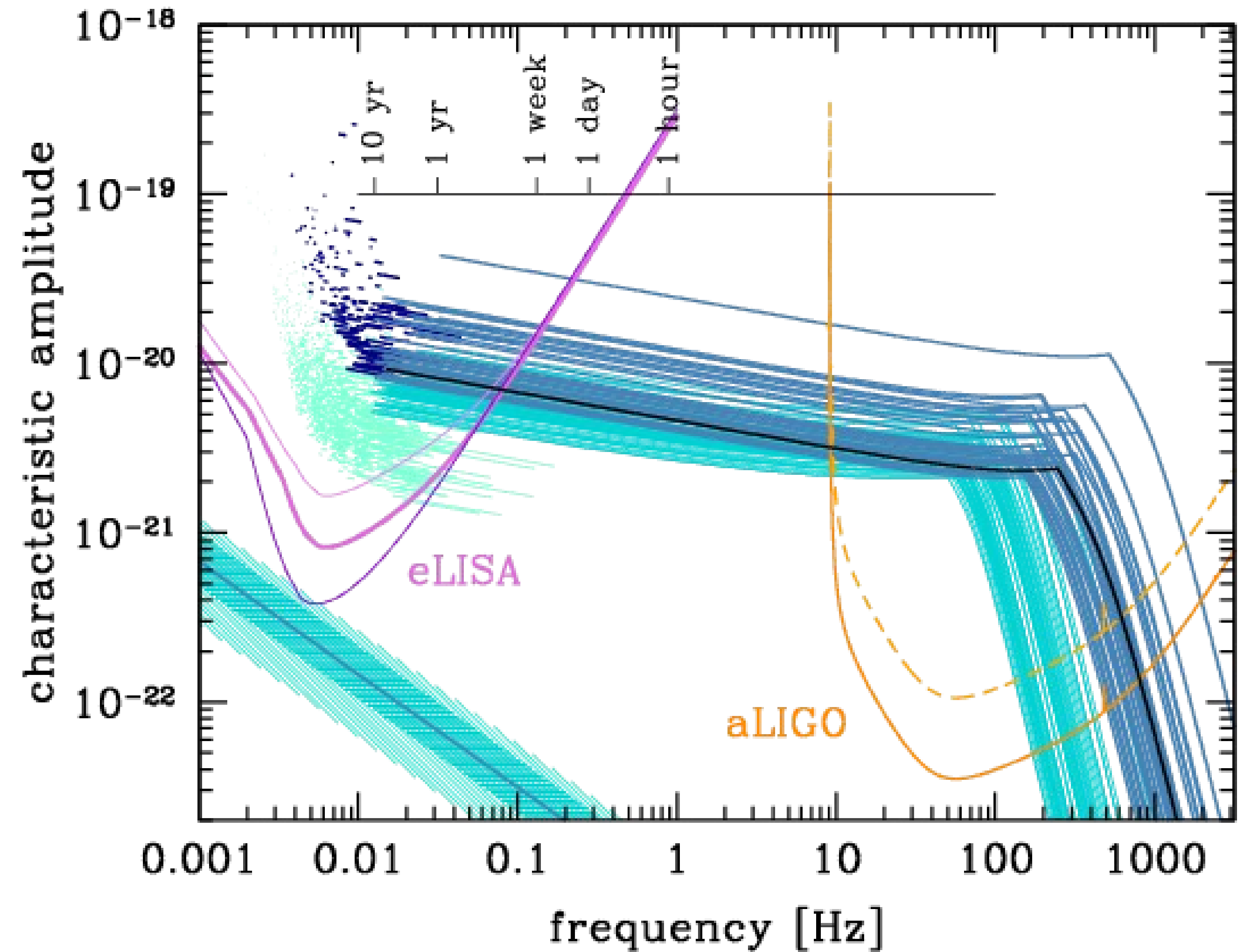
- Introduction
- Detectors
- Fisher-matrix formalism
- Analysis framework
- Segmented Fourier Transform
- Results:
 - Stellar-mass BBHs
- Conclusion

Introduction – GW Detection

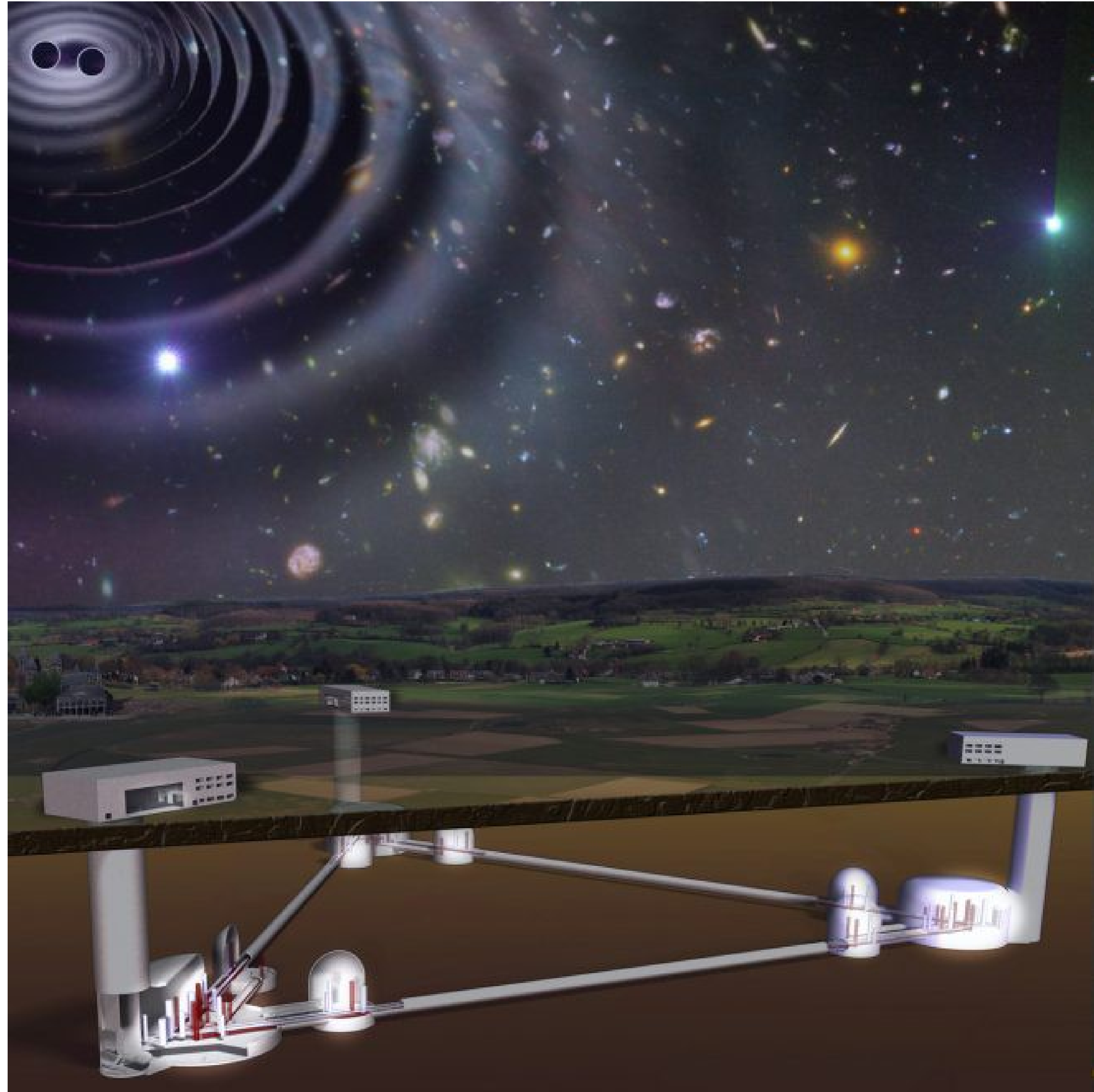


Introduction – Multiband approach

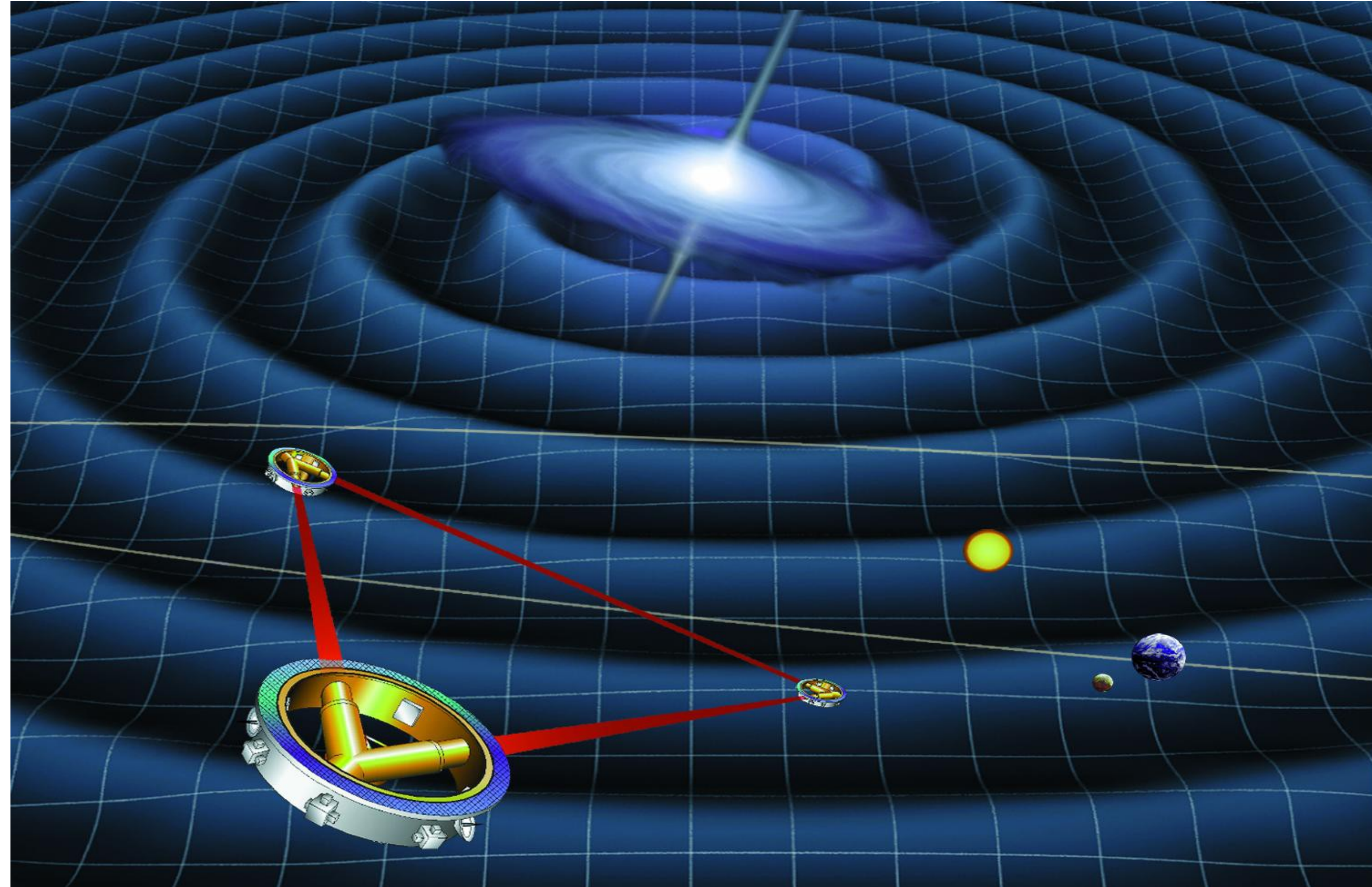
- Parameter estimation
- Multimessenger studies
- Testing GR



Introduction - Future Detectors



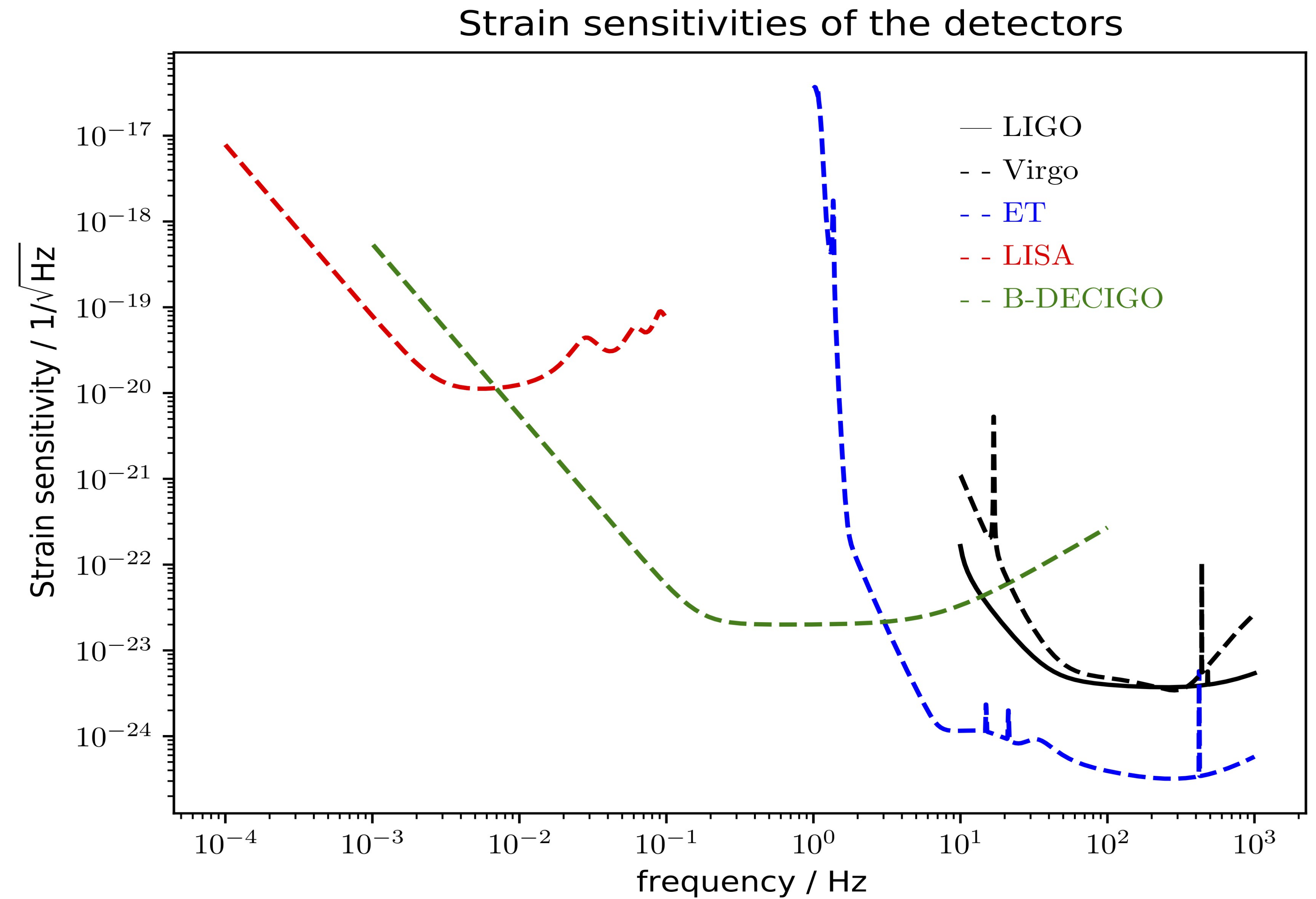
Einstein Telescope (ET)



Laser Interferometer Space Antenna
(LISA)

Detectors

- LIGO/Virgo detector network
- ET
- LISA
- B-DECIGO
 - geostationary orbit
- B-DECIGO
 - LISA-like orbit



Fisher-matrix formalism

- Signal in detector

$$s = h(\theta) + n$$

- Noise-weighted inner product

$$(a, b) = 4 \Re \int_0^\infty \frac{a(f) b^*(f)}{S_n(f)} df$$

- Likelihood

$$P(s, \theta) \propto \exp(-(s - h(\theta), s - h(\theta))/2)$$

- Expand around true source parameters

- Fisher-matrix

$$F_{kj} = (\partial_k h(\theta = \theta_0), \partial_j h(\theta = \theta_0))$$

- Standard deviation

$$\Delta \theta_i = \sqrt{(F^{-1})_{ii}}$$

- SNR

$$\text{SNR} = \sqrt{(h, h)}$$

Analysis framework

•Metric perturbation

$$\begin{pmatrix} H_+ & H_x & 0 \\ H_x & -H_+ & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

$$H_+ = \frac{c}{2r} \left(5 \frac{M_c^5}{t_c - t} \right)^{1/4} (1 + \cos^2(\alpha)) \cos(\phi(t) + \phi_c)$$

$$H_x = \frac{c}{2r} \left(5 \frac{M_c^5}{t_c - t} \right)^{1/4} 2 \cos^2(\alpha) \sin(\phi(t) + \phi_c)$$

•Rotate into detector frame

$$H_{\text{det}} = R H R^T$$

•Project onto detector arm vectors

$$h(t) = e_1^T H_{\text{det}} e_1 - e_2^T H_{\text{det}} e_2$$

Analysis framework

- Perform Fourier Transform

$$\partial_i h(t) \rightarrow \partial_i h(f)$$

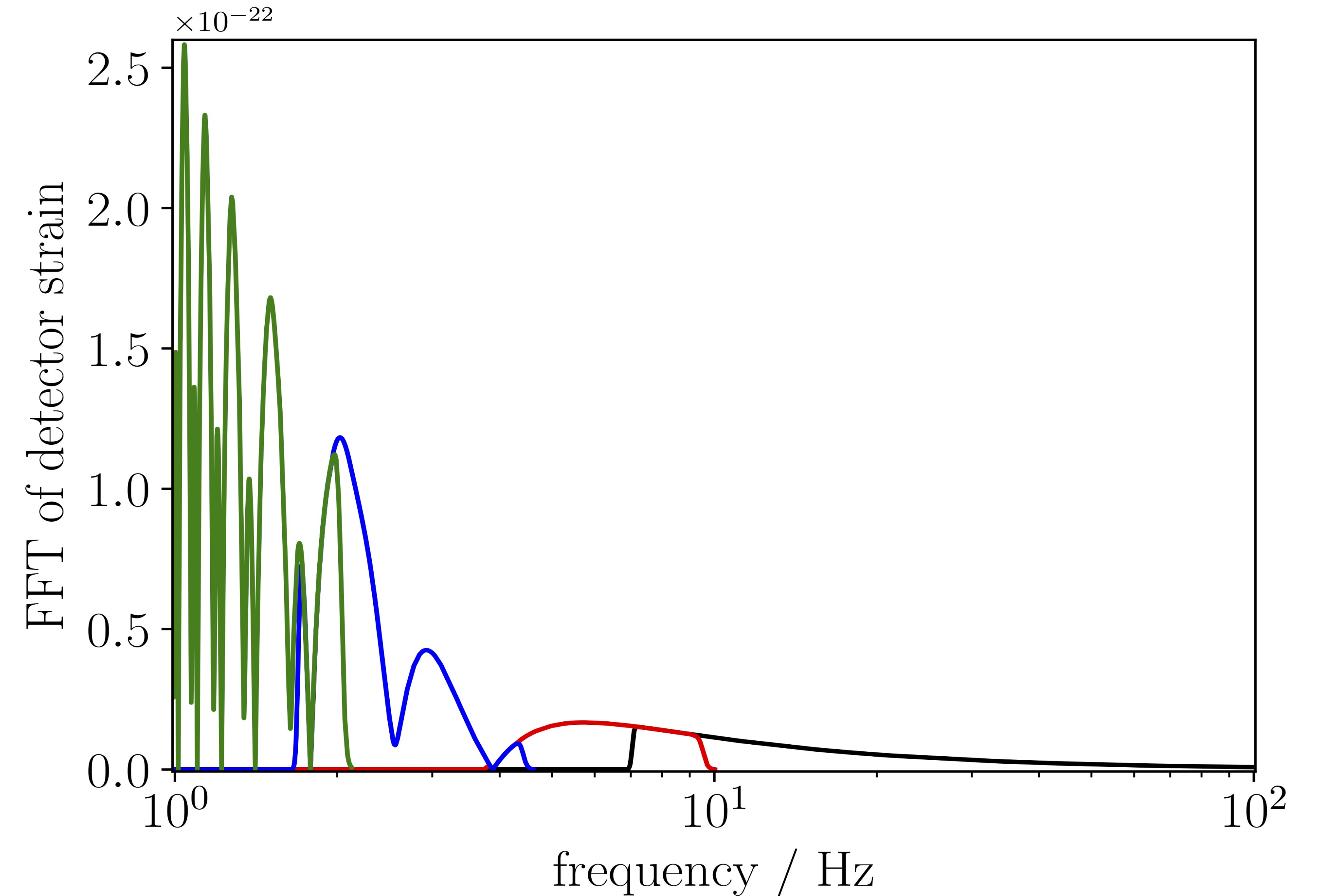
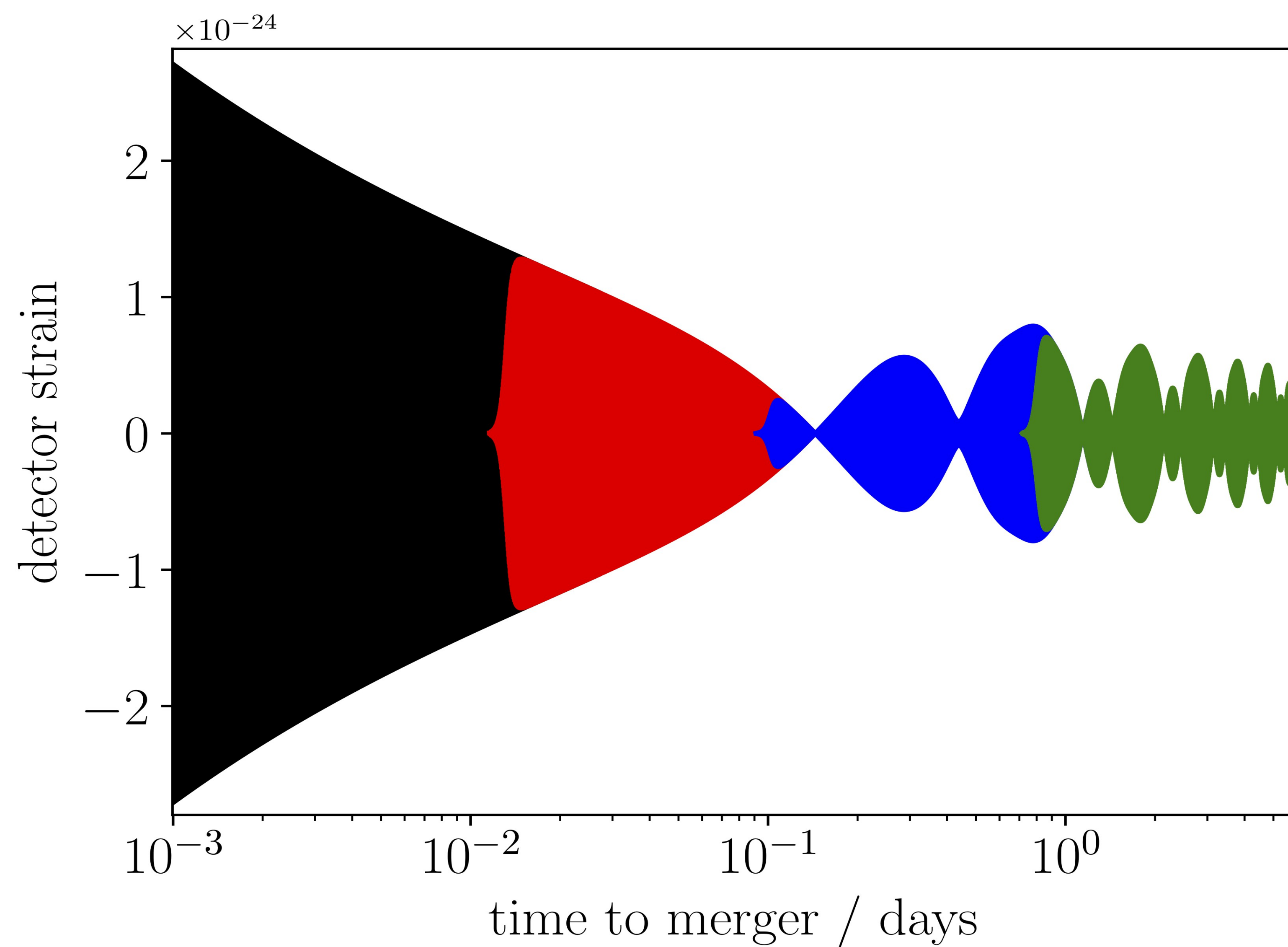
- Compute Fisher matrix

$$F_{kj} = (\partial_k h, \partial_j h)$$

- Invert Fisher matrix

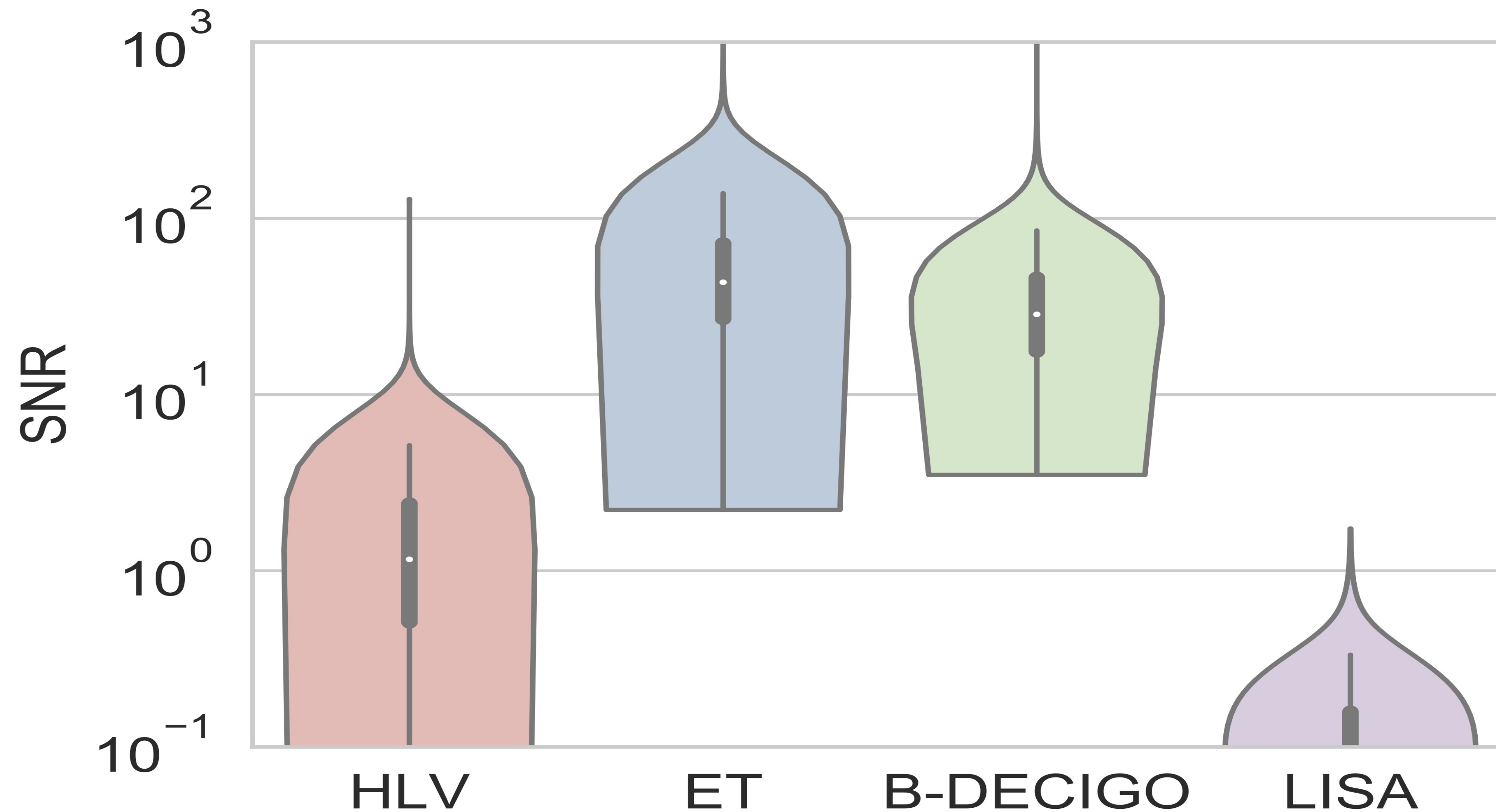
$$\Delta \theta_i = \sqrt{(F^{-1})_{ii}}$$

Segmented Fourier Transform



Choose in each segment the time resolution corresponding to the highest frequency in the segment!

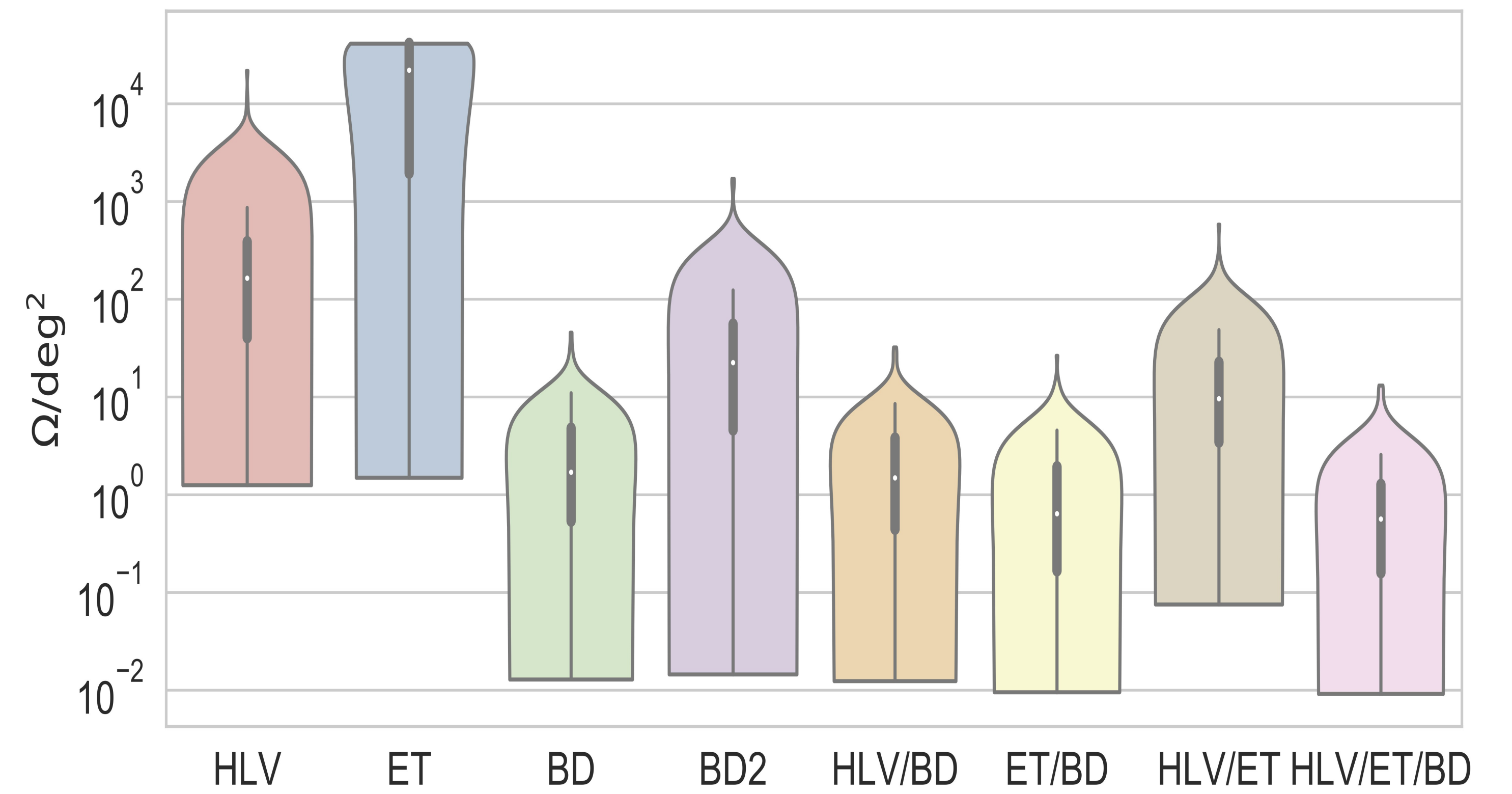
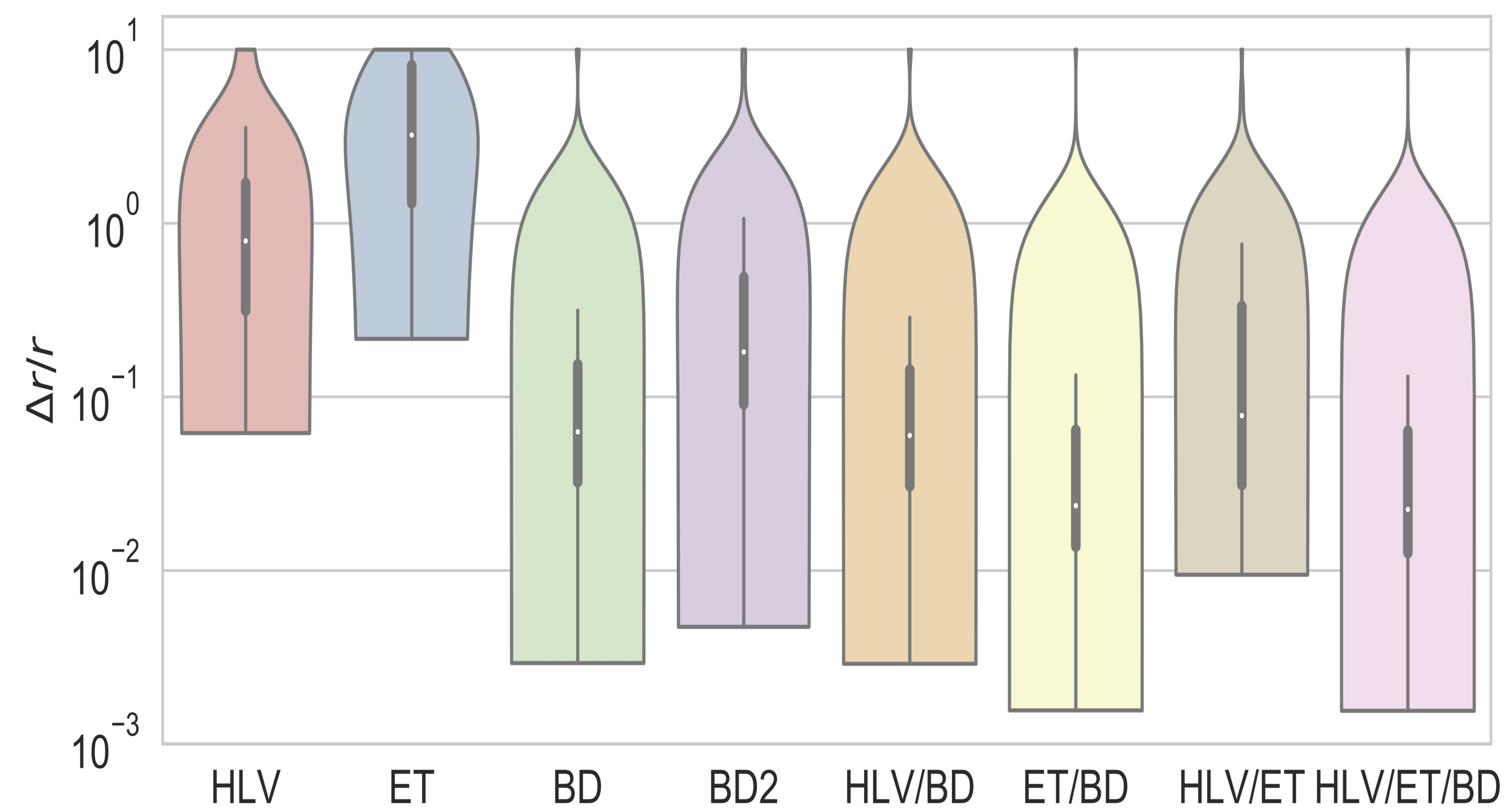
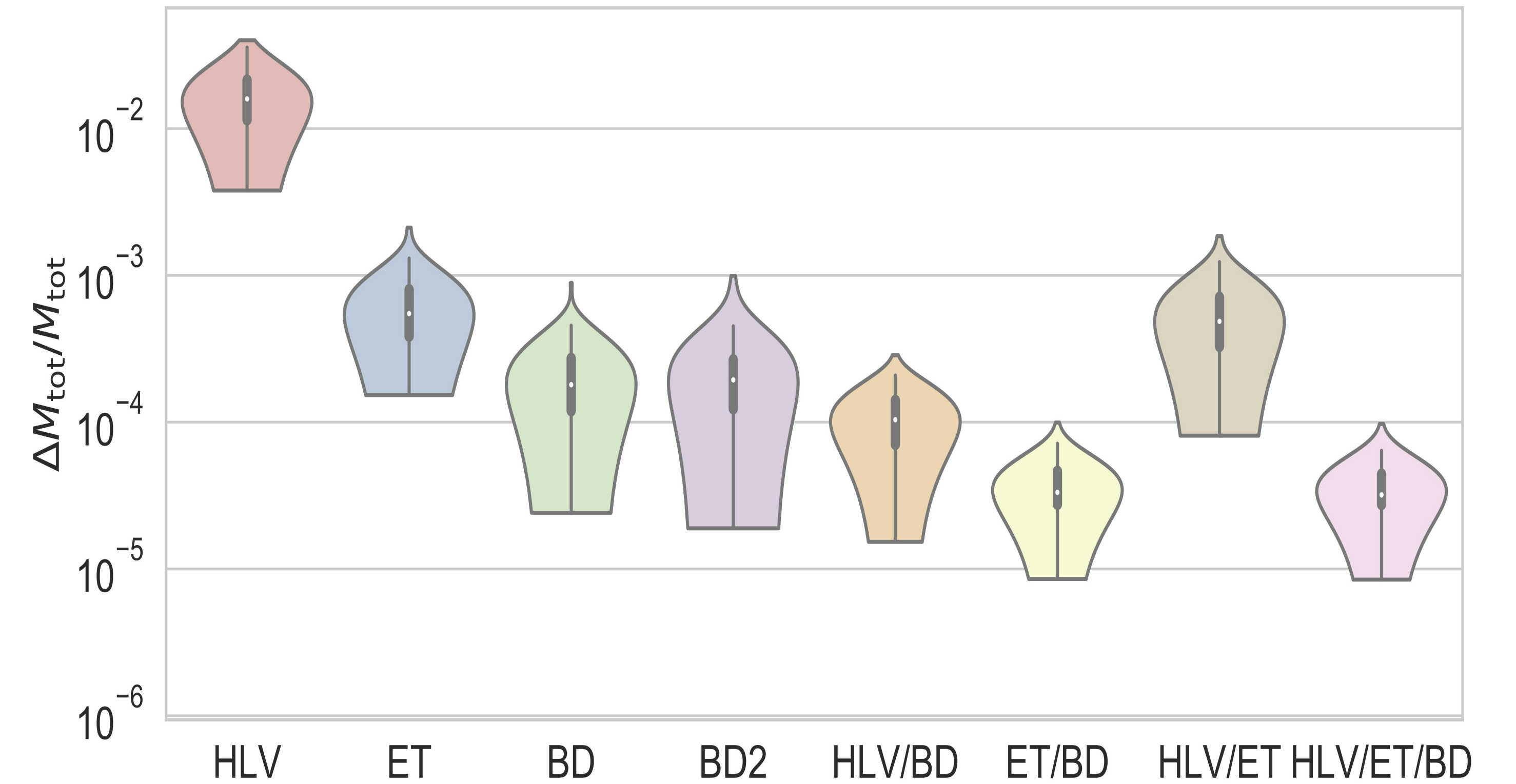
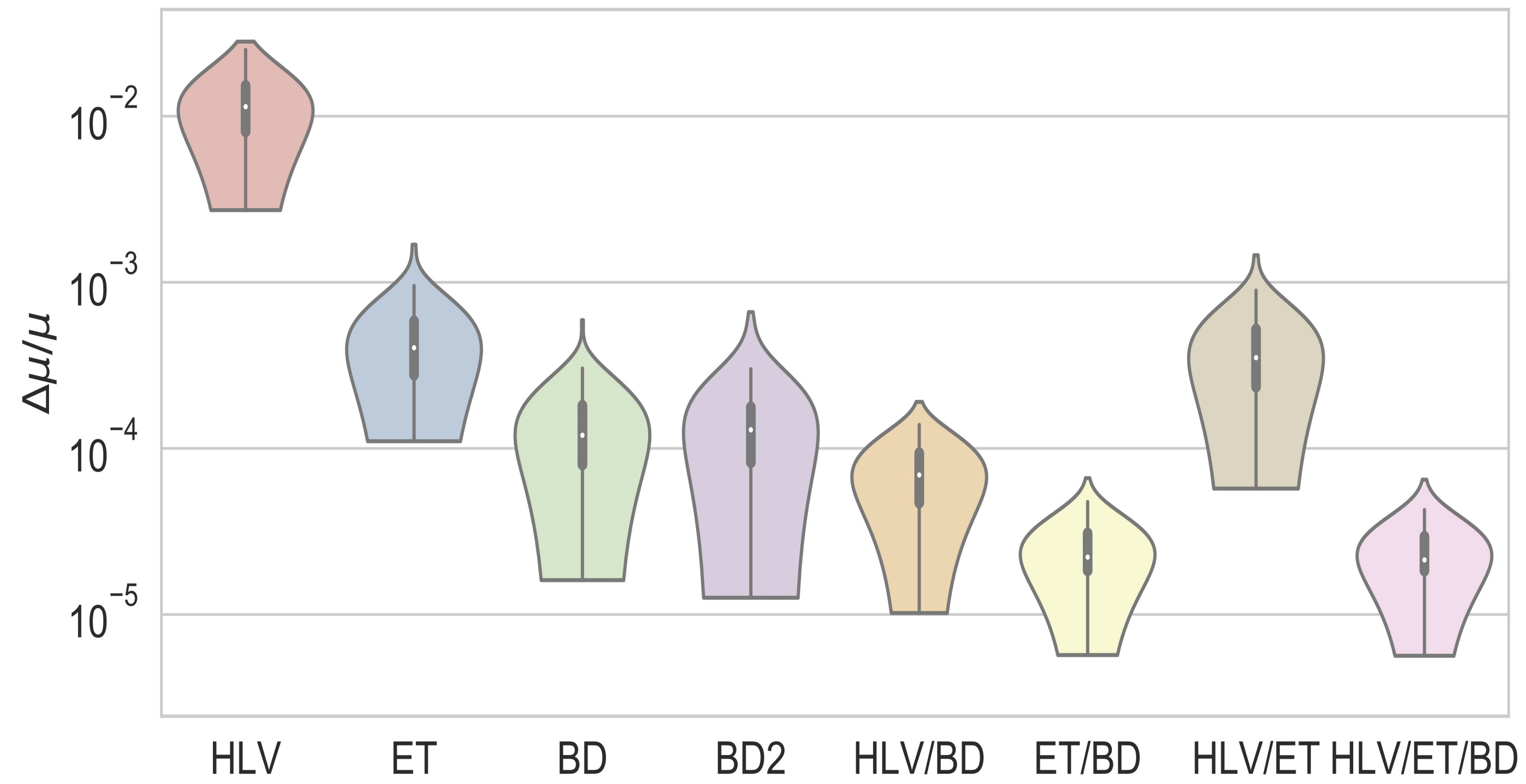
Stellar-mass BBHs: detection capabilities



SNR > 10 13/1000 968/1000 938/1000 0/1000

BBH population: mass spectrum is power-law with index -1.6 , $5 M_{\text{solar}} < M_{\text{BH}} < 60 M_{\text{solar}}$

Parameter estimates



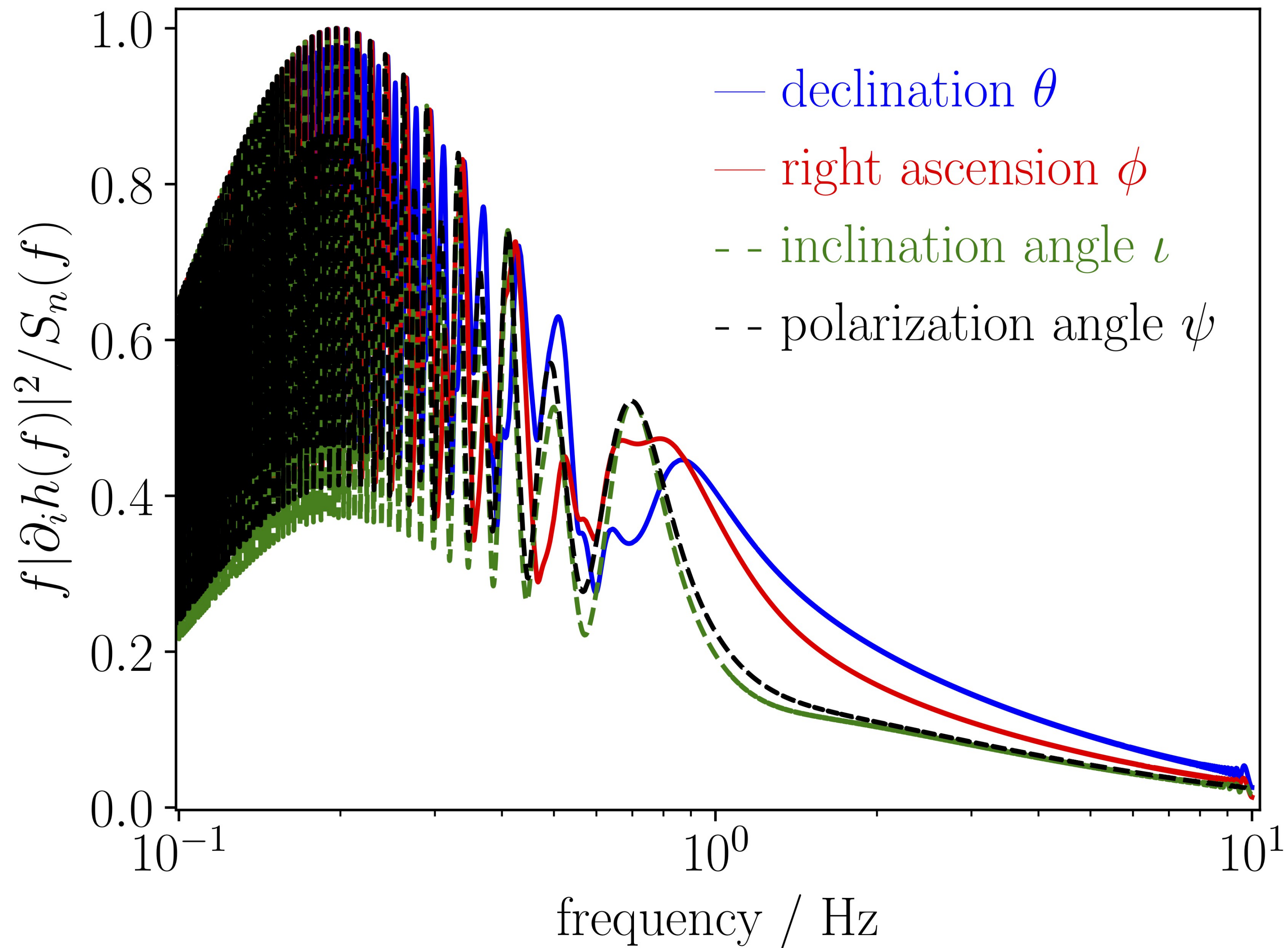
Results

- B-DECIGO: geostationary orbit is preferable over heliocentric orbit
- Estimate of mass parameters benefits from multiband parameter estimation
- LISA: no good candidate for multiband parameter estimation of stellar-mass BBHs

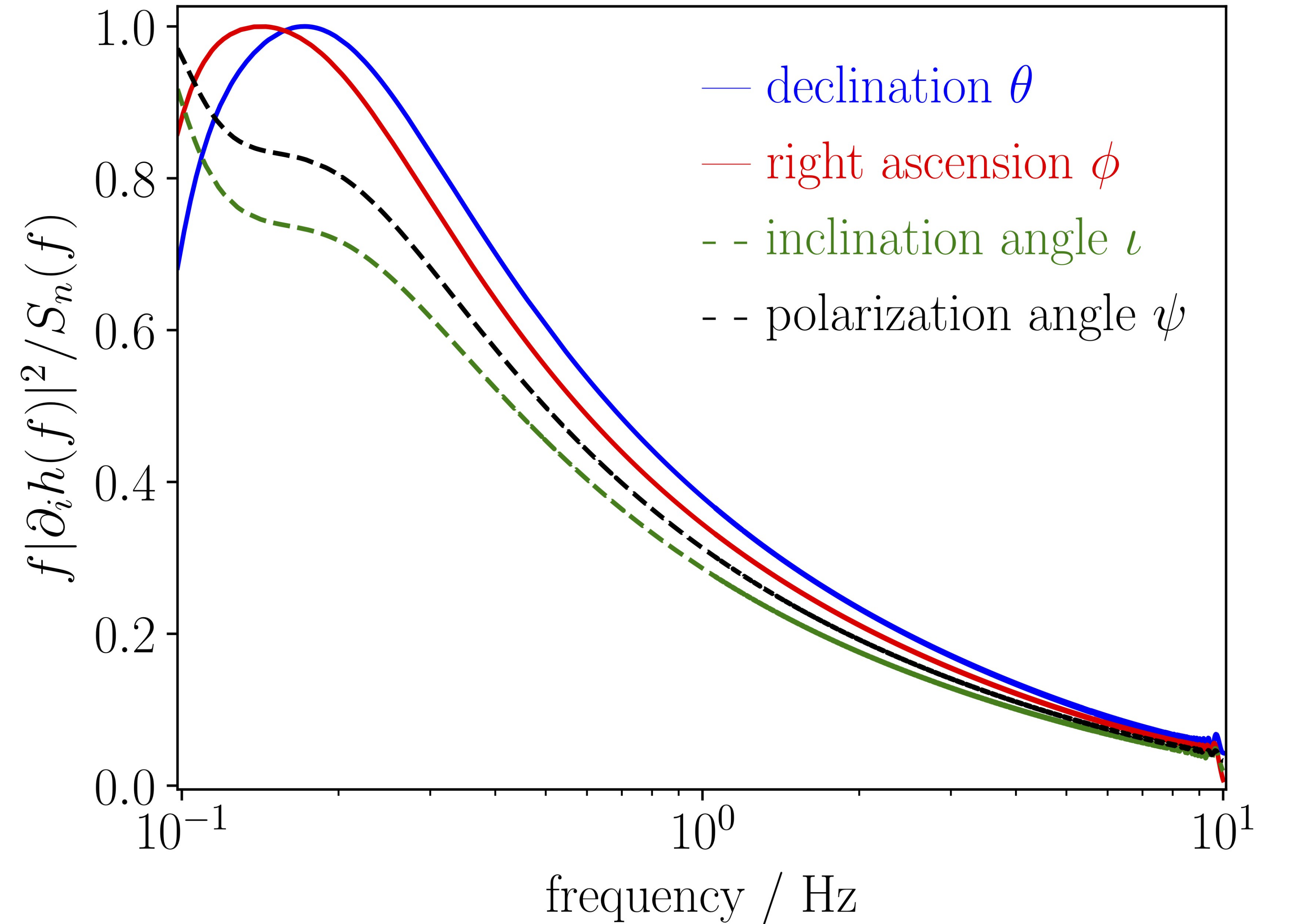
Outlook

- Investigate different detector designs
- Multi-messenger studies
- Perform studies involving large statistics

Movement effects in B-DECIGO



geostationary orbit



heliocentric orbit

Intermediate-mass BBHs: detection capabilities



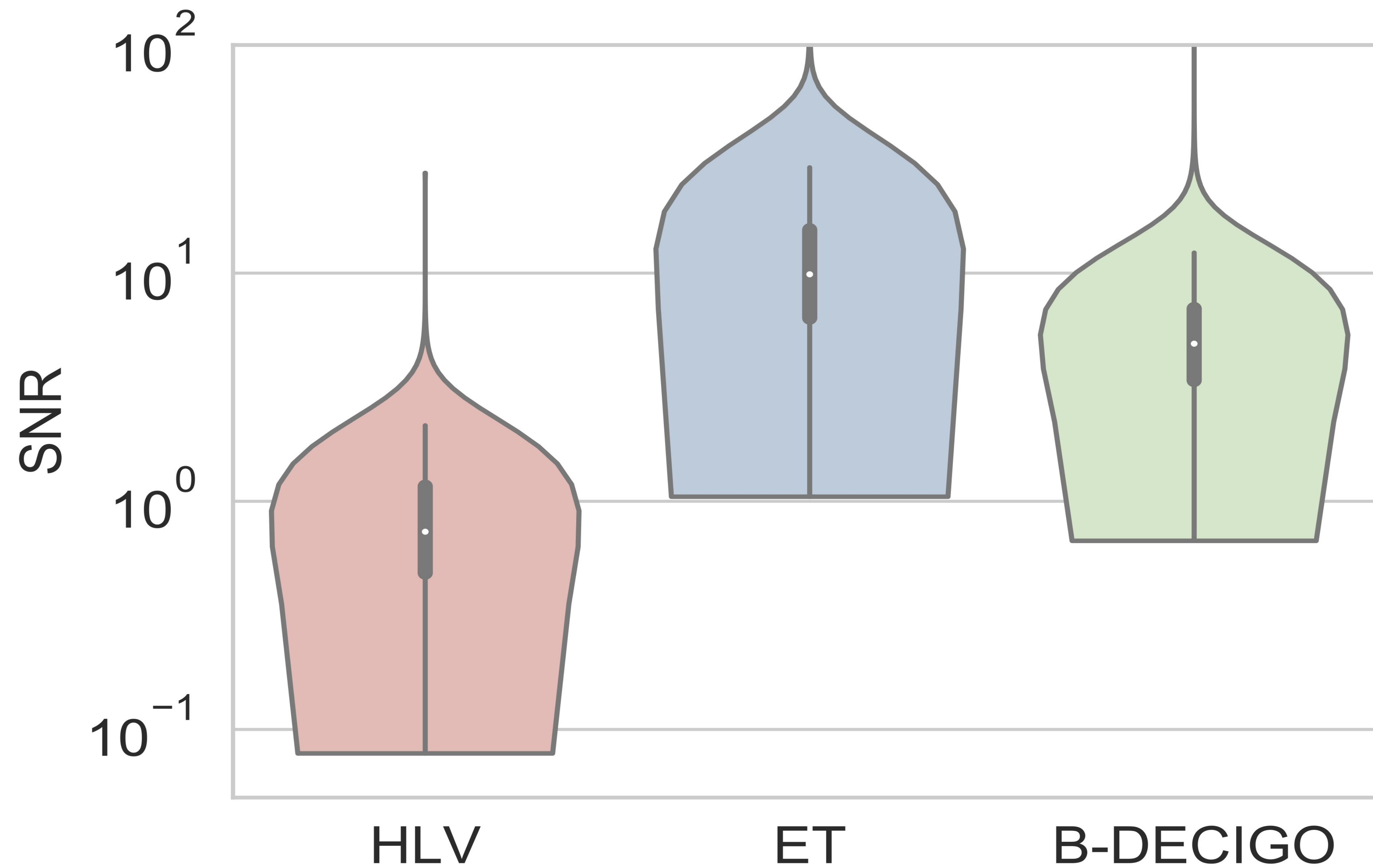
SNR > 10

241/1000

1000/1000

227/1000

Neutron star binaries: detection capabilities



SNR > 10

1/1000

492/1000

104/1000