

THE GALACTIC-EXTRAGALACTIC TRANSITION

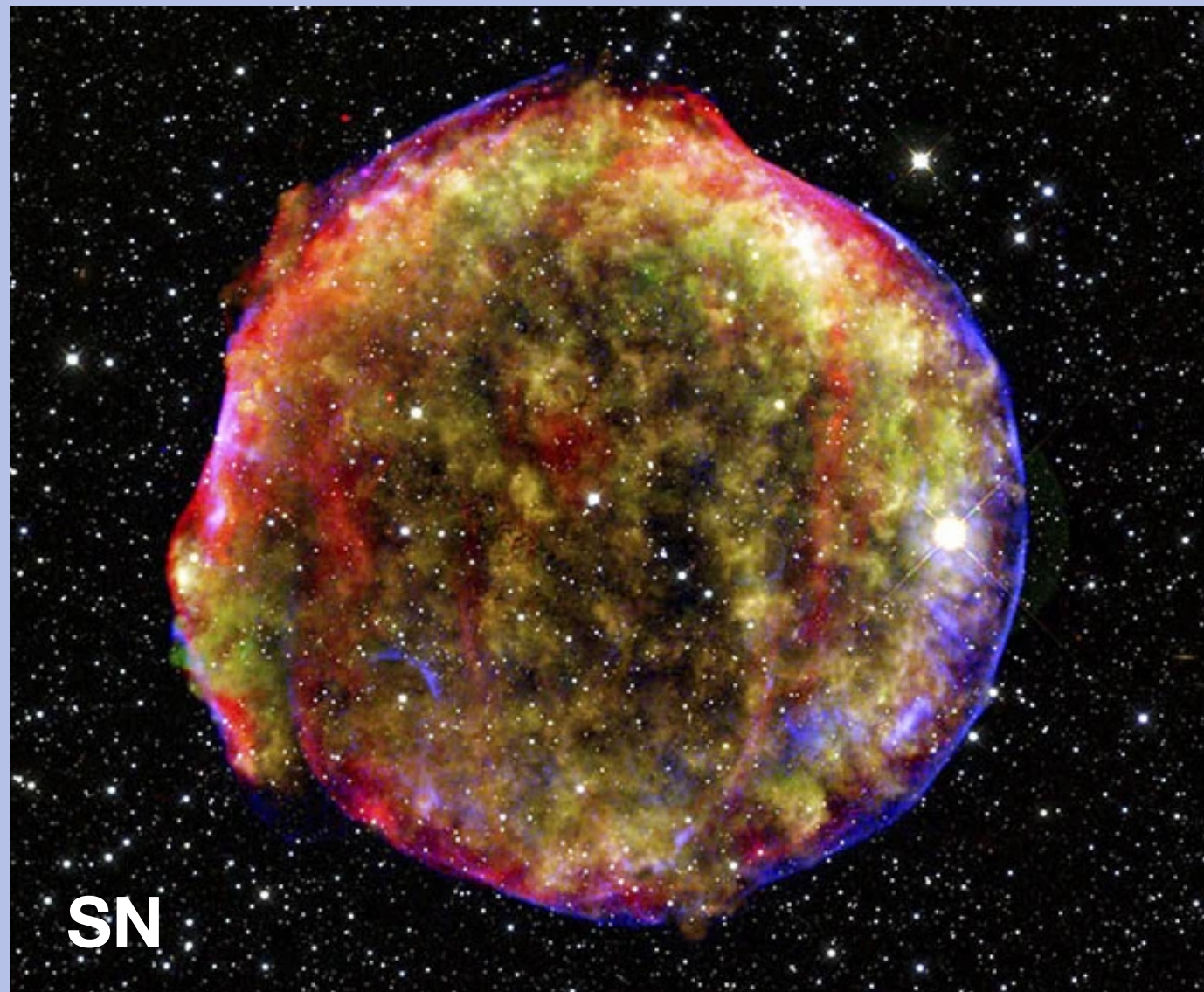
PROPAGATION OF COSMIC RAYS IN GALACTIC TURBULENT
MAGNETIC FIELDS AND MULTI-MESSENGER OBSERVATIONS



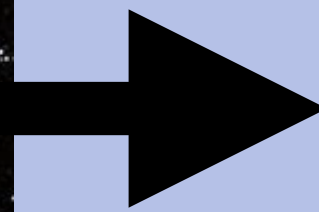
Luis Enrique Espinosa Castro
Passage of the Year 2025

Supervisors: Prof. Carmelo Evoli,
Prof. Pasquale Blasi, Dr. Giulia Pagliaroli

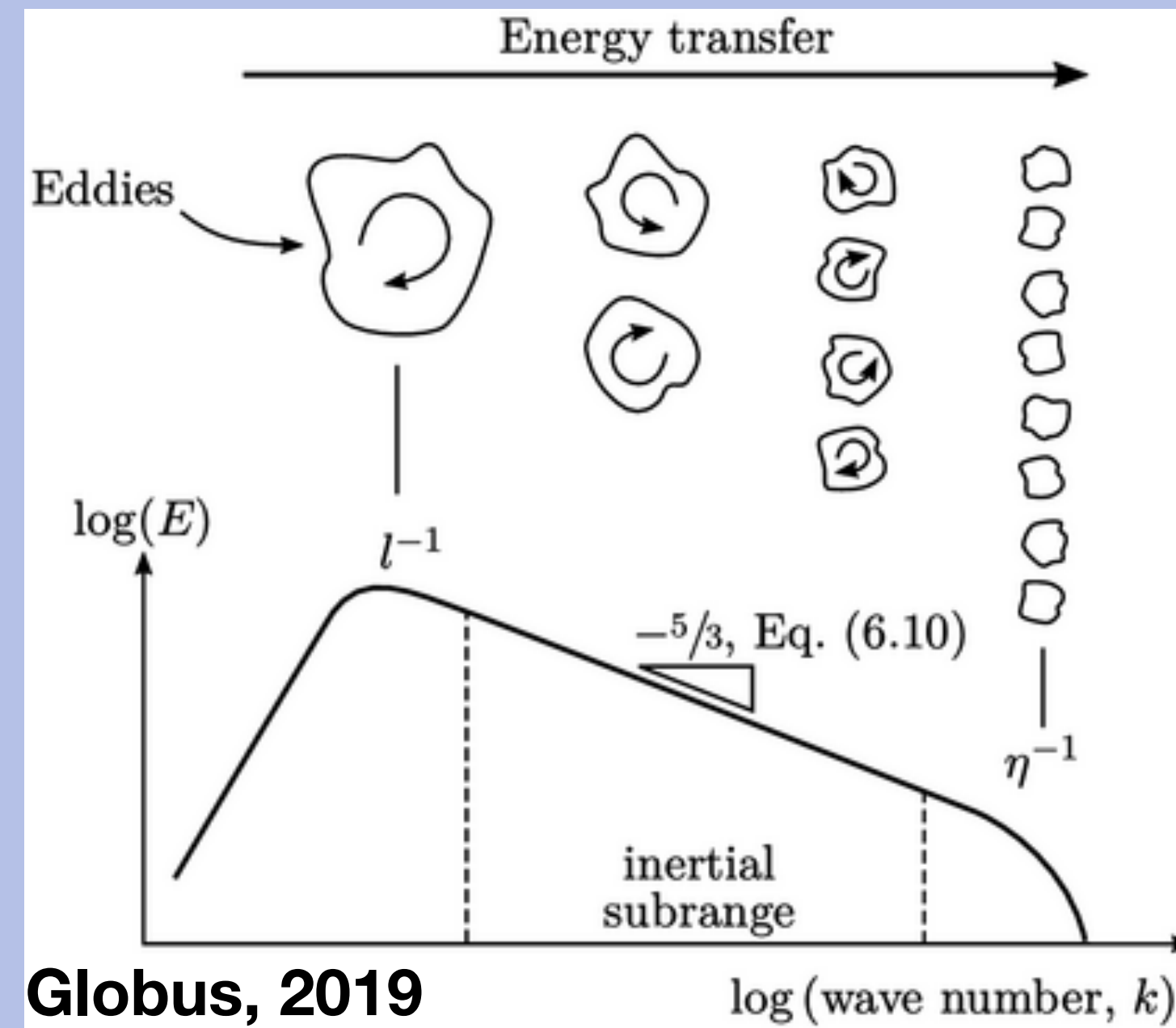
Simple paradigm of Galactic cosmic ray propagation



SN

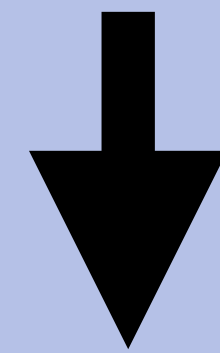


Turbulence cascade

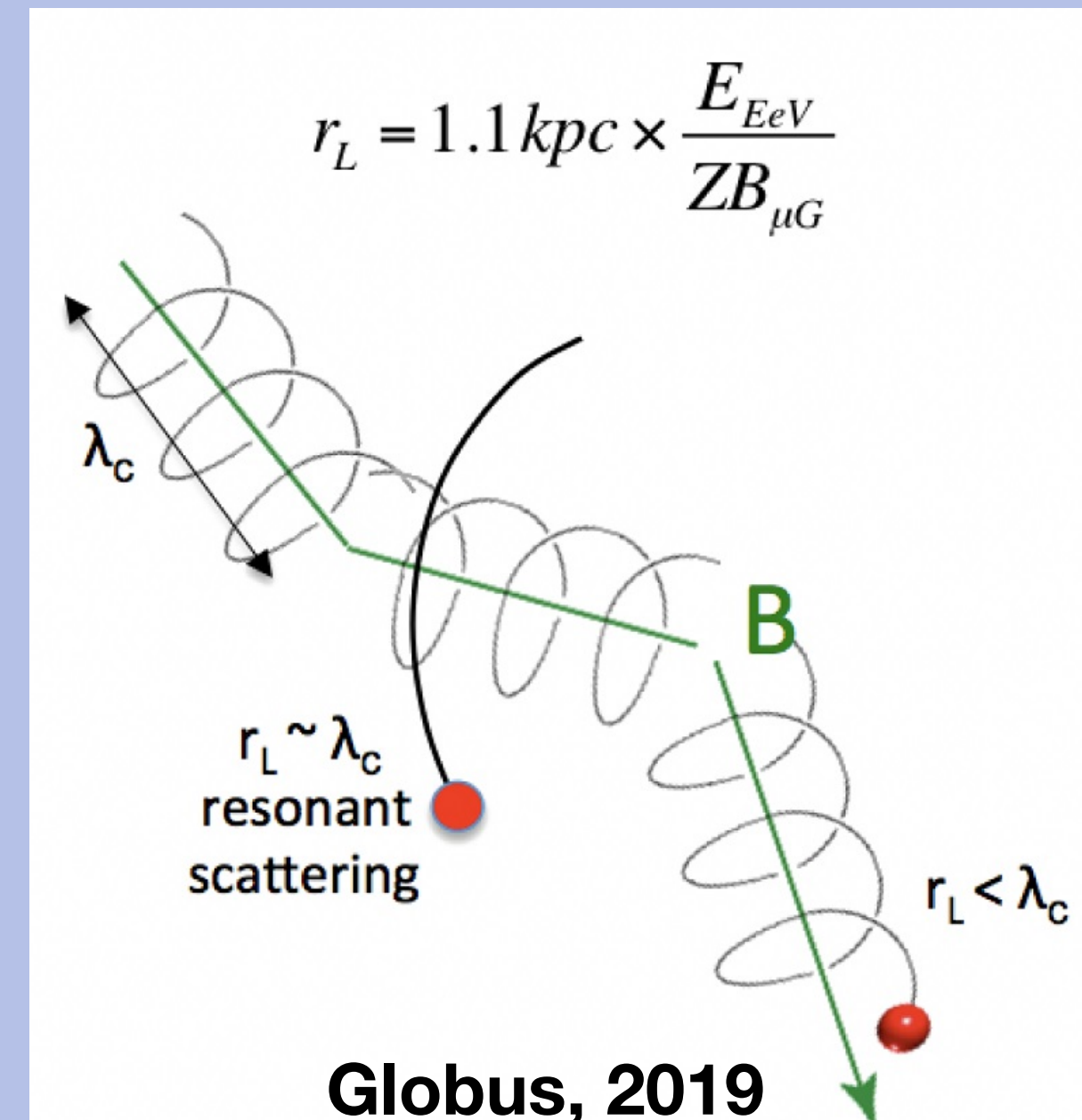


Globus, 2019

Kolmogorov spectrum $\propto k^{-5/3}$
Kraichnan spectrum $\propto k^{-3/2}$



Resonant scattering with Alfvén waves ($k_{\parallel}^{-1} \sim r_L$)



Globus, 2019

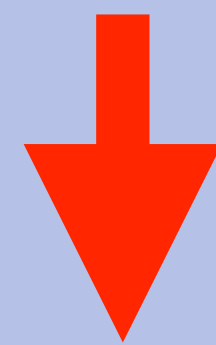
Simple description of magnetic turbulence.

More complete description of turbulence **requires MHD numerical treatment.**

Simple paradigm of Galactic cosmic ray propagation

Diffusion tensor: $D_{ij} = (D_{\parallel} - D_{\perp})b_i b_j + D_{\perp} \delta_{ij} - D_A \epsilon_{ijk} b_k$

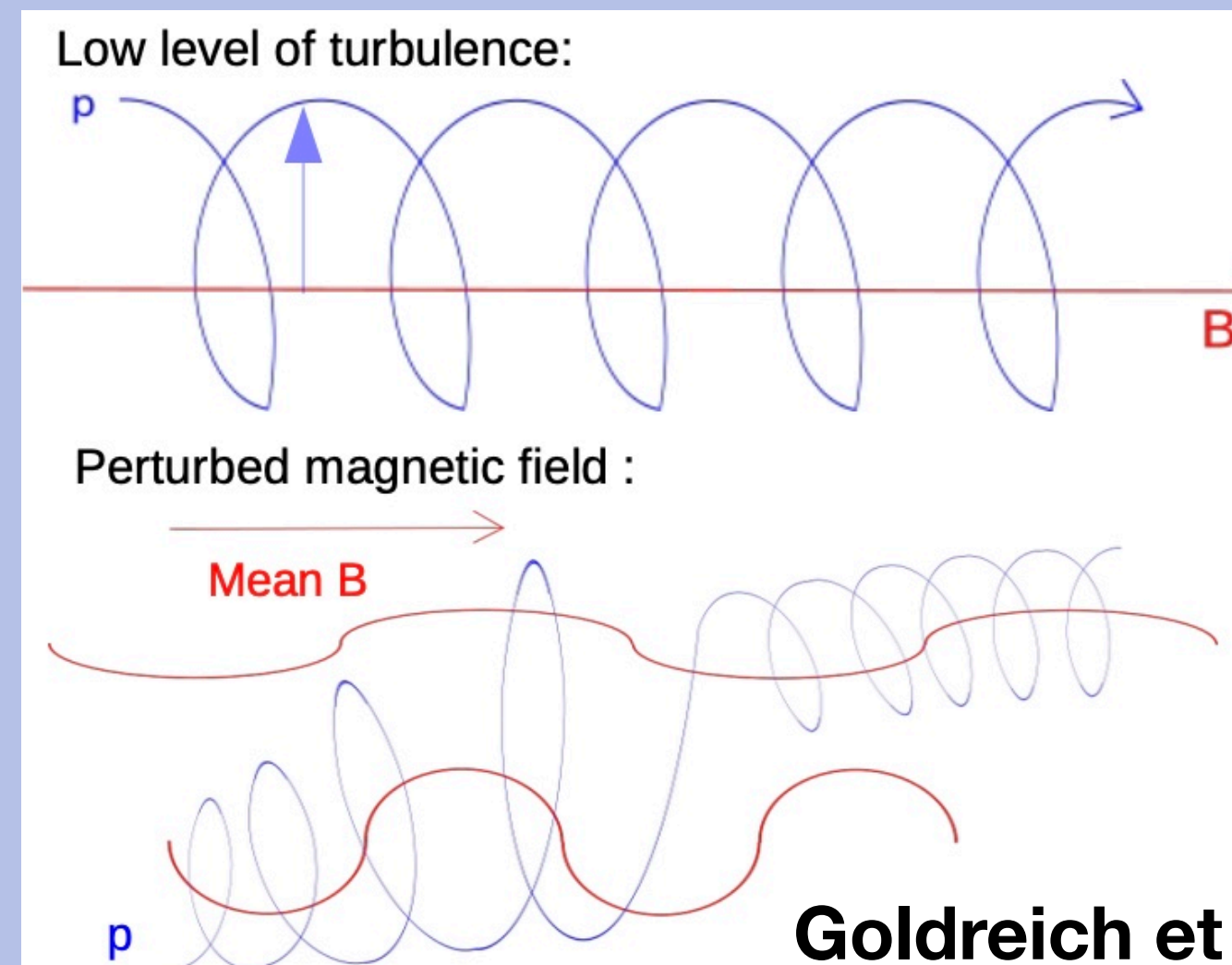
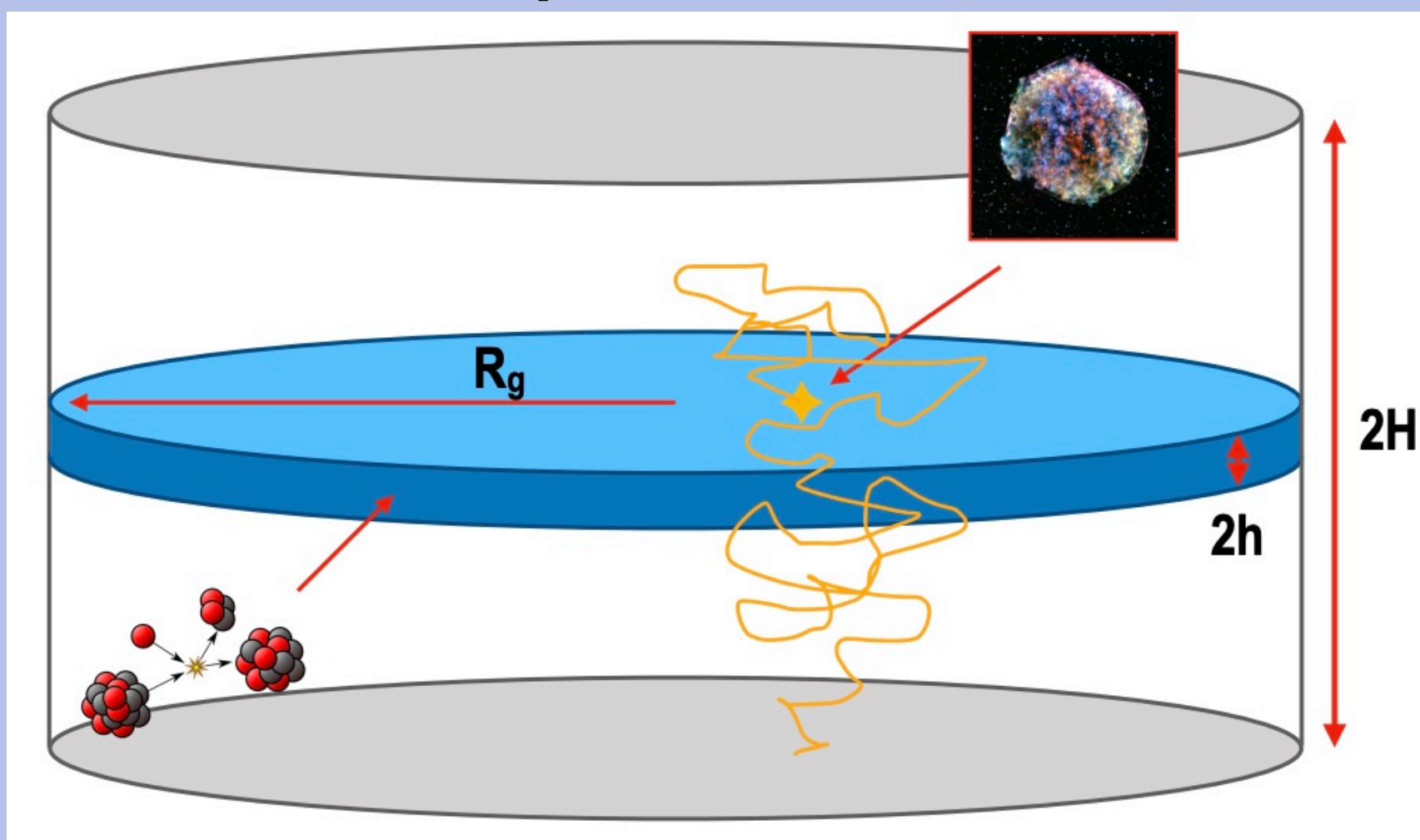
Cosmic ray transport: $-\nabla_i D_{ij}(\mathbf{r}) \nabla_j N(\mathbf{r}) = Q(\mathbf{r})$



Cylindrical coordinate system
assuming azimuthal symmetry

$$\left(-\frac{1}{r} \frac{\partial}{\partial r} \left[r D_{\perp} \frac{\partial}{\partial r} \right] - \frac{\partial}{\partial z} \left[D_{\perp} \frac{\partial}{\partial z} \right] + u_r \frac{\partial}{\partial r} + u_z \frac{\partial}{\partial z} \right) N(\mathbf{r}) = Q(\mathbf{r})$$

Evoli & Dupletsa, 2023



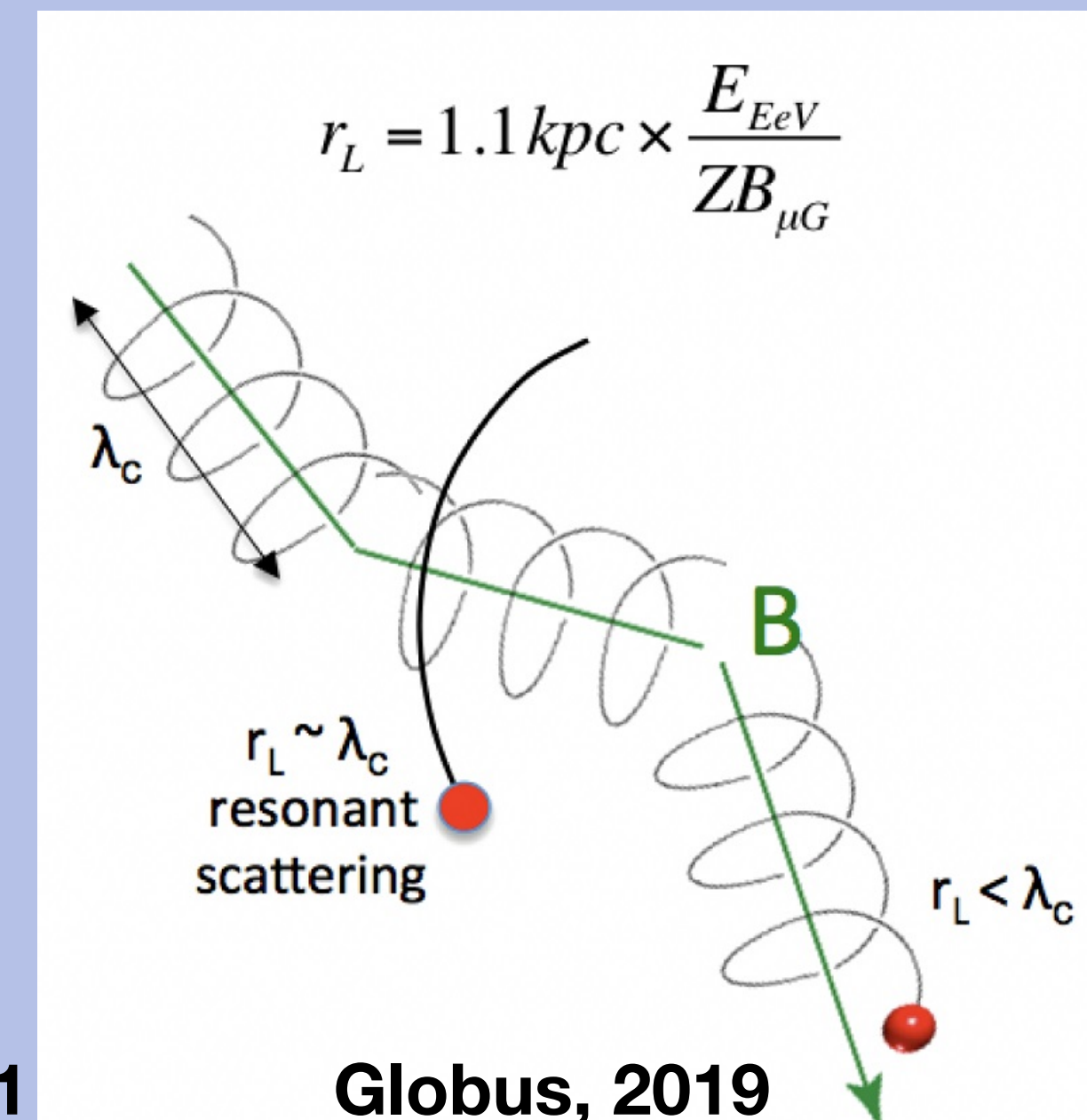
Goldreich et al., 2001

Drift velocities:

$$u_r = - \frac{\partial(D_A b_{\phi})}{\partial z}$$

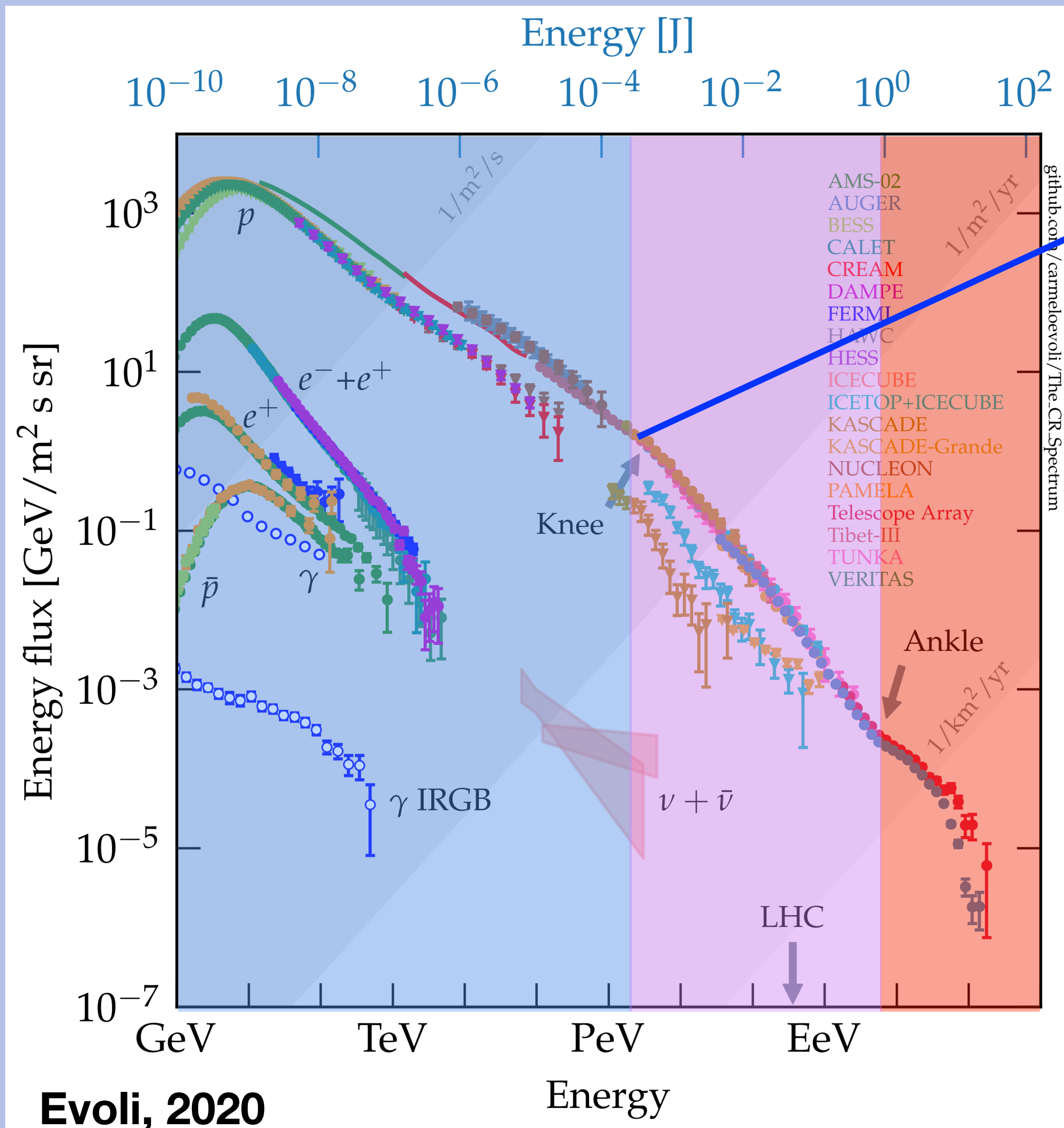
$$u_z = \frac{1}{r} \frac{\partial(r D_A b_{\phi})}{\partial r}$$

Resonant scattering with Alfvén
waves ($k_{\parallel}^{-1} \sim r_L$)



Globus, 2019

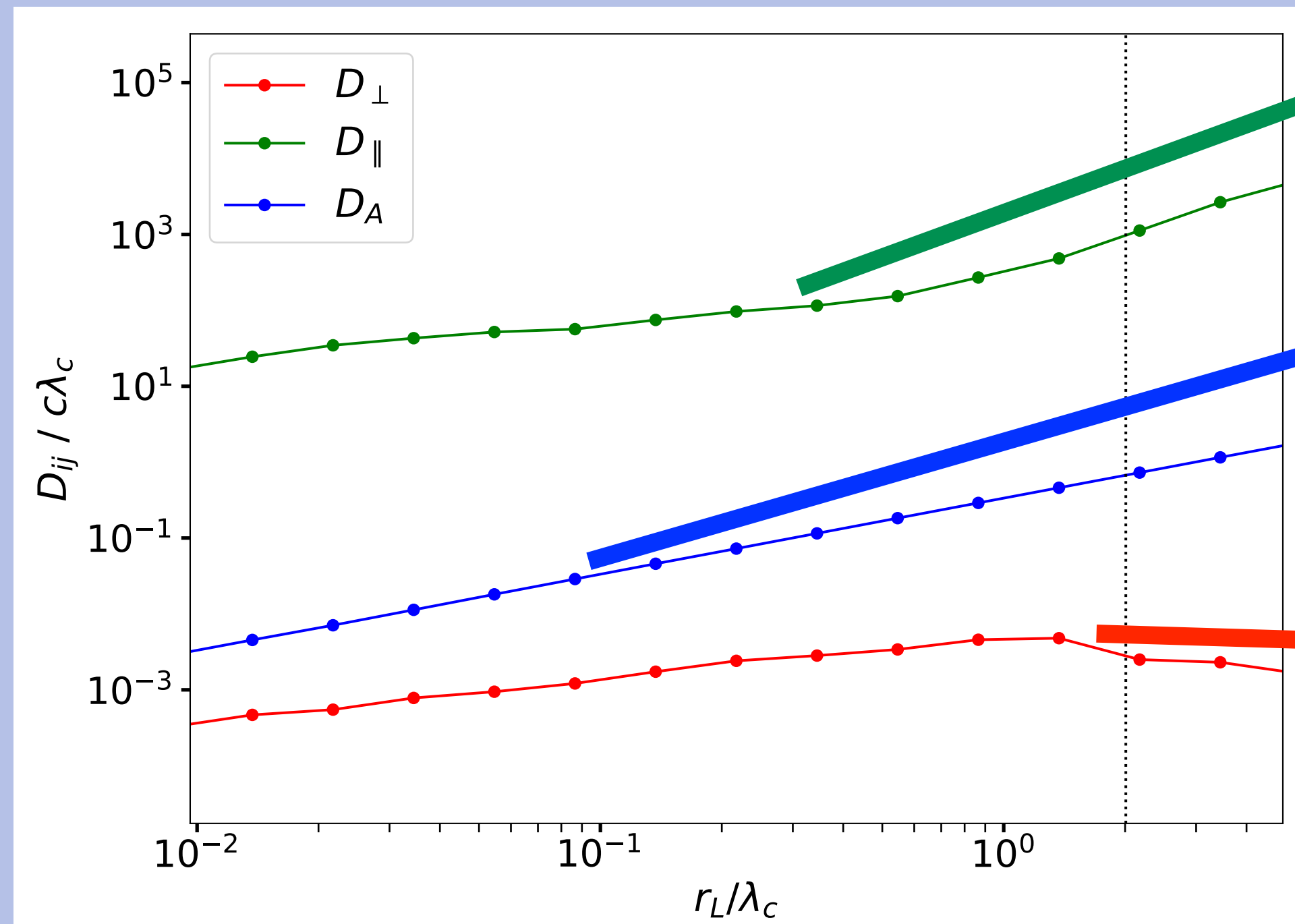
Cosmic ray galactic-extragalactic transition



Maximum energy achieved by Galactic accelerators?
Escape of cosmic rays from the Galaxy?

Numerical simulations

- **Synthetic magnetic fields:** turbulent spectrum assumed to be Kolmogorov and isotropic, with random components Gaussian-distributed.
- **Test-particle simulations** of TeV-PeV particles. Diffusion coefficients measured as function of rigidity and turbulence level.



QLT coefficient

$$D_{\parallel} \propto r_L^{1/3}$$

Bohm-like coefficient

$$D_A \propto r_L$$

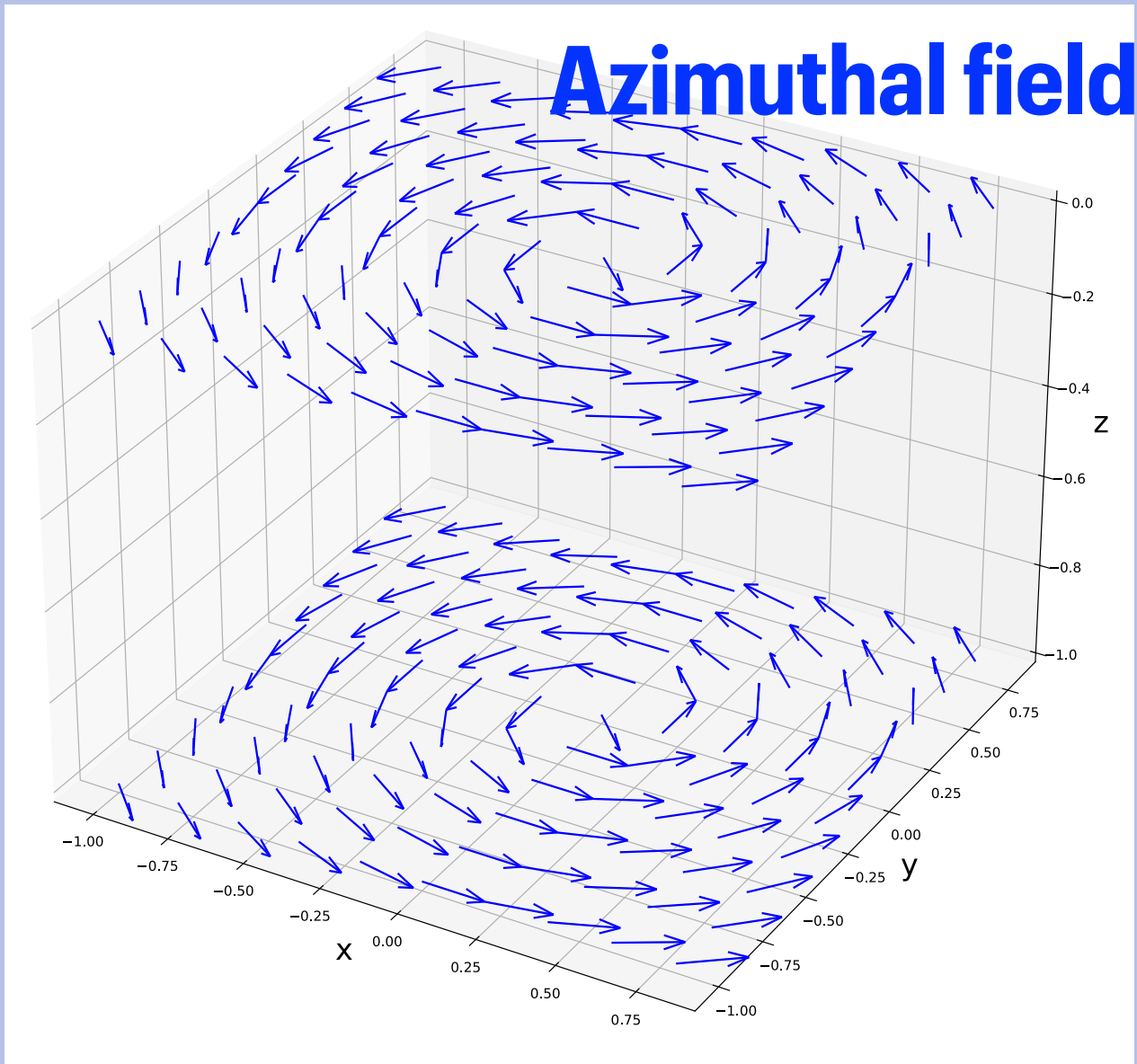
$$v_D \sim \frac{r_L c}{3L}$$

Corroboration of anomalous perpendicular behaviour

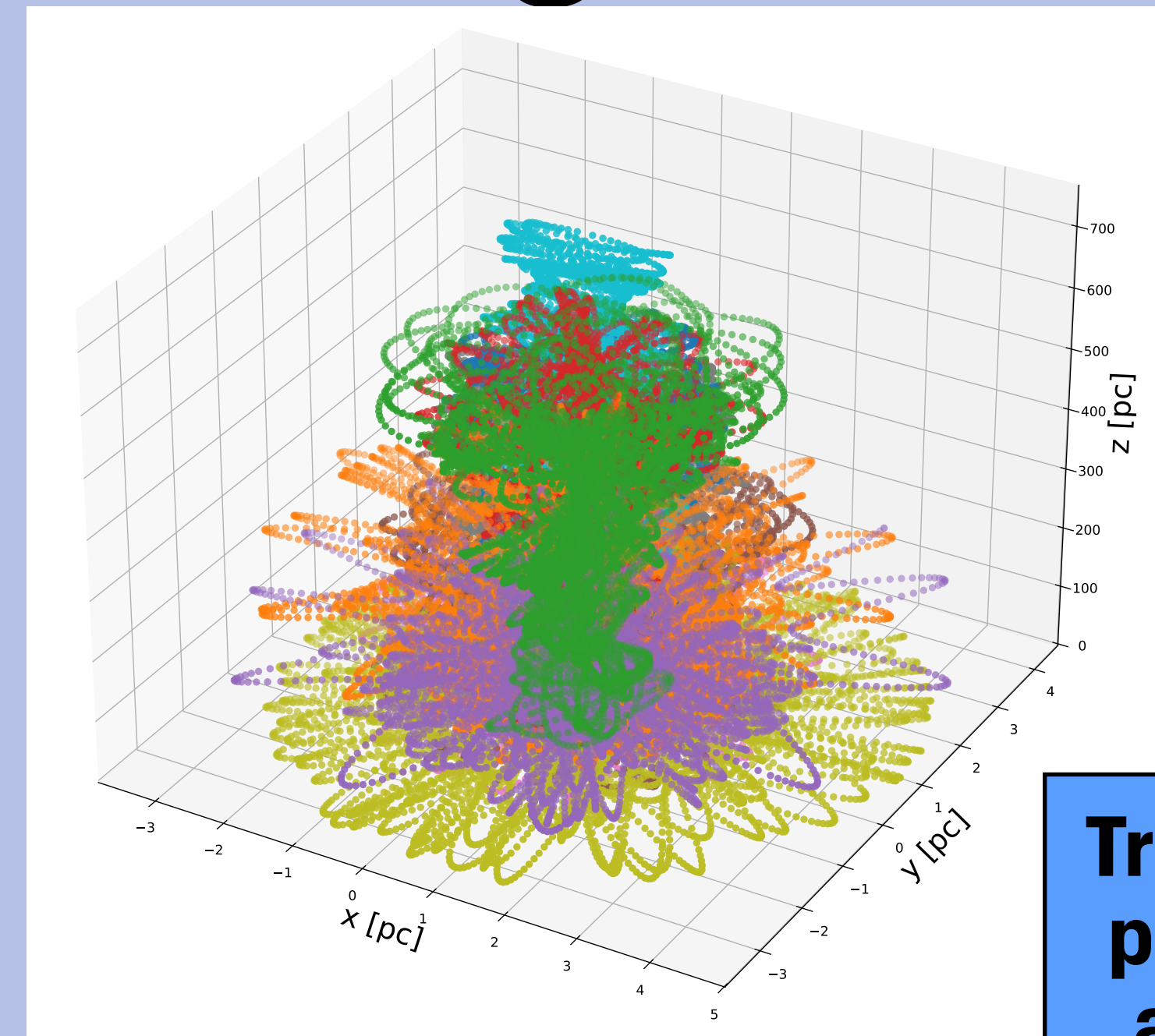
$$D_{\perp} \propto r_L^{1/2}$$

Cosmic ray escape time in Galactic magnetic fields

Galaxy-like
magnetic field
+ turbulence

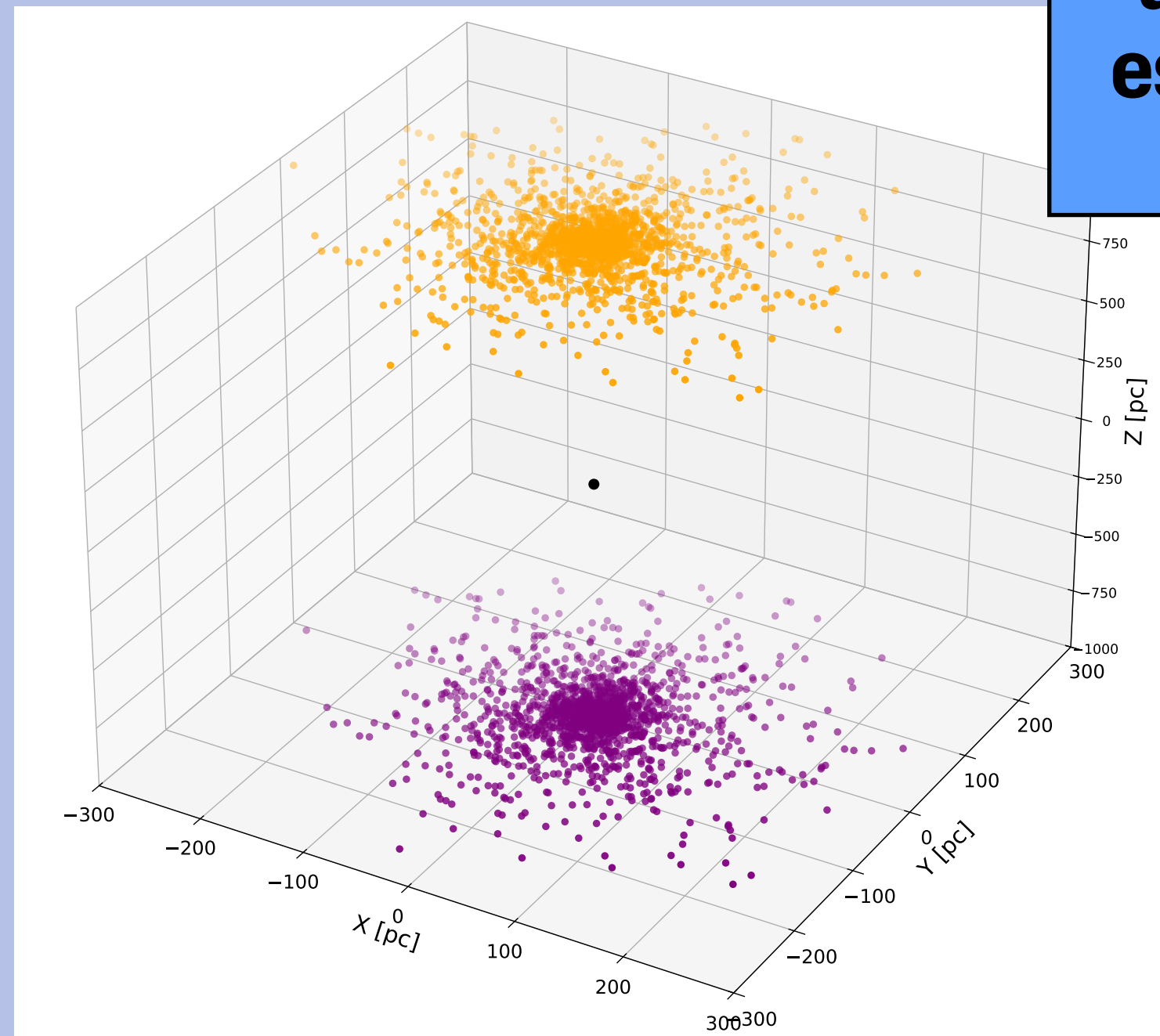
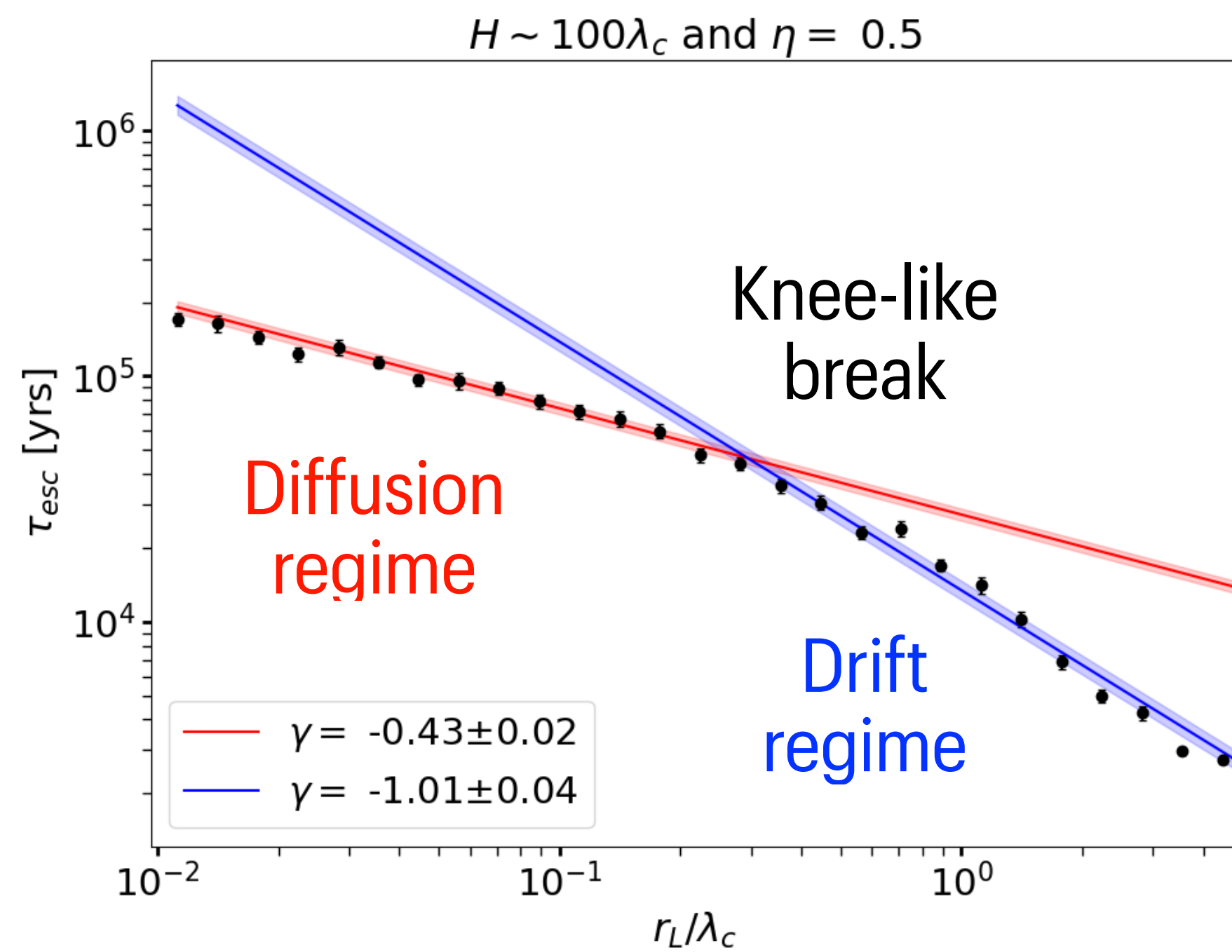


Particle injection



Track particle
propagation
and record
escape from
halo

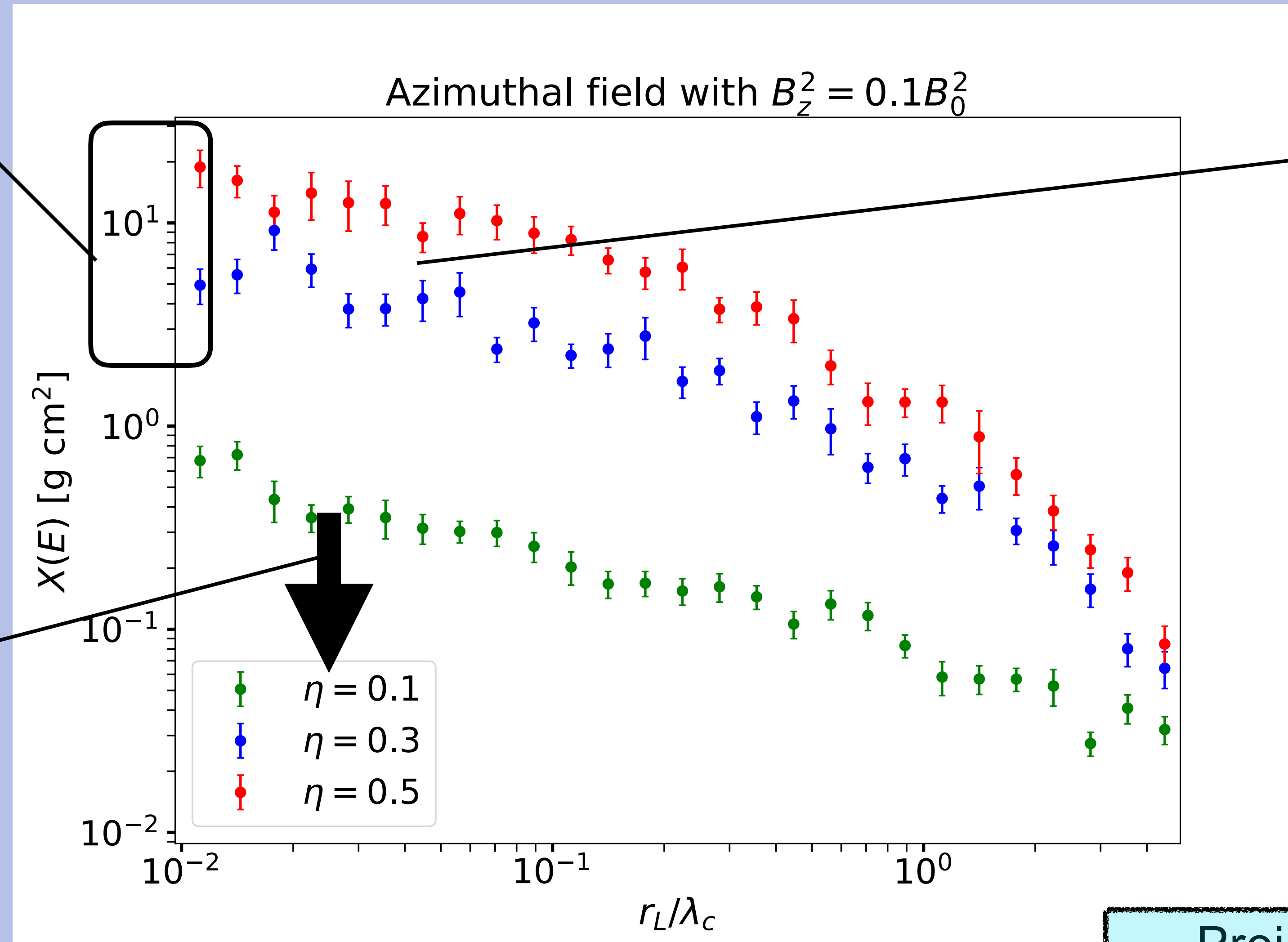
Compute escape
times and grammage



Cosmic ray grammage in Galactic magnetic fields

Grammage higher than estimates from B/C measurements

Lowering turbulence could further decrease grammage



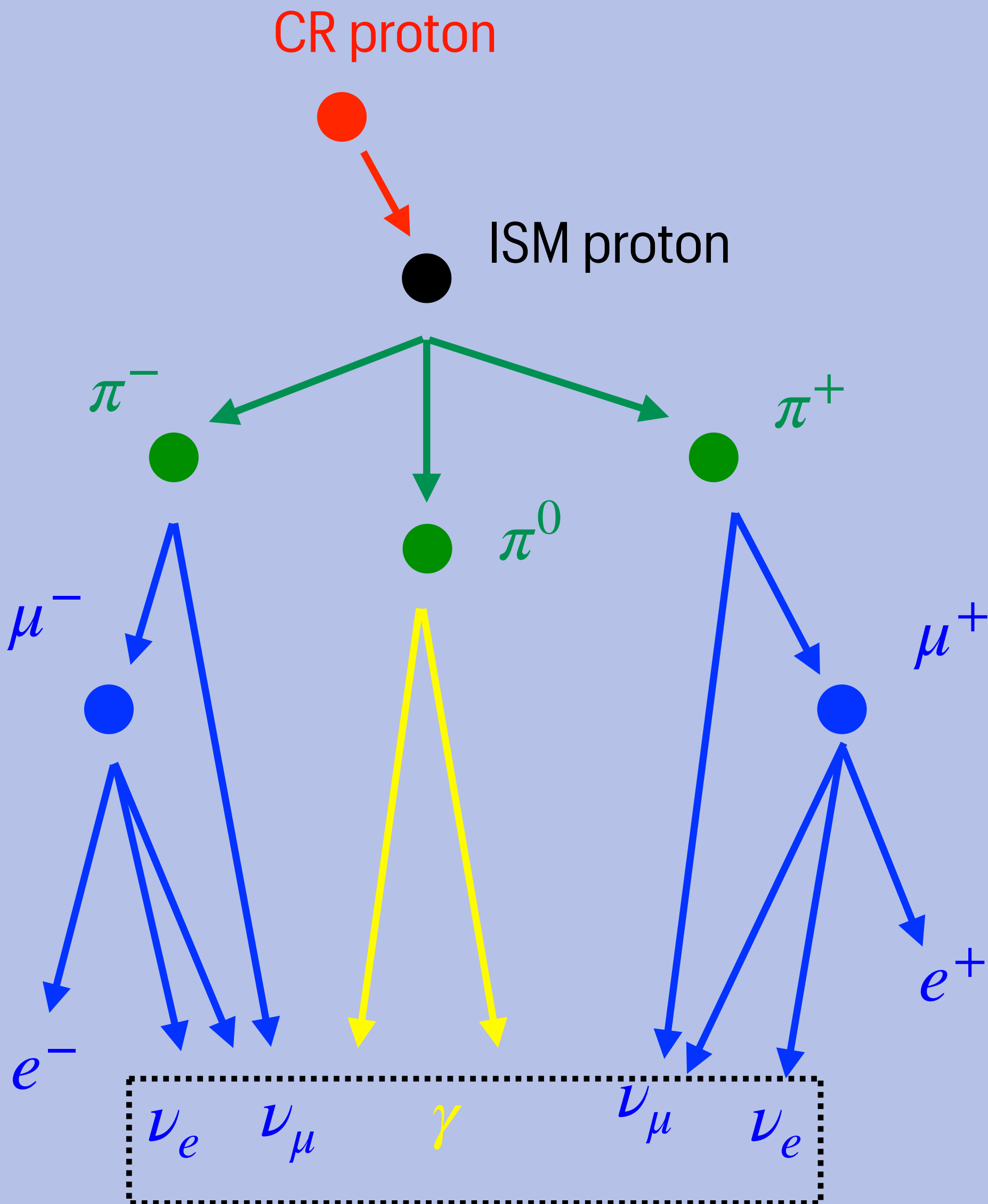
Parallel diffusion dominates and makes escape faster

Diffusion-drift interplay and enhancement

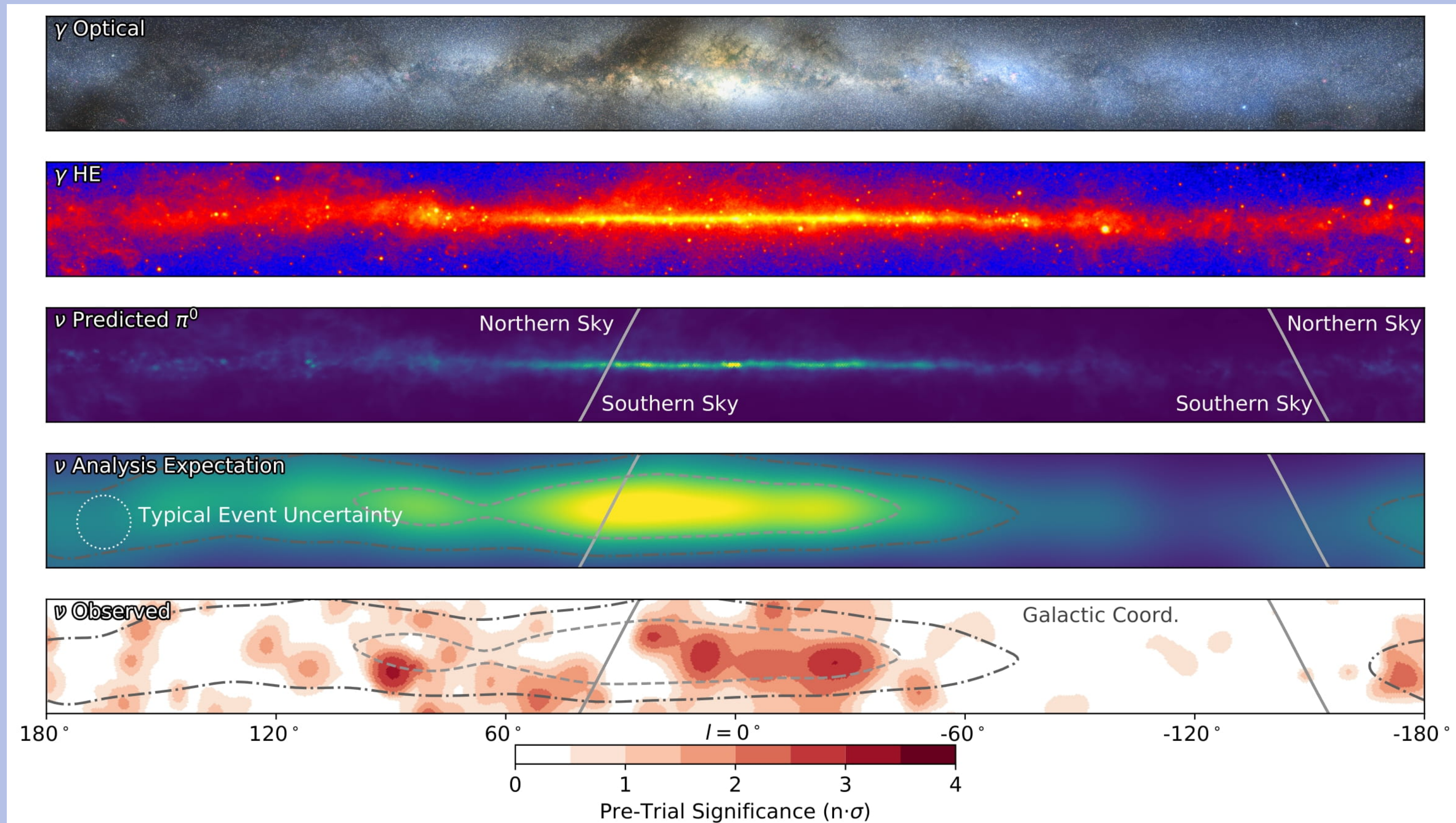
Project being finalised

Future: consider cosmic ray propagation in MHD turbulence

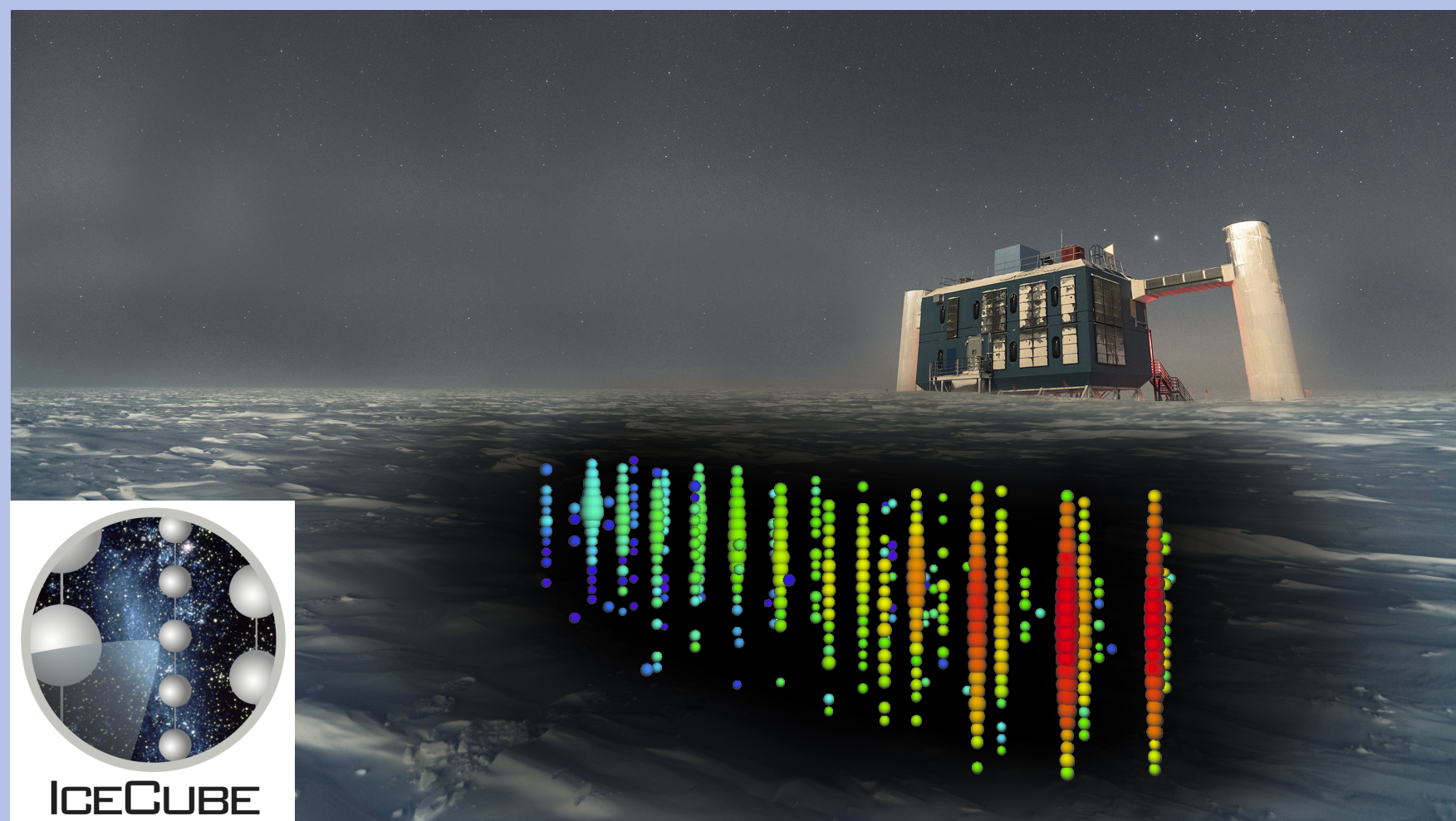
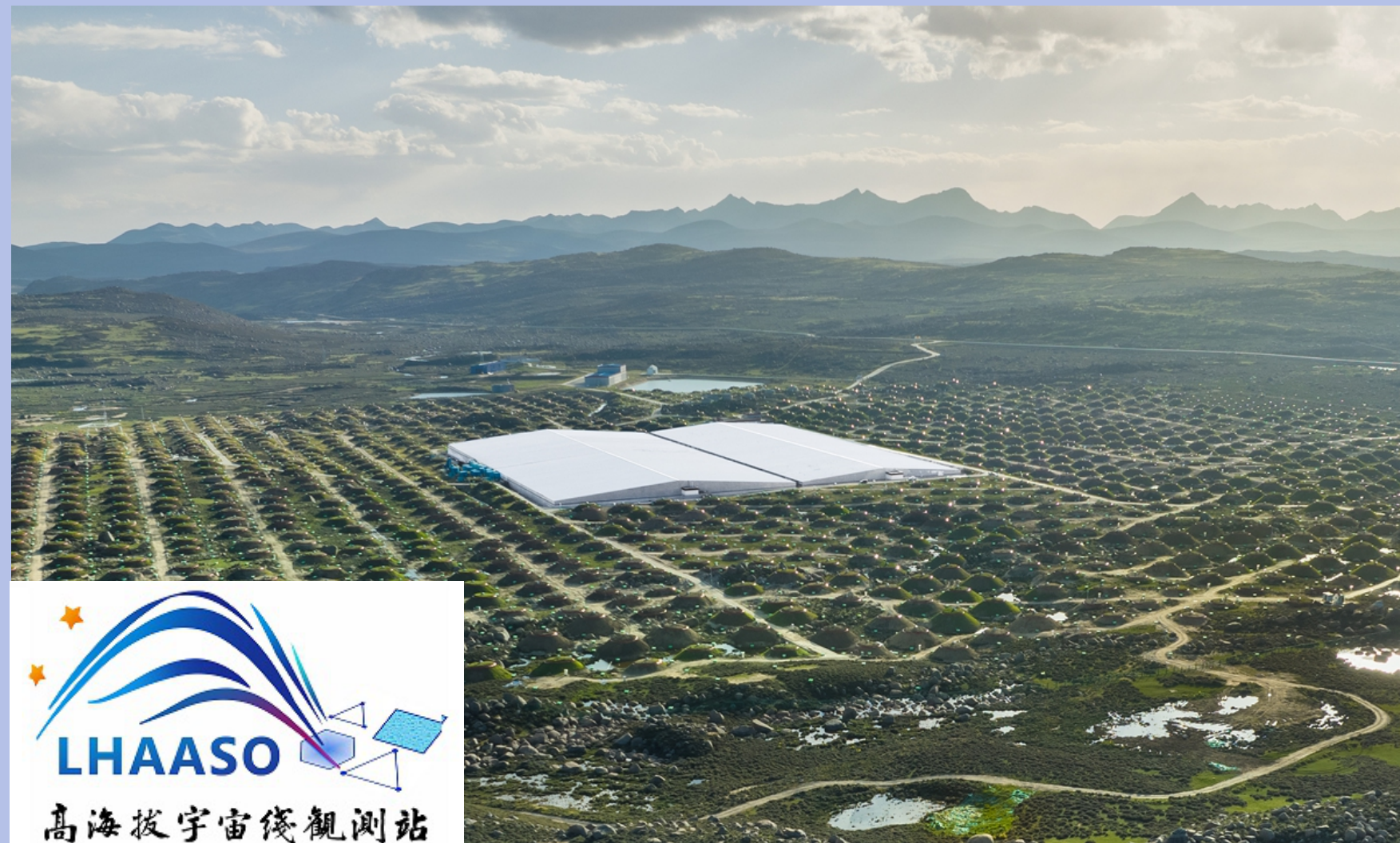
Secondary particles and diffuse fluxes



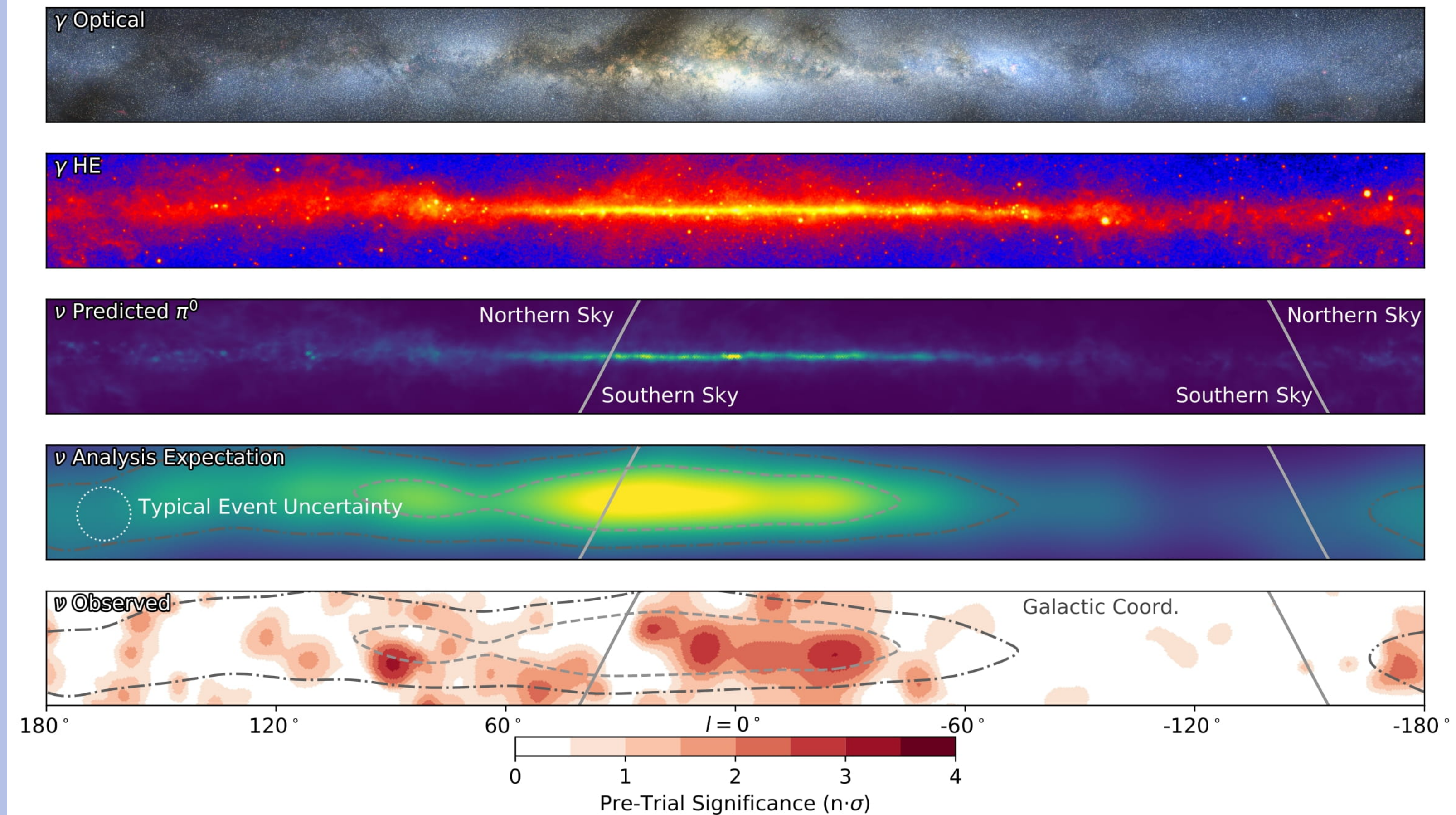
IceCube Coll., 2023



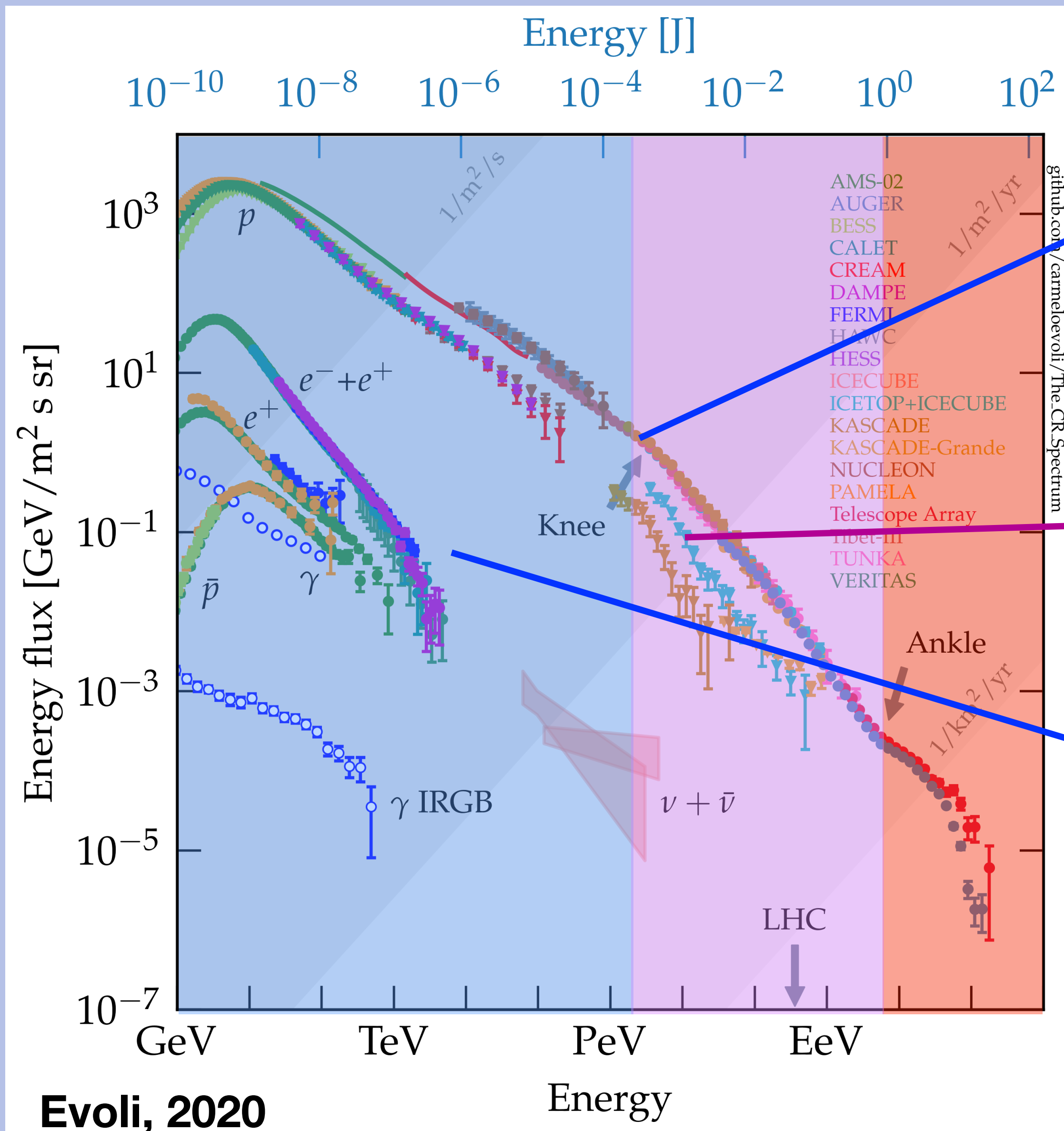
Secondary particles and diffuse fluxes



IceCube Coll., 2023



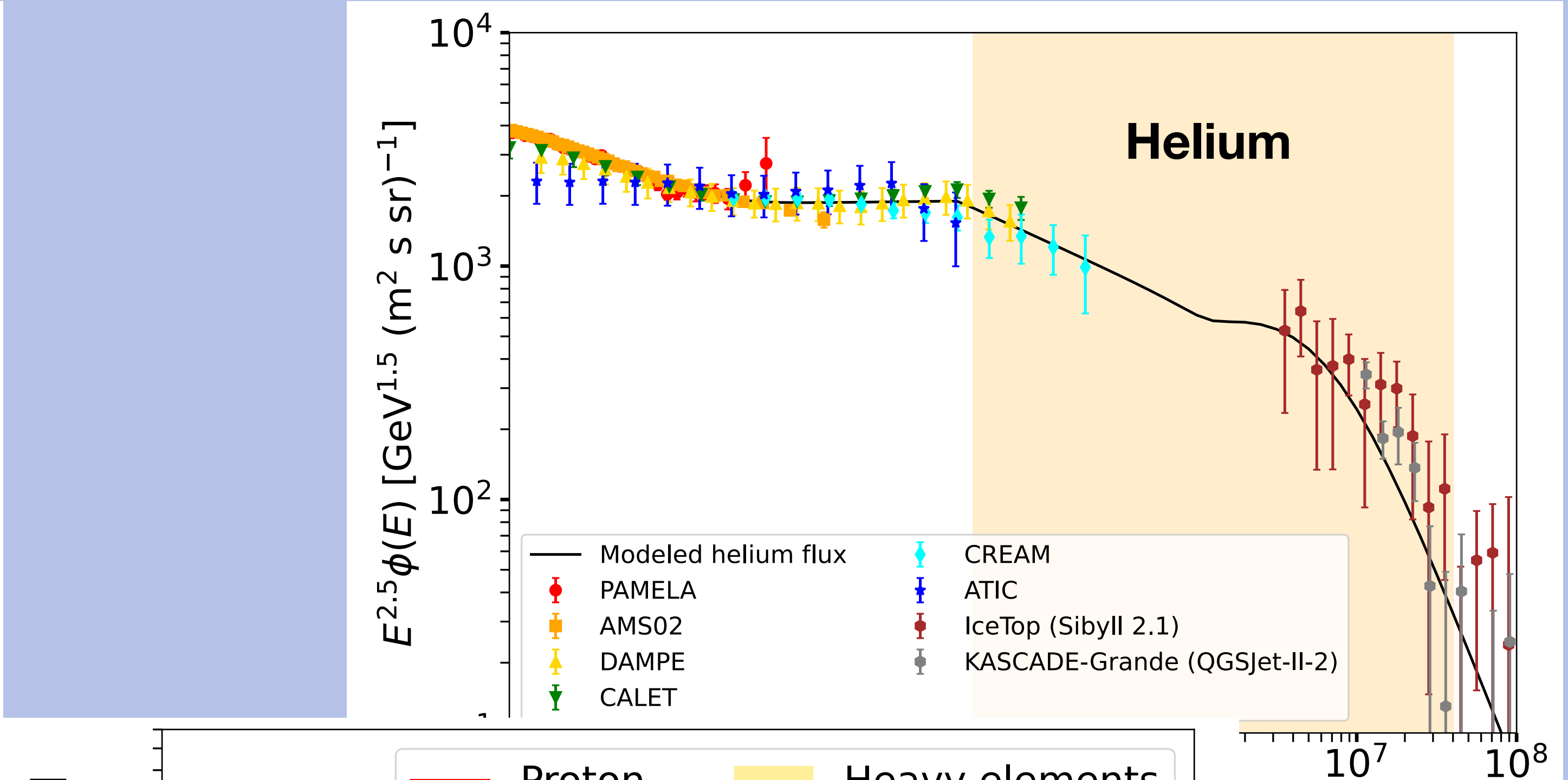
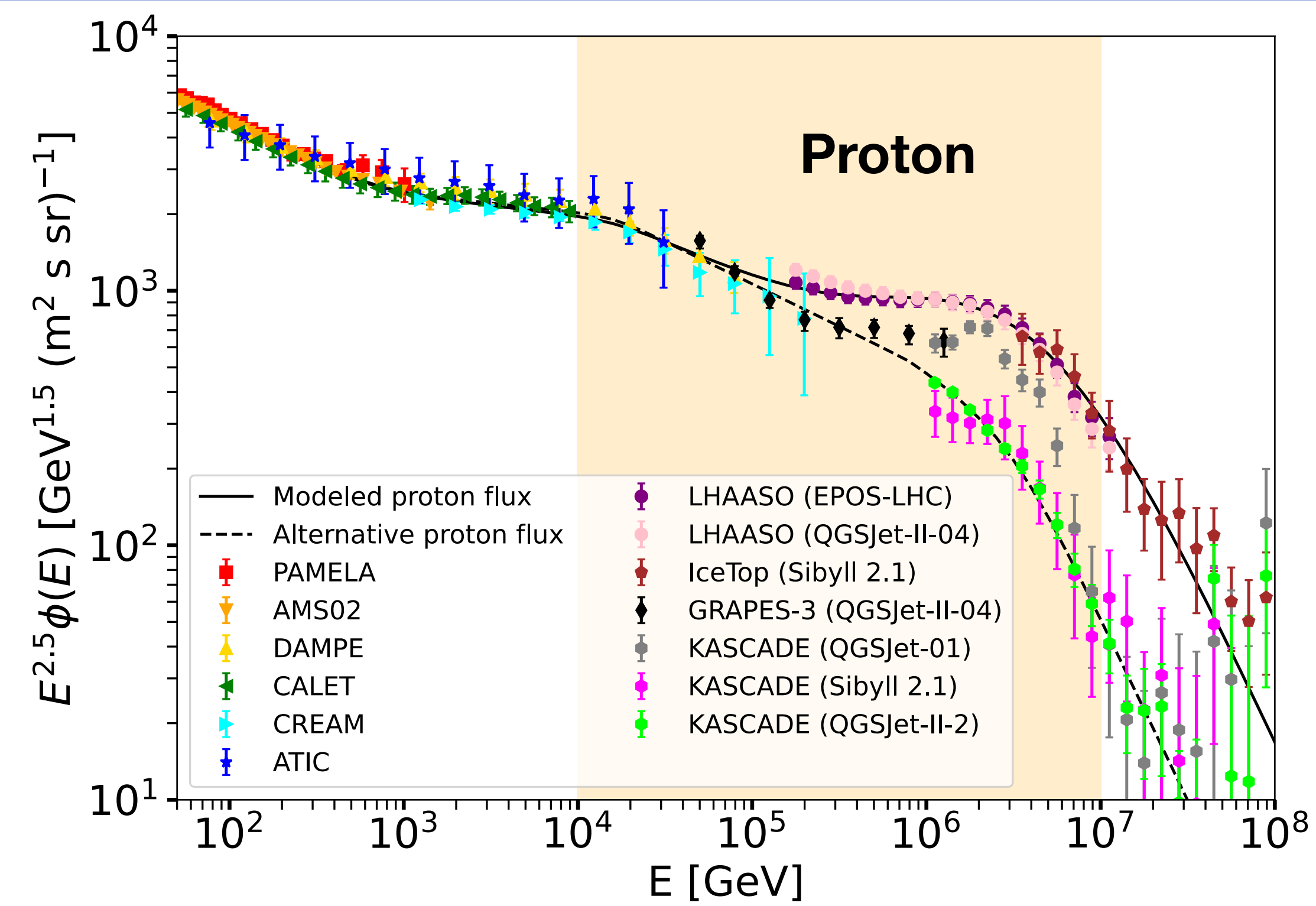
Cosmic ray galactic-extragalactic transition



Maximum energy achieved by Galactic accelerators?
Escape of cosmic rays from the Galaxy?

Additional population in transition regime?

Spatial dependence of cosmic ray density and spectrum?

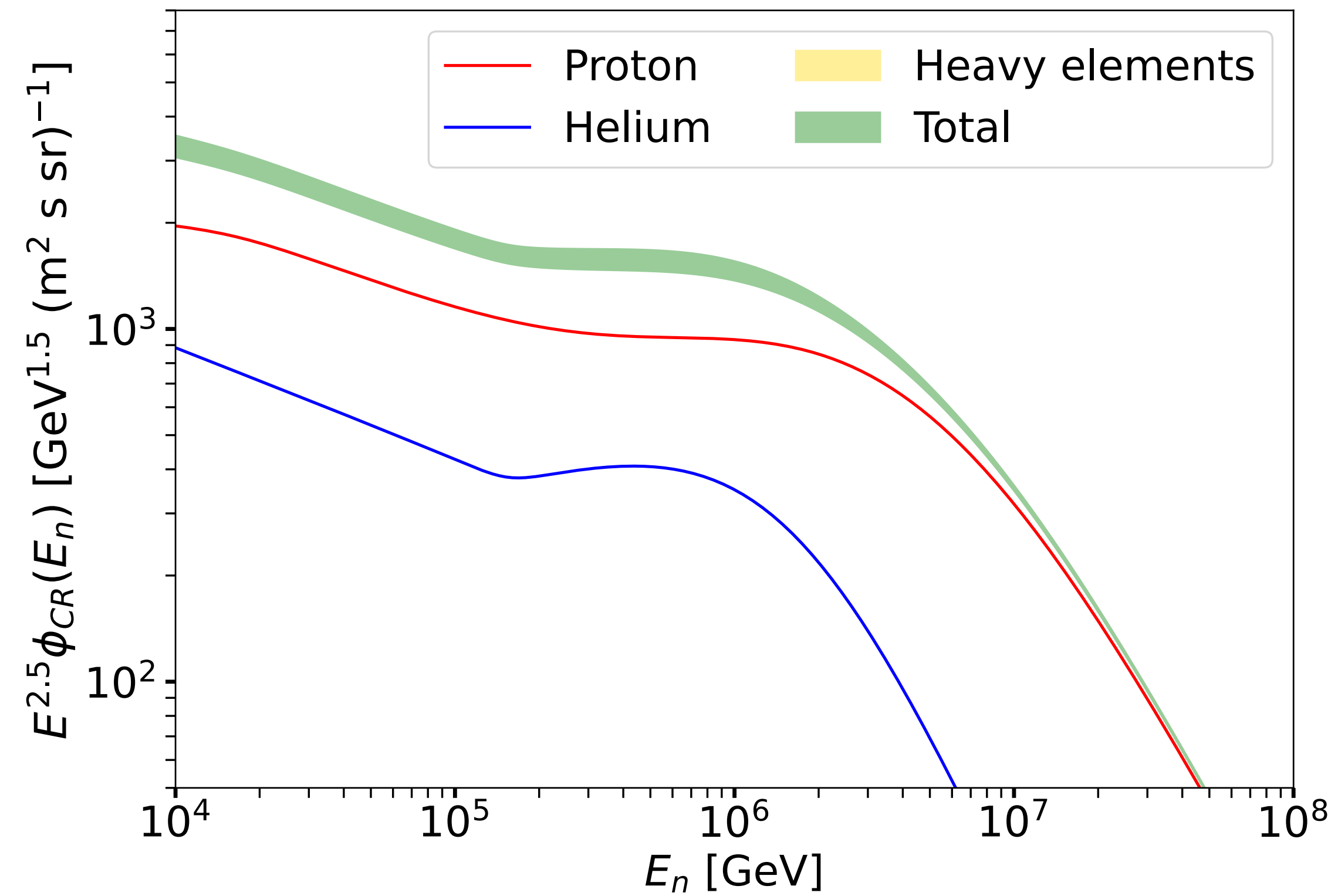


$$\phi(E) = K \left(\frac{E}{E_0} \right)^{-\alpha_1} \prod_{i=1}^{i=4} \left[1 + \left(\frac{E}{E_{b,i}} \right)^{1/\omega_i} \right]^{-(\alpha_{i+1} - \alpha_i) \omega_i}$$

$$\phi_{\text{CR}}(E_n) = \sum_A A^2 \phi_A(AE_n)$$

Nucleon flux (pointing to $\phi_{\text{CR}}(E_n)$)

Nuclei flux (pointing to $\phi_A(AE_n)$)



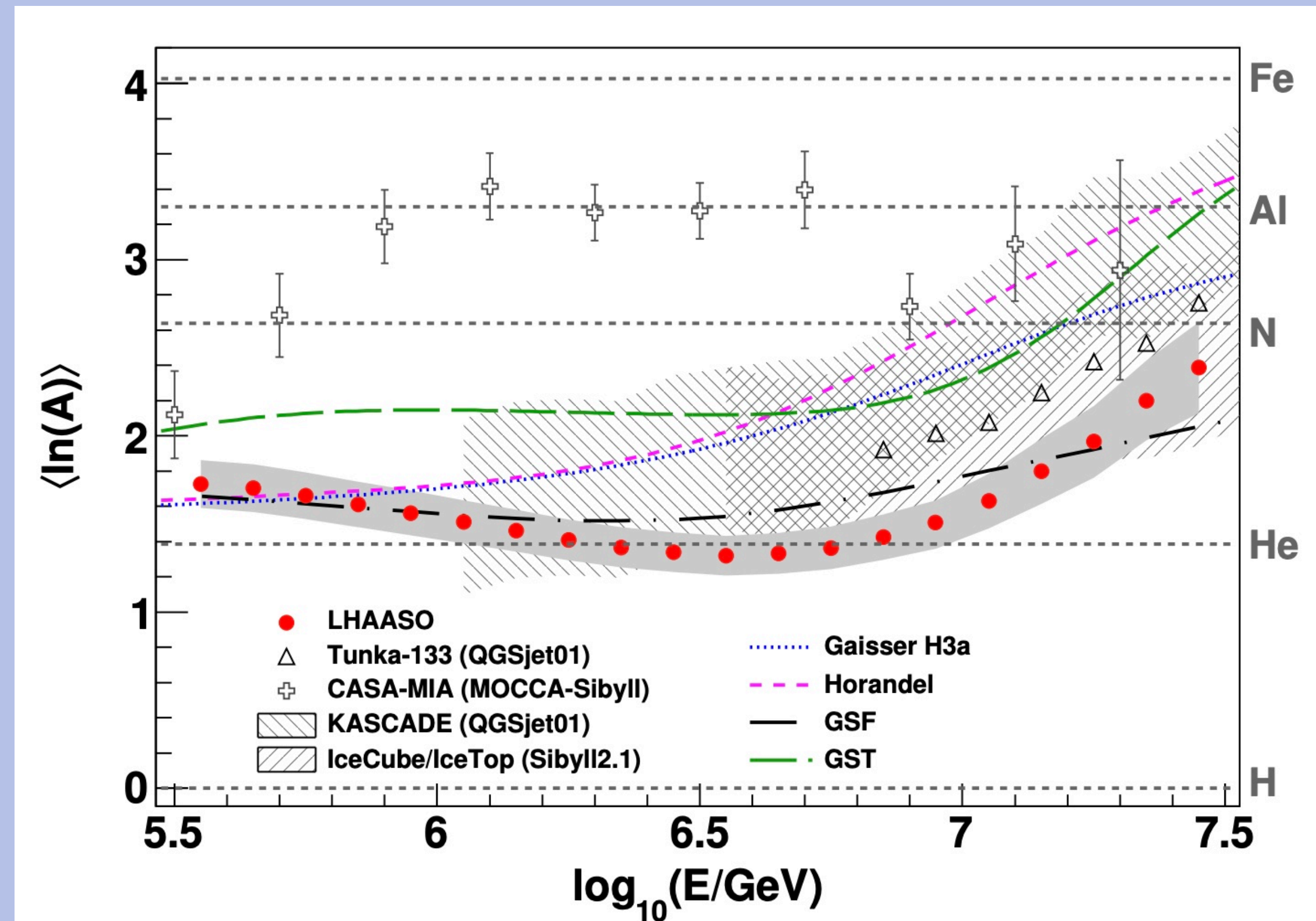
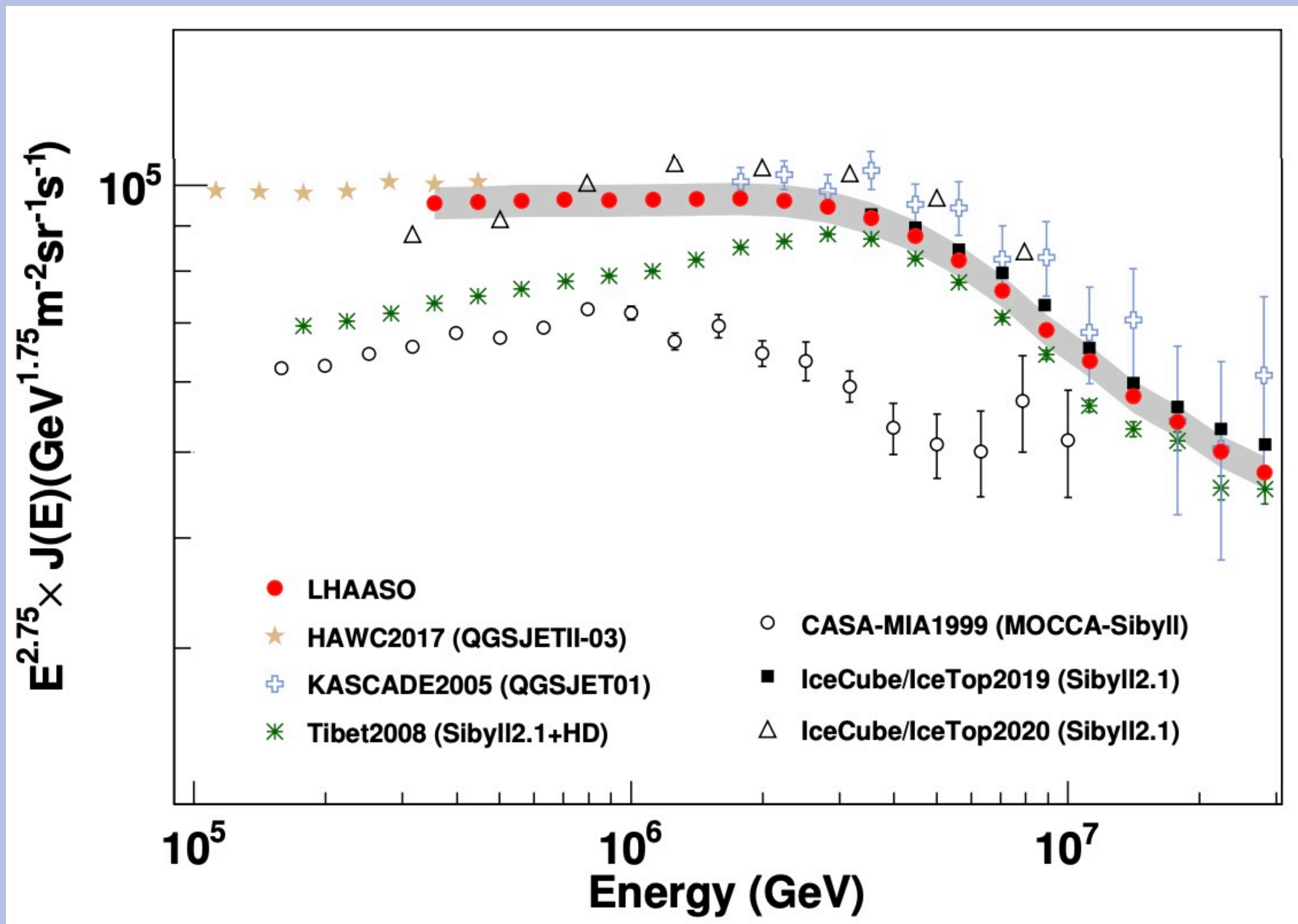
Additional project: Galactic cosmic ray flux and composition

See Igor's presentation

Project being finalised

Currently, also measurements of the all-particle flux and mean logarithmic mass by LHAASO available across the cosmic ray knee.

LHAASO Coll., 2024



Absorption

- CMB Vernetto & Lipari, 2016

Cross-section

- AAFrag Kachelriess et al., 2023

$$\phi_{\gamma}(E_{\gamma}; s, l, b) = \int_0^{\infty} ds \, n_{gas}(s, l, b) e^{-\tau(s, E_{\gamma})} \int_{E_{\gamma}}^{\infty} dE_n \frac{d\sigma}{dE_{\gamma}}(E_n, E_{\gamma}) \phi_{CR, \odot}(E_n)$$

Galactic gas

- Emission lines Porter et al., 2021, Dundovic et al., 2021
- Dust opacity Aghanim et al., 2016, Ade et al., 2011

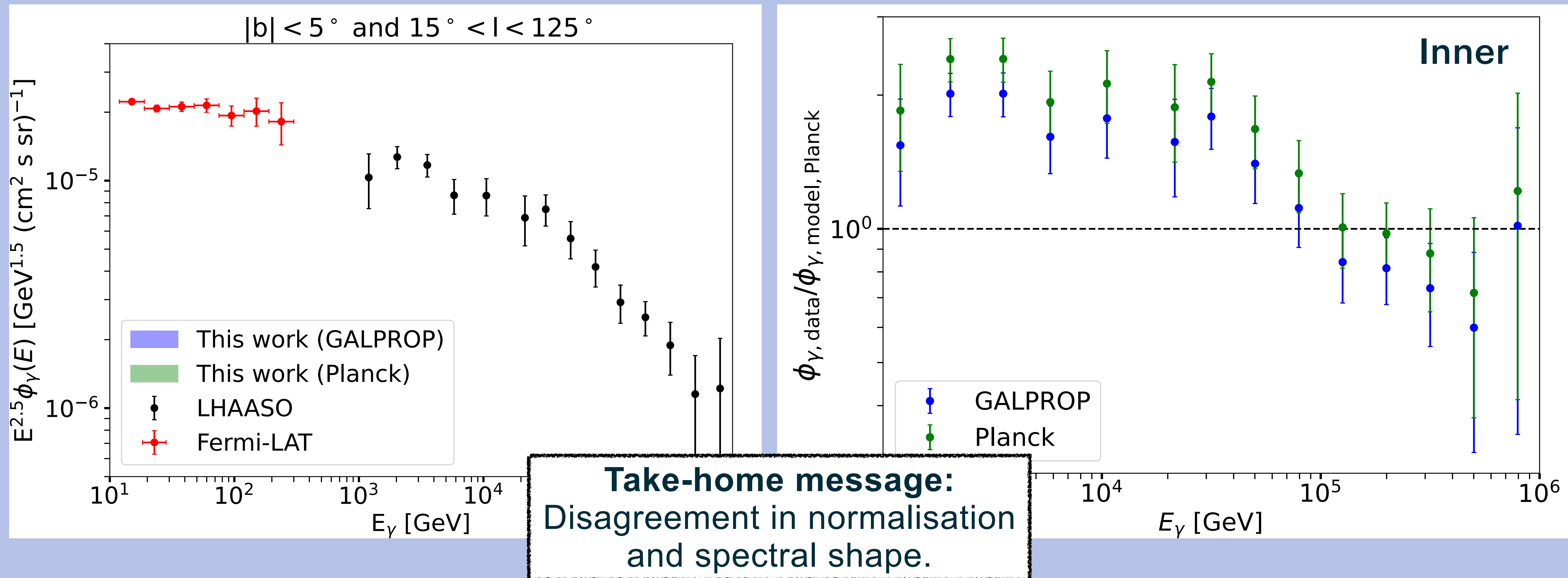
Cosmic ray nucleon flux

- Phenomenological model
- Uniform distribution
- Space-independent spectrum

Gamma-ray Diffuse Emission: Comparison with LHAASO

- Excess in LHAASO observations found only in the inner region at low energies.
- No distinction from space-dependent to space-independent spectrum in LHAASO regions

Espinosa Castro et al., MNRAS Lett, 2025

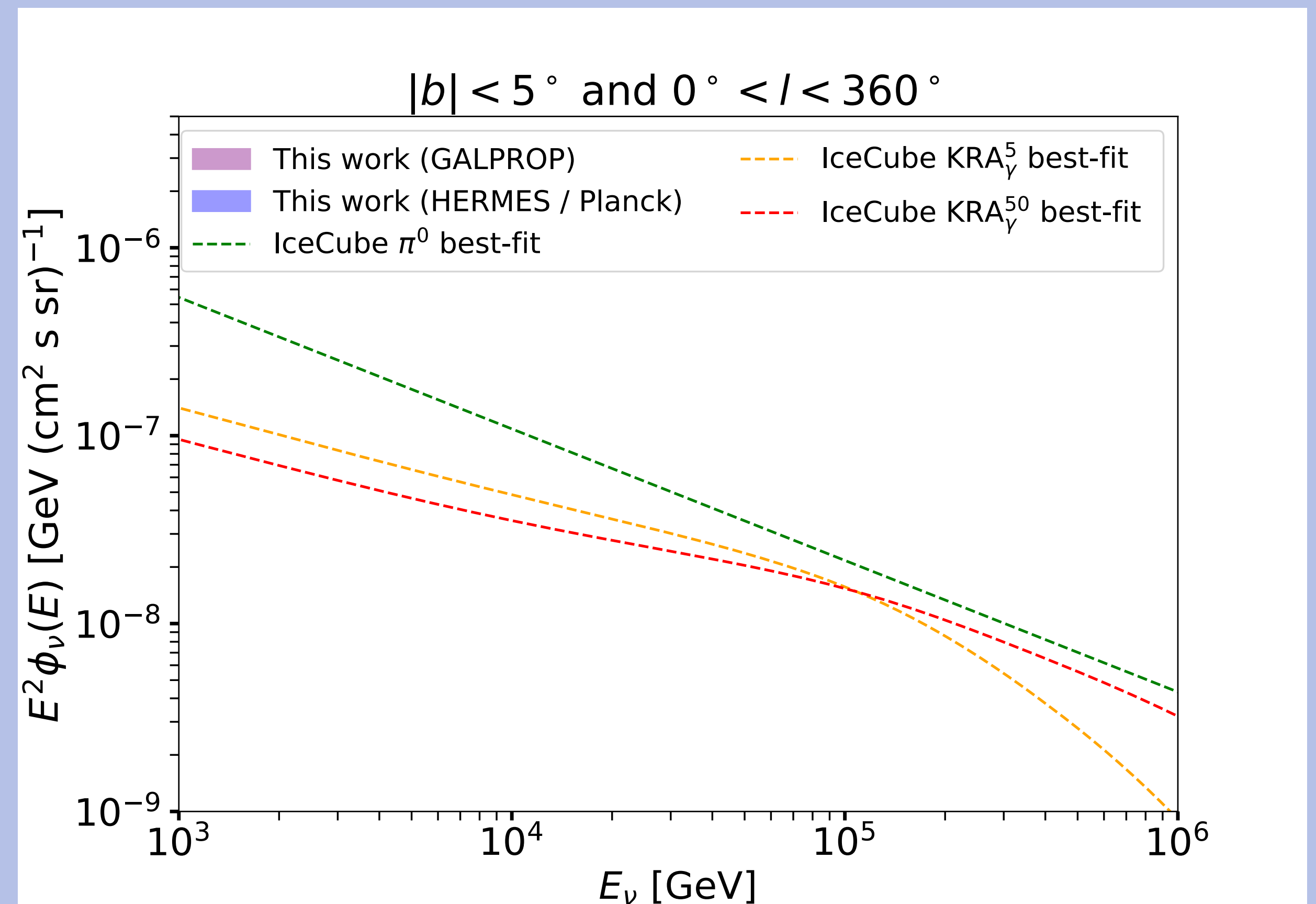
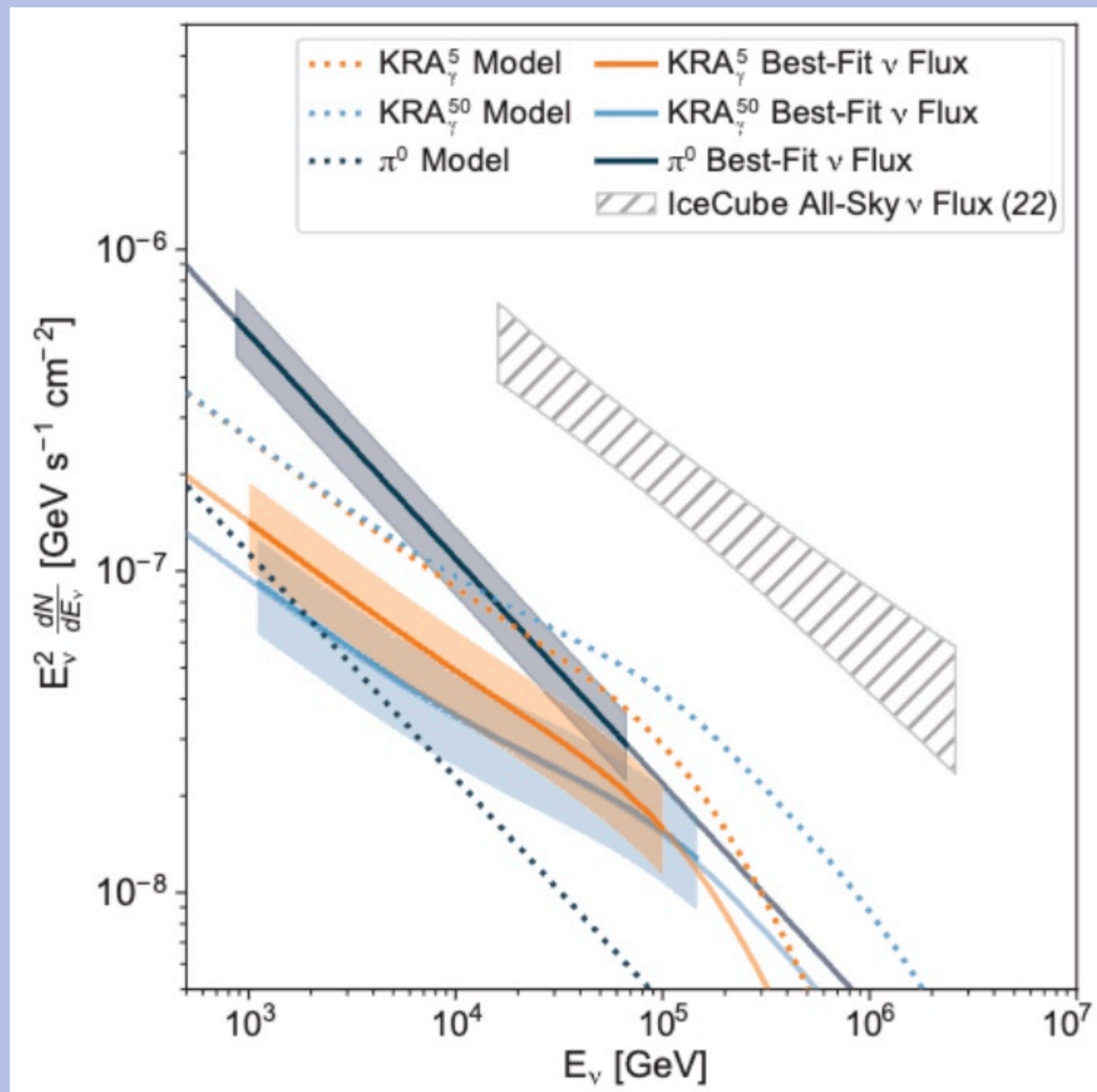


Neutrino Diffuse Emission: Comparison with IceCube

- Overall normalisation can be reproduced but different spectral shape.
- Strong constraints on contribution from Galactic sources.

Paper in prep.

IceCube Coll., 2023



SUMMARY

- Perpendicular diffusion has an **anomalous rigidity dependence** in synthetic field simulations.
- Propagation explanation of cosmic ray knee may be inadequate and predict **higher confinement times** in Galactic magnetic fields.
- Galactic cosmic rays at the knee seem to be **incompatible** with observations of VHE gamma-rays.
- All-particle flux and composition analysis suggests **second population** required at the knee to explain data.
- \implies Is the cosmic ray knee explained by the maximum acceleration energy of a second population of Galactic sources peaking at PeV energies?

PUBLICATIONS

- L. E. Espinosa Castro, F. L. Villante, V. Vecchiotti, C. Evoli and G. Pagliaroli, MNRAS Lett., Vol. 543, 1, 2025, p. L20–L26
- L. E. Espinosa Castro, F. L. Villante, V. Vecchiotti, C. Evoli, and G. Pagliaroli, PoS ICRC2025, 640 (2025)
- L. E. Espinosa Castro, C. Evoli, and P. Blasi, PoS ICRC2025, 037 (2025)
- I. Vaiman, C. Evoli, and L. E. Espinosa Castro, PoS ICRC2025, 148 (2025)

CONFERENCES AND SEMINARS

- Contributed talk in 39th International Cosmic Ray Conference - July 2025; Geneva, Switzerland
- Poster in 39th International Cosmic Ray Conference - July 2025; Geneva, Switzerland
- Contributed talk in Toulouse, Arcetri, and L'Aquila Retreat - October 2025; Arcetri, Italy

OUTREACH ACTIVITIES

- SHARPER (European Research Night September) / Street Science - September 2024; L'Aquila, Italy
- SHARPER (European Research Night September) / Street Science - September 2025; L'Aquila, Italy

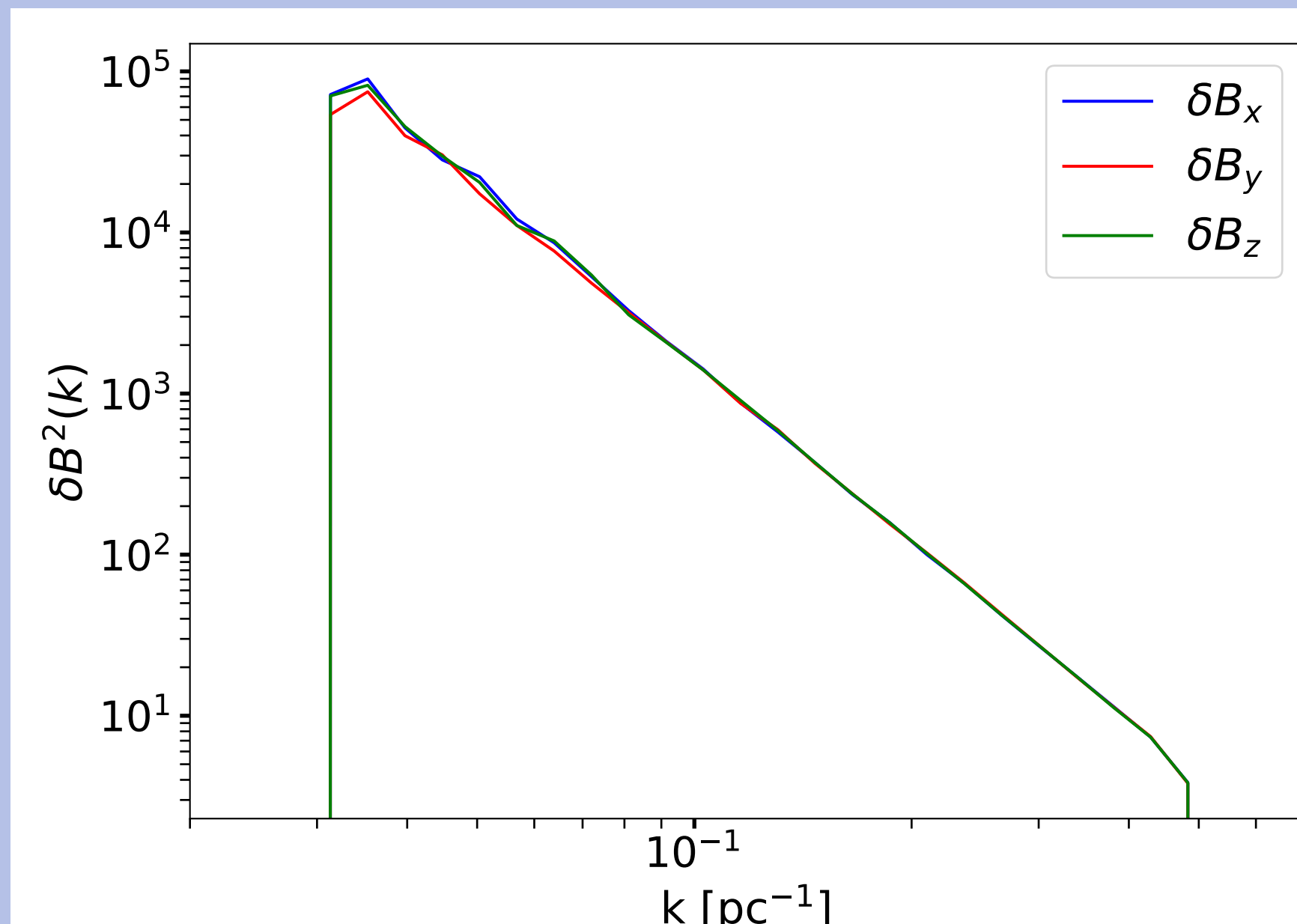
BACKUP SLIDES

Numerical simulations

- **Synthetic magnetic fields:** turbulent spectrum assumed to be Kolmogorov and isotropic, with random components Gaussian-distributed.

$$\text{IFFT in grid } \delta B(\vec{x}) = \int d^3k \delta \tilde{B}(\vec{k}) e^{-i\vec{x} \cdot \vec{k}}$$

$$W(k) \propto \frac{\delta B^2 l_b}{\pi k^2} \frac{(kl_b)^q}{[1 + (kl_b)^2]^{(s+q)/2}}$$



Inputs:

- δB_{rms} given by turbulence level $\eta = \frac{\delta B_{rms}}{B_0}$
- Spacing of grid $\Delta x \sim 10^{-2}$ pc
- Number of grid points $N_{grid} = 2048$
- Kolmogorov turbulent spectrum $s = 5/3, q = 4$
- Bend-over scale $l_b \sim \text{few pc}$

Additional quantities:

- Size of grid $L = \Delta \cdot N_{grid}$
- Minimum turbulent scale $L_{min} = 2 \cdot \Delta$
- Maximum turbulent scale $L_{max} = L/2$
- Correlation length $\lambda_c = \frac{4\pi}{\delta B^2} \int_0^\infty dr \int_0^\infty dk \frac{\sin(kr)}{kr} k^2 W(k)$

Simulation parameters

- Uniform field with $B_0 = 1\mu G$
 - Turbulence levels $\eta = \frac{\delta B_{rms}}{B_0} = 0.1, 0.3, 0.5$
 - $\Delta = 0.15 \text{ pc} \sim 10 \cdot r_L (E = 10^{15} \text{ eV})$
 - $N_{grid} = 2048$
 - Kolmogorov spectrum, i.e. $\gamma = 5/3$
 - $L = 102.4 \text{ pc}$, $L_{min} = 0.2 \text{ pc}$, $L_{max} = 12.8 \text{ pc}$ and $\lambda_c = 2.73 \text{ pc}$
- ⇒ Scattering resonance around PeV energy

- Number of particles $N_p = 10^3$
- Number of position/velocity measurements $N_t = 10^5$
 - Step for position/velocity measurements $\Delta t = 0.1 r_L/c$
 - Maximum distance travelled by particles $D = 10^4 r_L$
- Minimum and maximum integrations steps $l_{min} = 0.1 \text{ pc}$ and $l_{max} = 100 \text{ Mpc}$

Numerical simulations

Ansatz (Bieber & Matthaeus, 1997):

**Mean displacements
method**

$$D_{ij} = \frac{\langle \Delta x_i \Delta x_j \rangle}{2\tau}$$

TGK method

$$D_{ij} = \int_0^\infty dt \langle v_i(0) v_j(t) \rangle = \int_0^\infty dt R_{ij}(t)$$

$$R_{\parallel}(t) = \frac{c^2}{3} e^{-t/\tau_{\parallel}}$$

$$R_{\perp}(t) = \frac{c^2}{3} \cos \omega t e^{-t/\tau_{\perp}}$$

$$R_A(t) = -\frac{c^2}{3} \sin \omega t e^{-t/\tau_A}$$

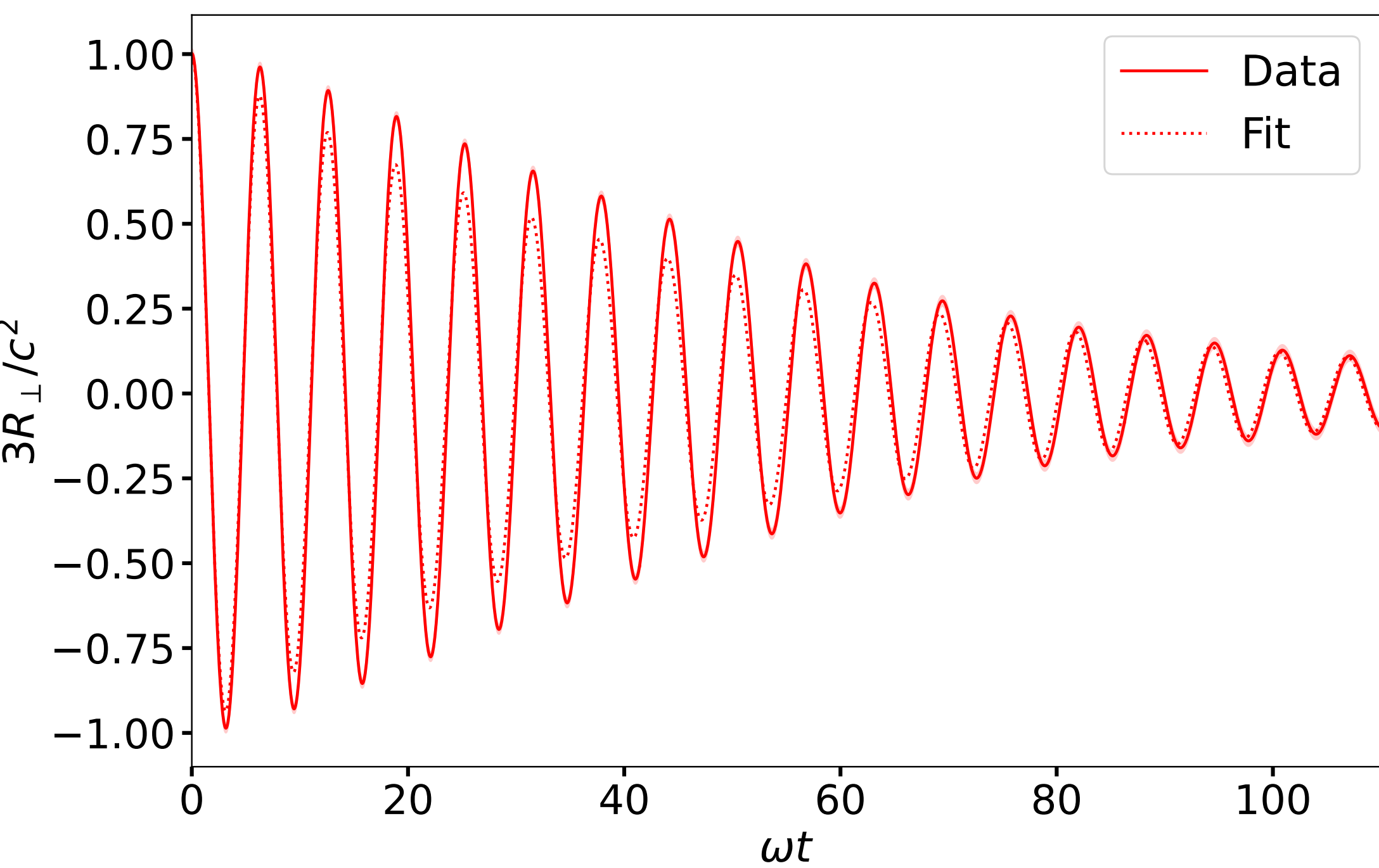
$$\text{If } \omega^{-1} \ll \tau_{\perp}, \quad D_{\perp} \propto \frac{R^{\alpha_{\perp}}}{(R^{-1} R^{\alpha_{\perp}})^2} = R^{2-\alpha_{\perp}}$$

$$\text{If } \omega^{-1} \gg \tau_{\perp}, \quad D_{\perp} \propto R^{\alpha_{\perp}}$$

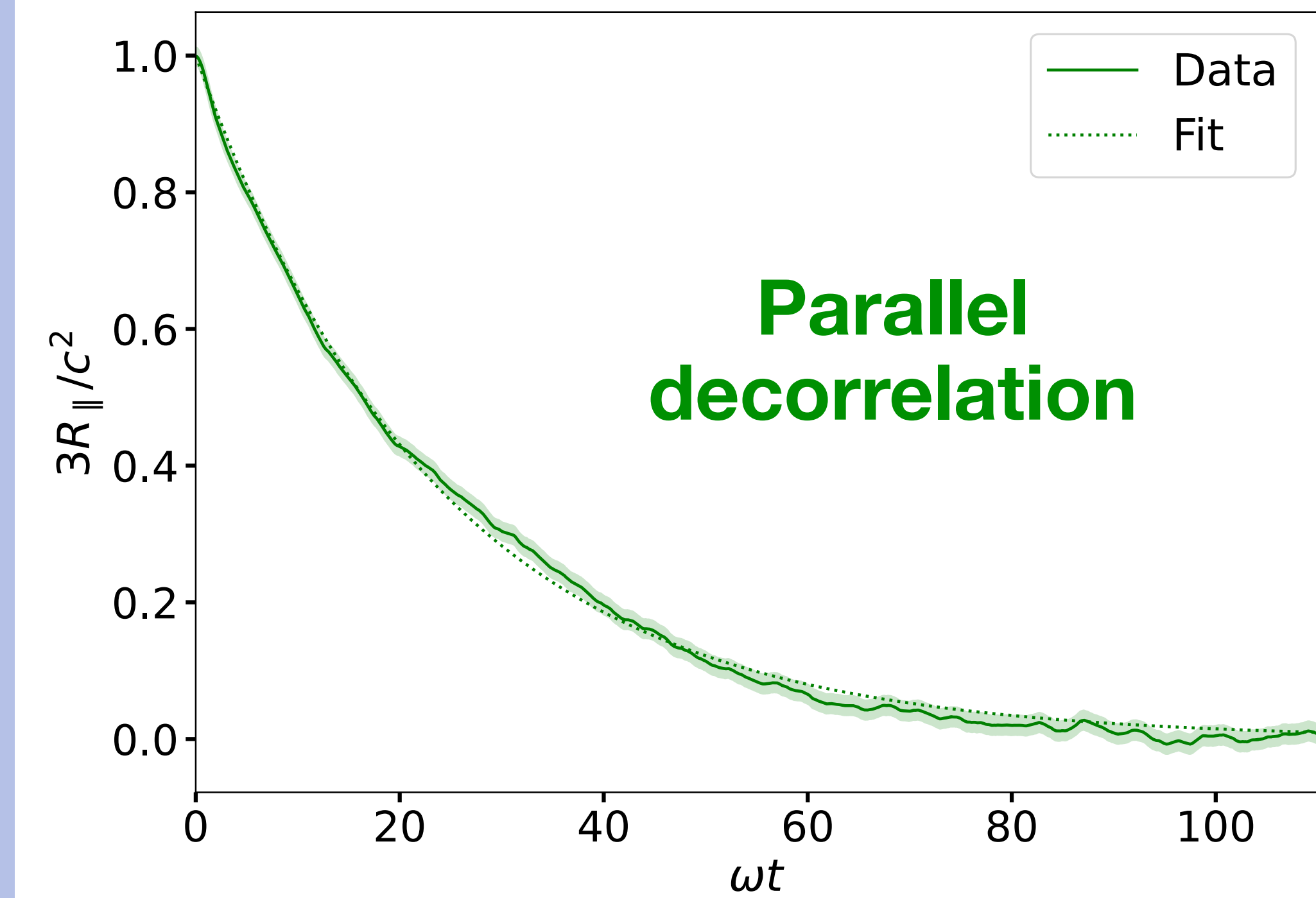
$$\text{If } \omega^{-1} \ll \tau_A, \quad D_A \propto \frac{R^{-1} R^{2\alpha_A}}{(R^{-1} R^{\alpha_A})^2} = R$$

$$\text{If } \omega^{-1} \gg \tau_A, \quad D_A \propto R^{2\alpha_A-1}$$

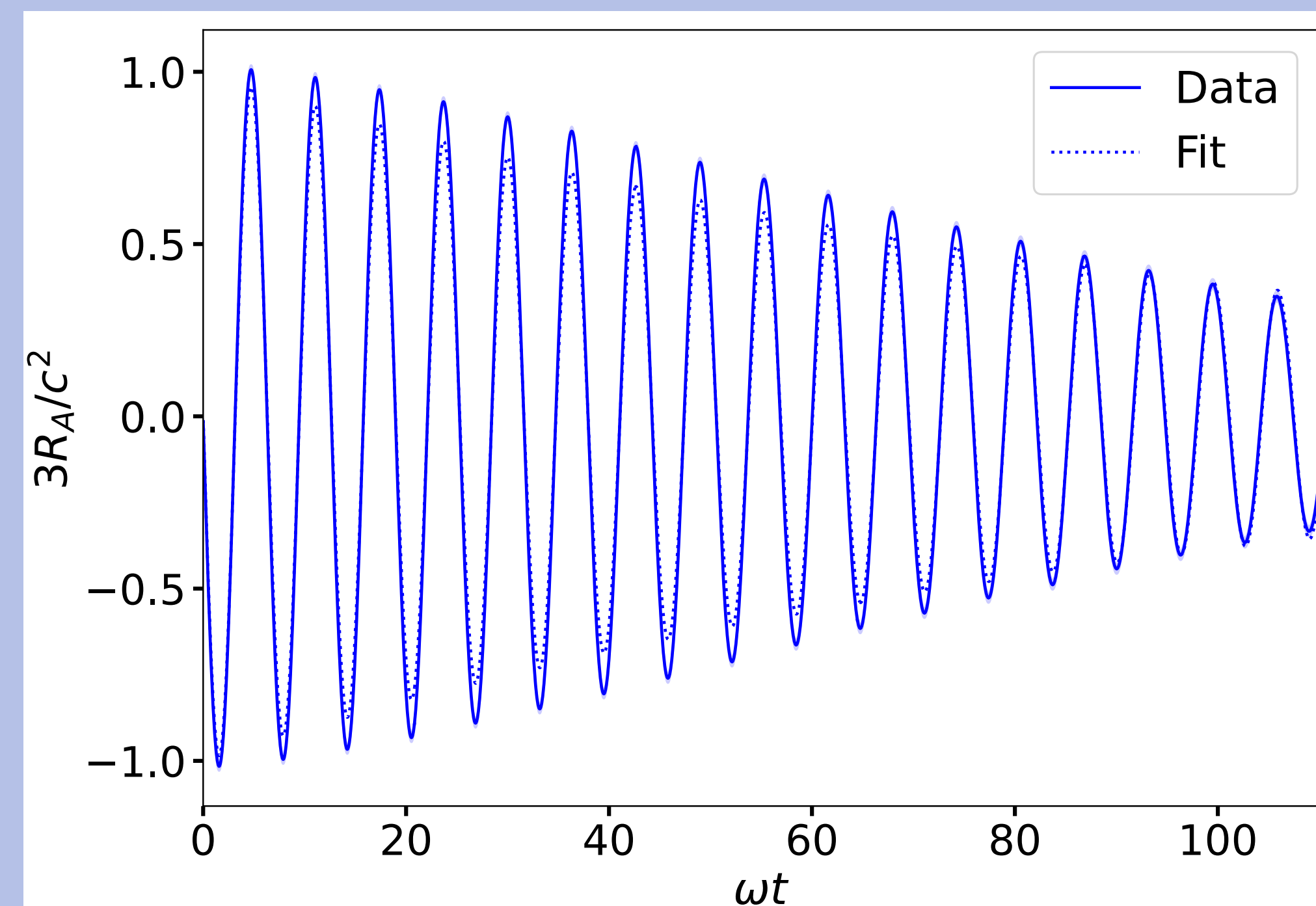
**Perpendicular
decorrelation**



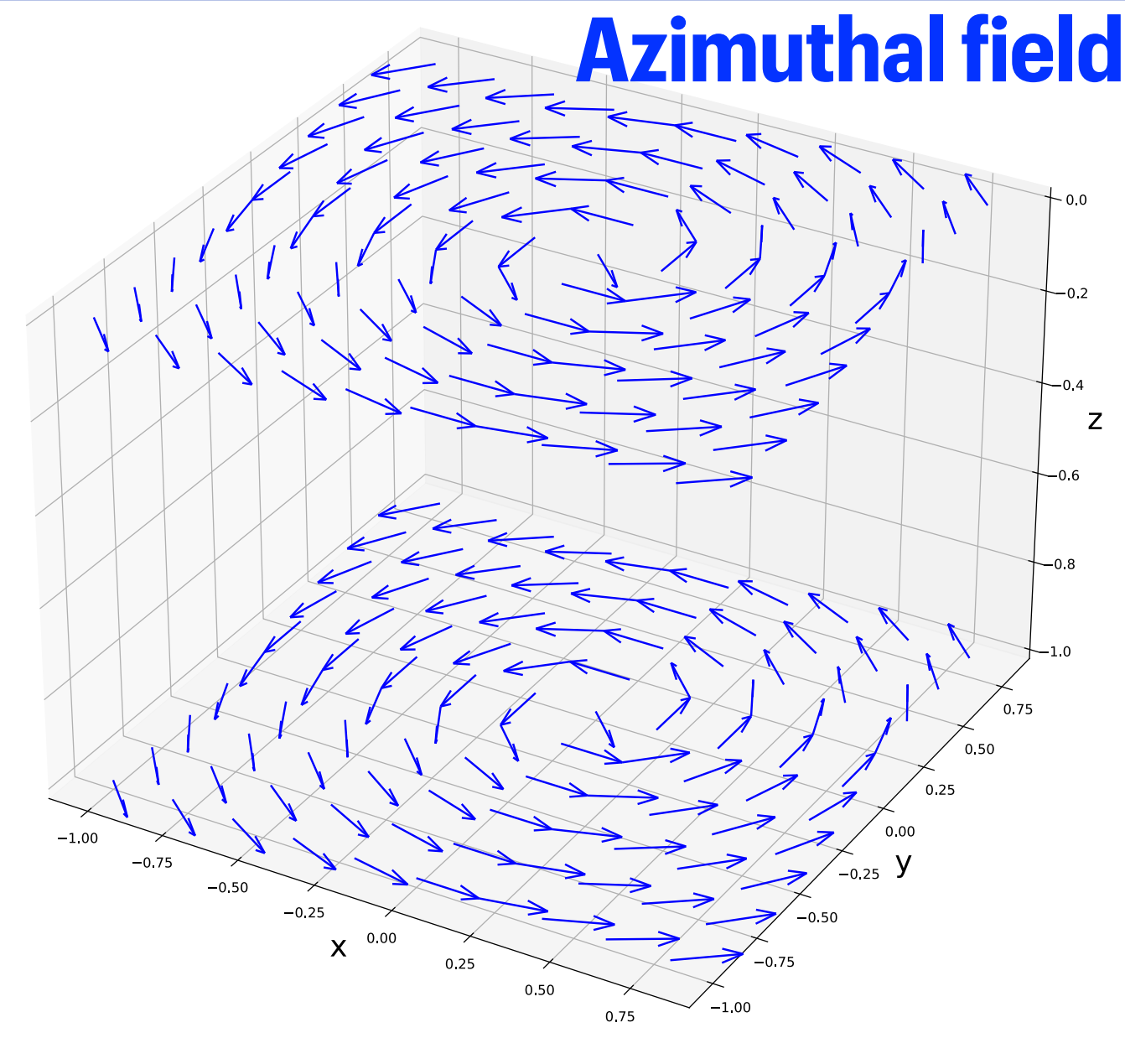
**Parallel
decorrelation**



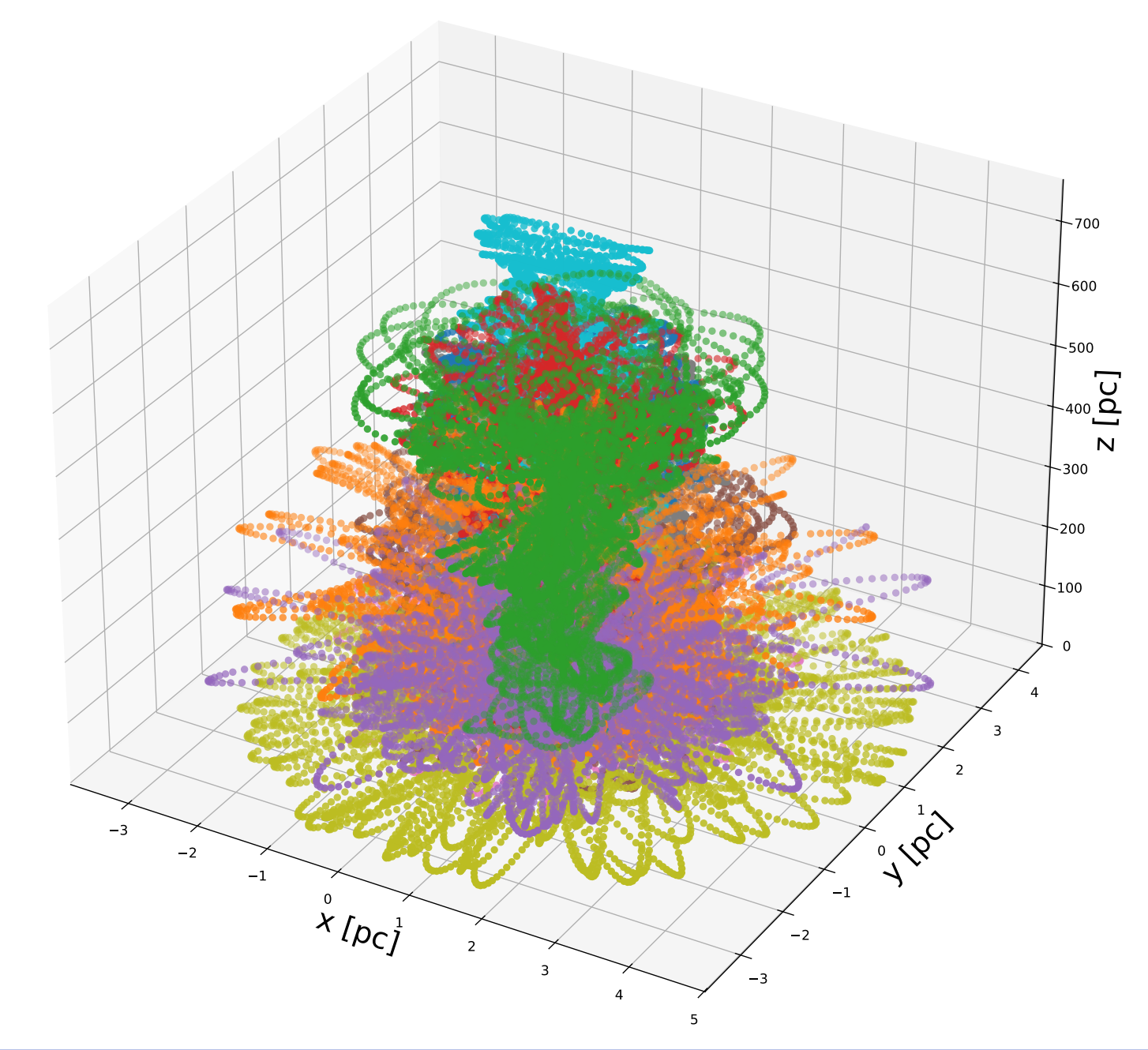
**Antisymmetric
decorrelation**



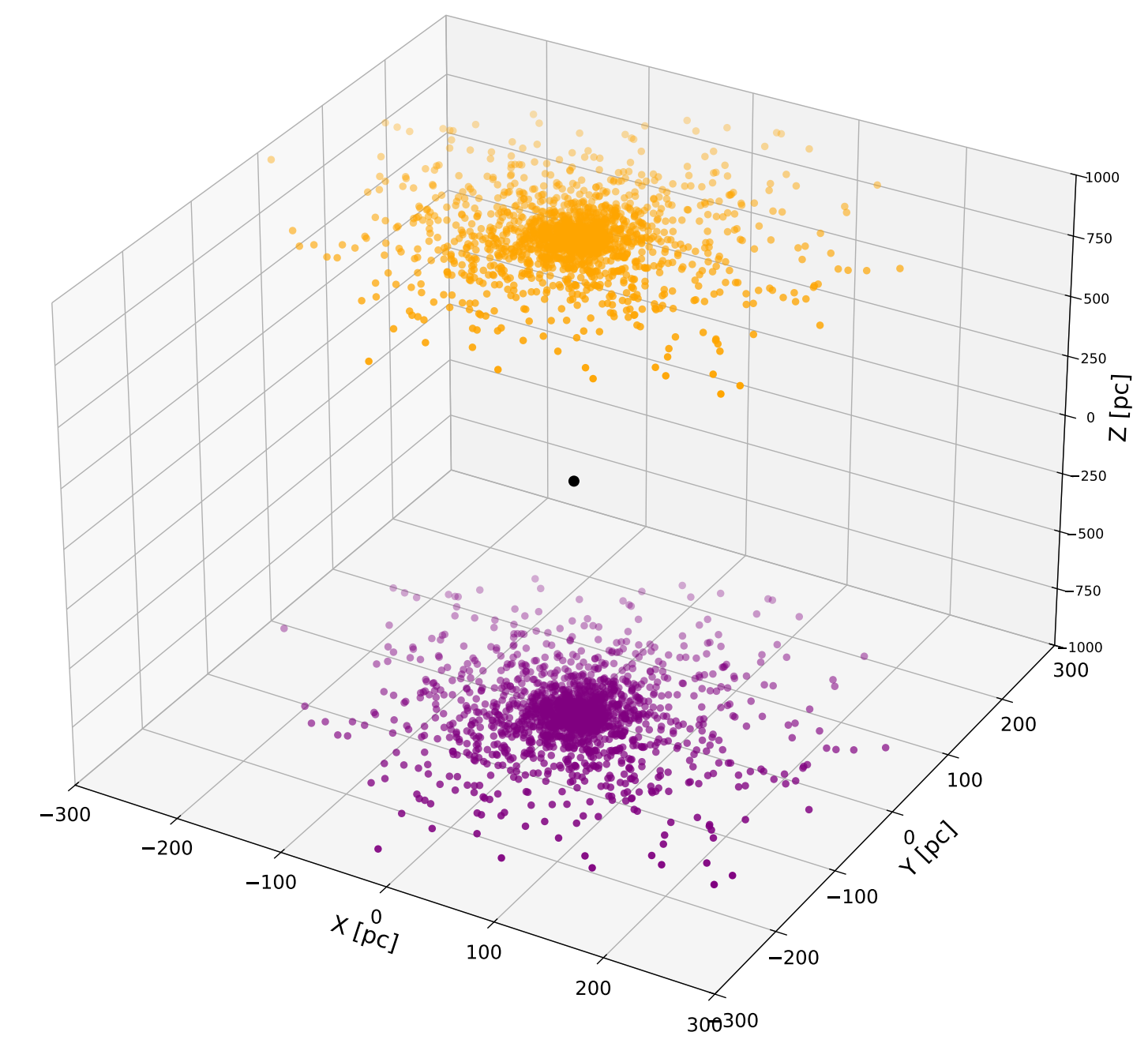
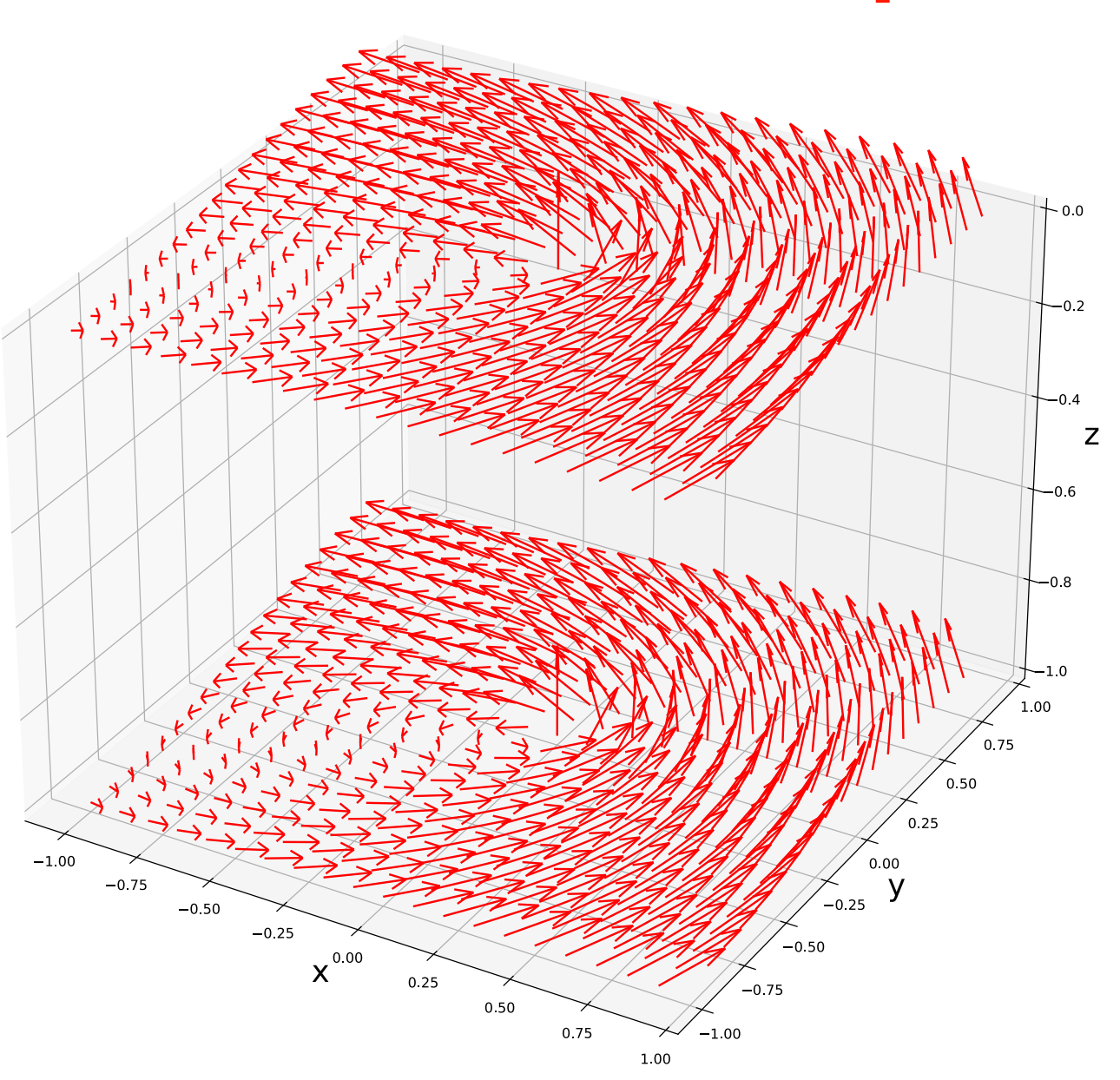
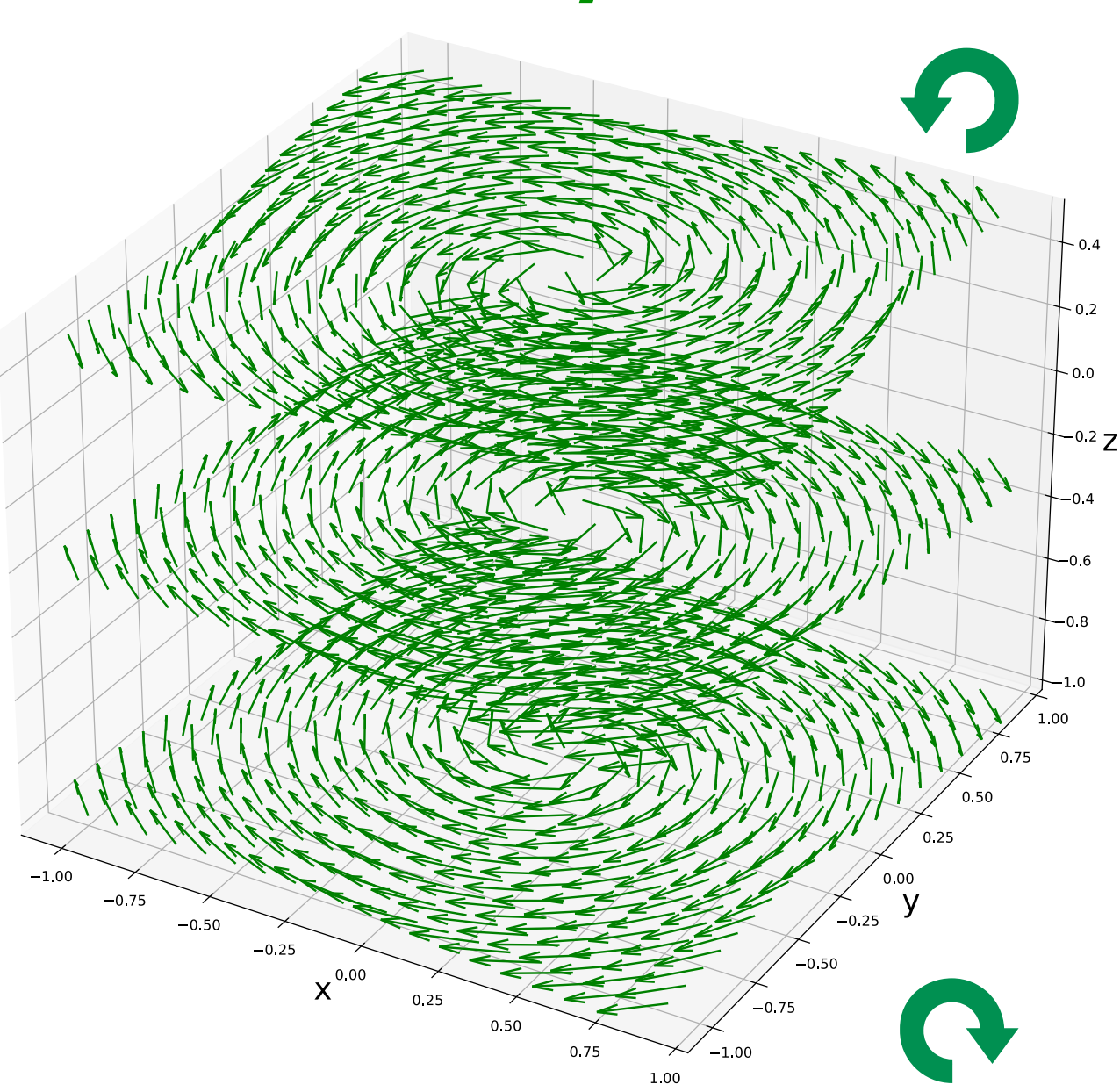
Cosmic ray escape time in Galactic magnetic fields



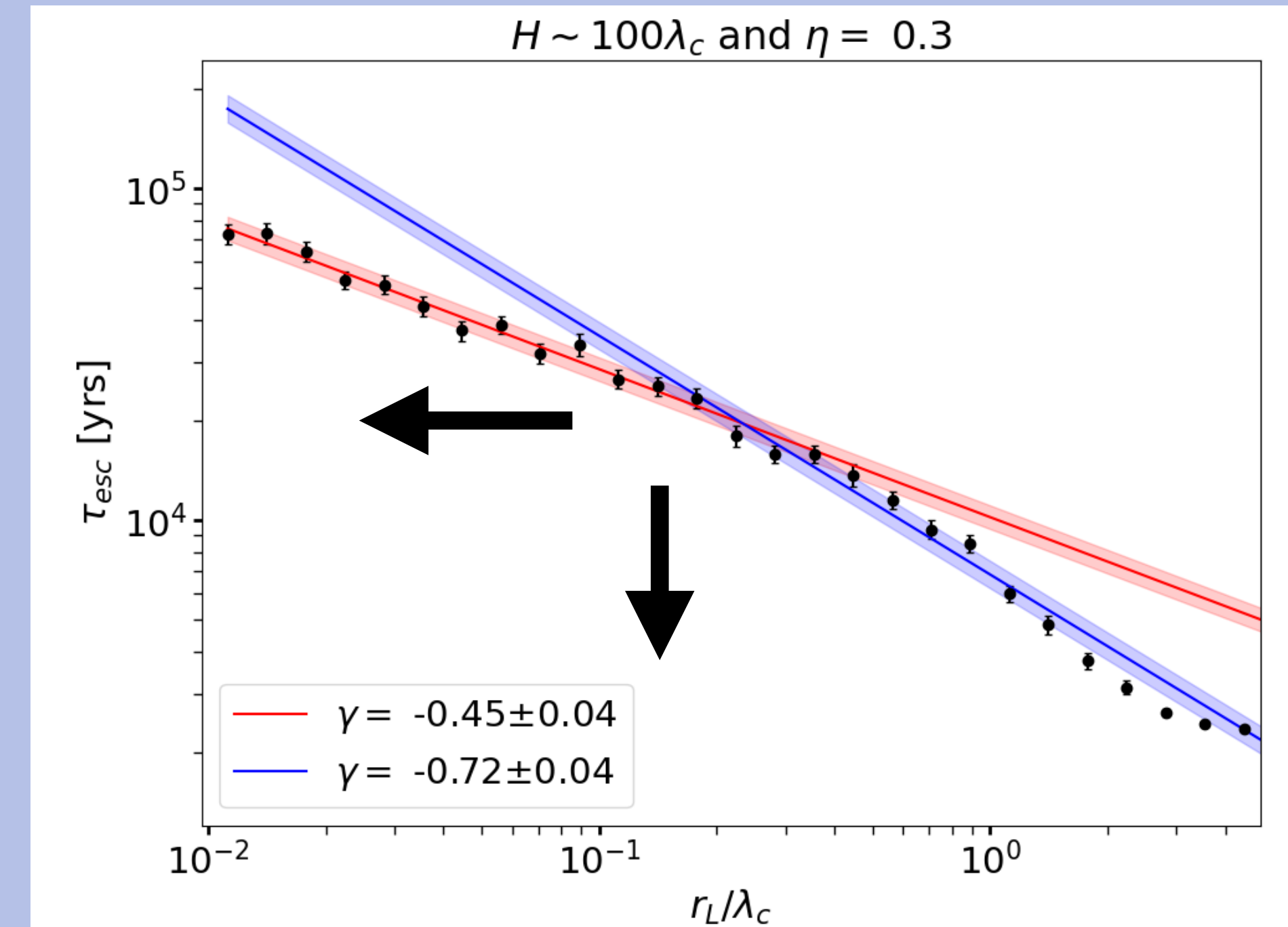
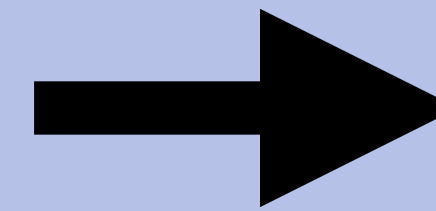
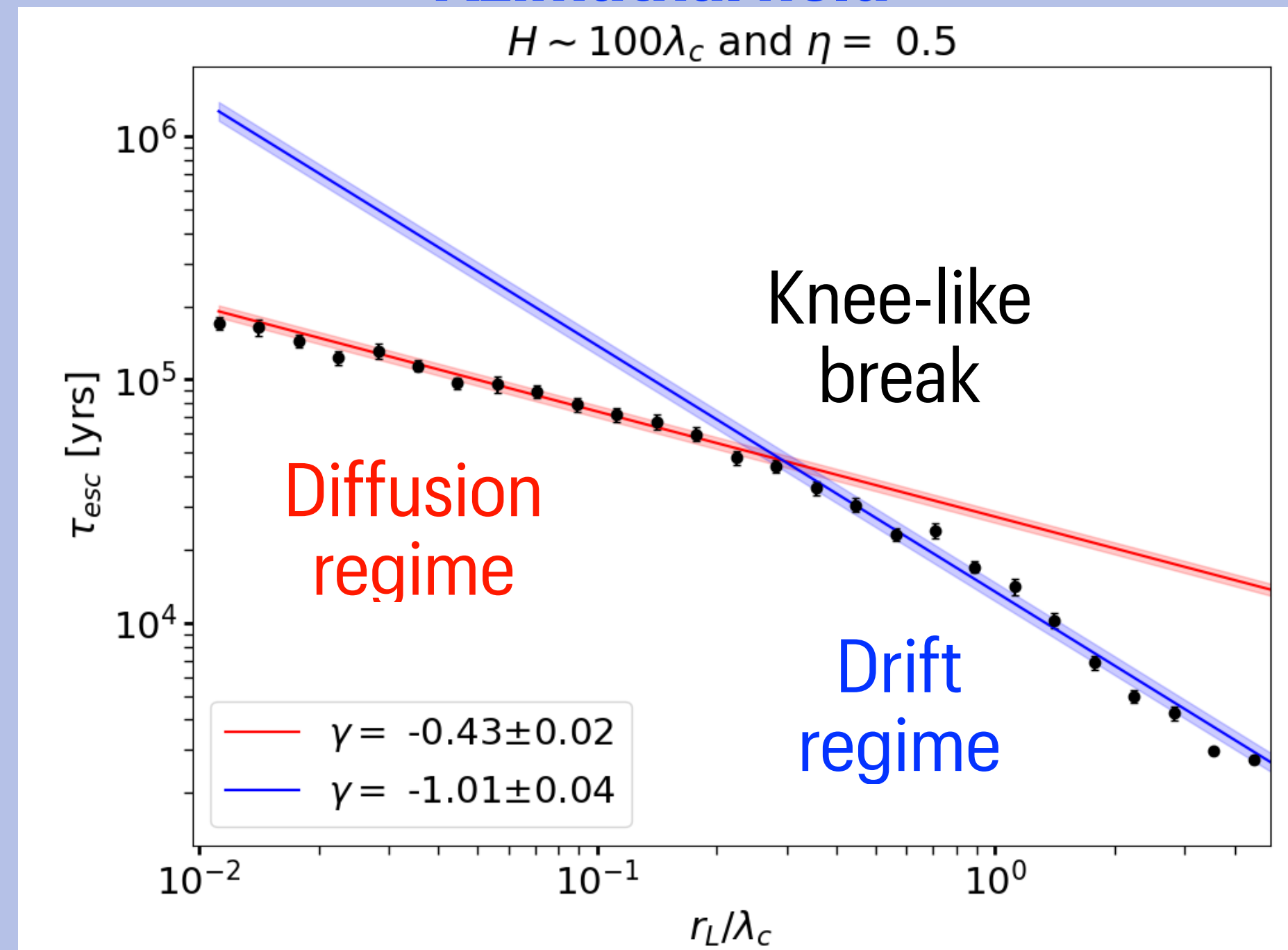
Particle injection



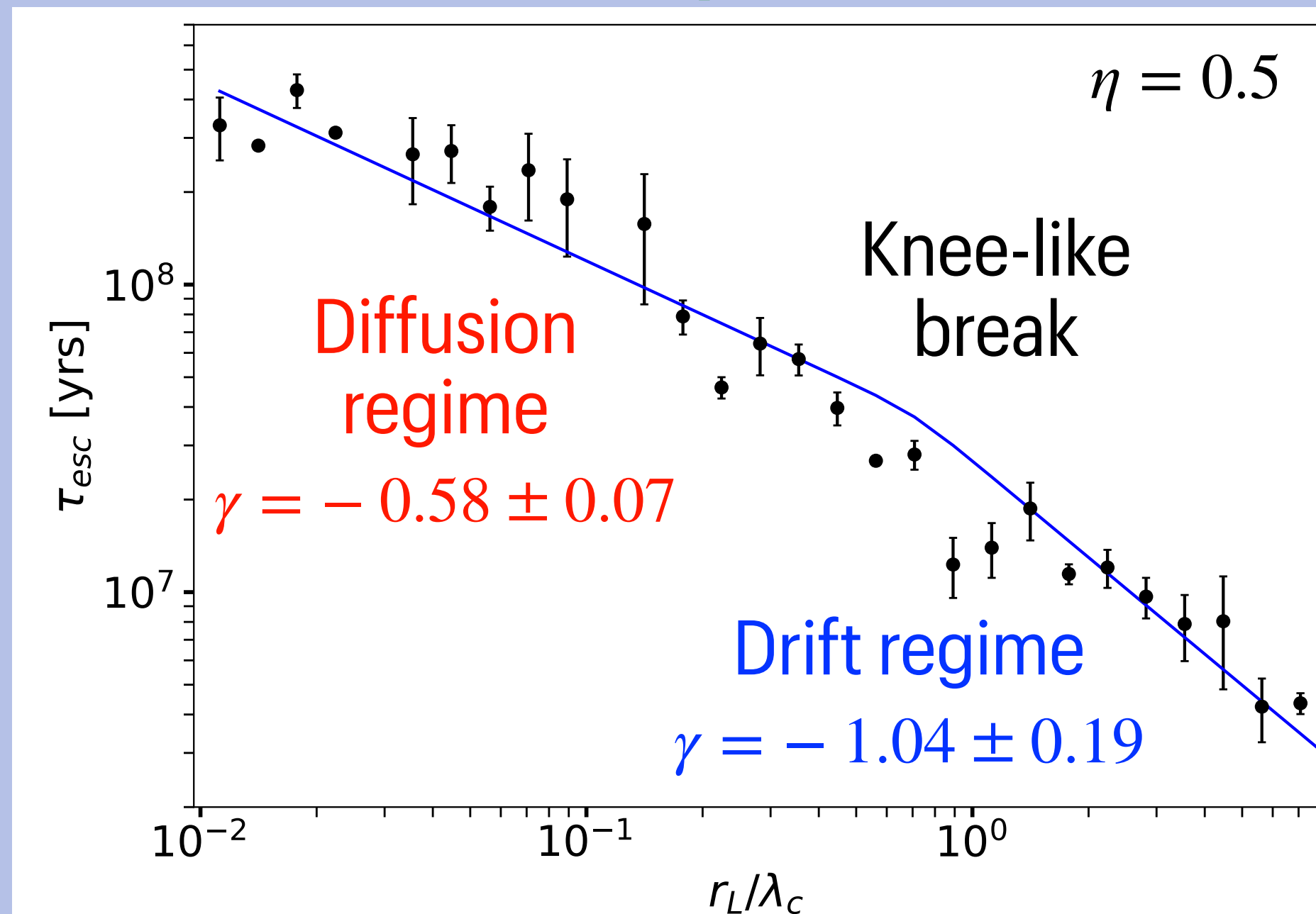
Azimuthal antisymmetric field **Field with vertical component**



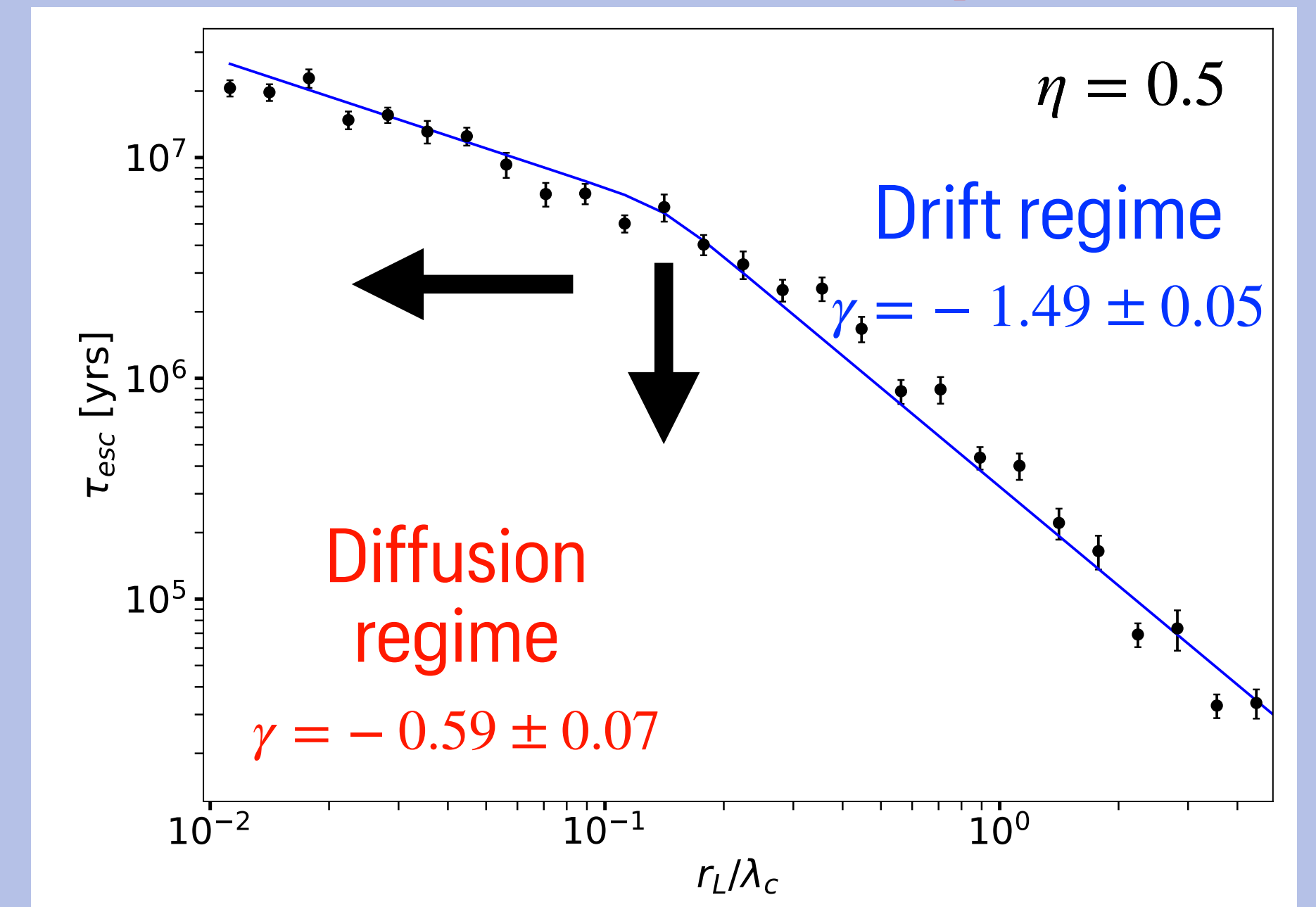
Azimuthal field



Azimuthal antisymmetric field



Field with vertical component

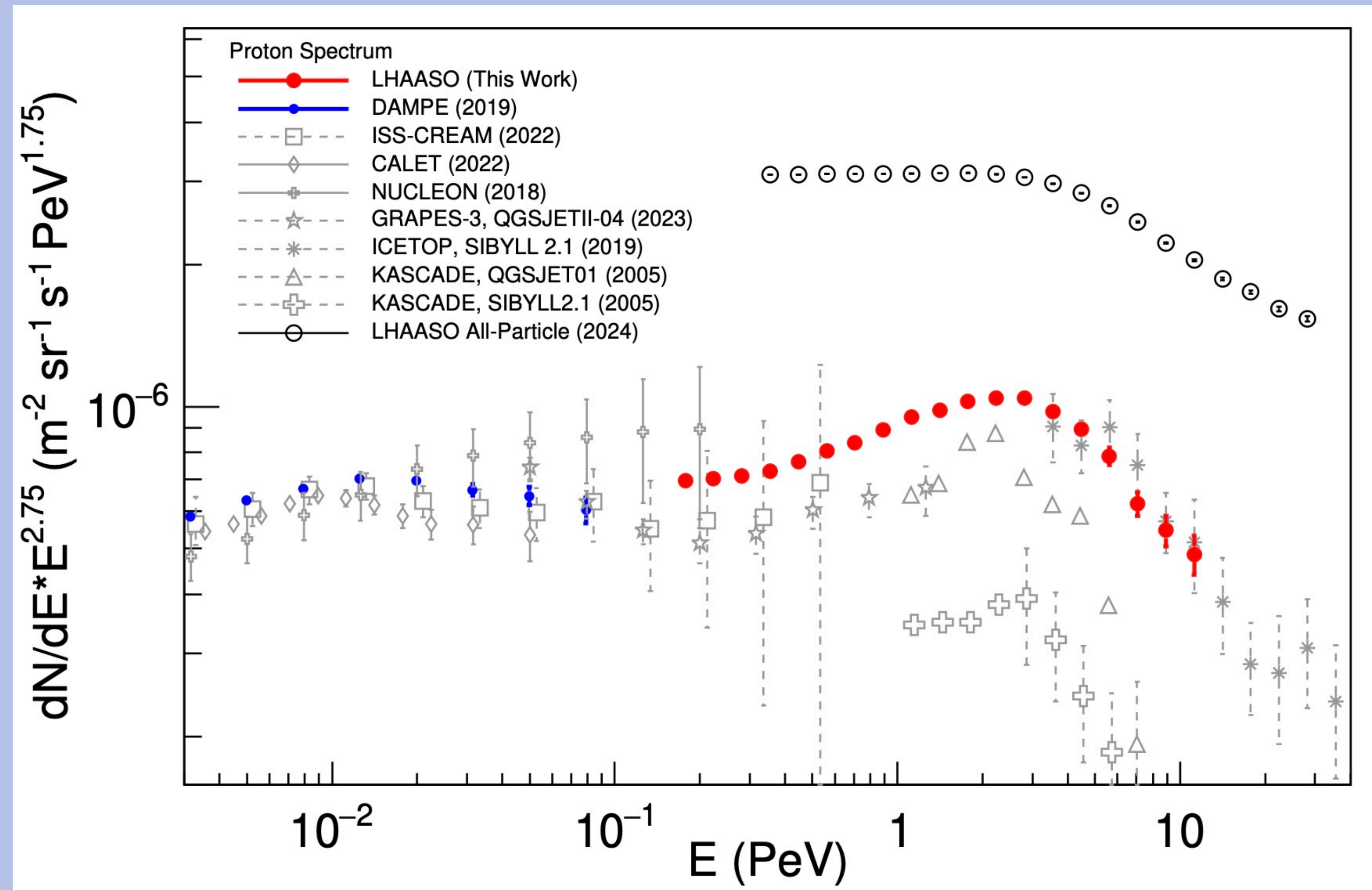


Motivation: LHAASO proton knee

- LHAASO connecting low- (< 100 TeV) and high-energy (> 1 PeV) proton measurements.
- Spectral breaks at $R \sim 300$ GV, $R \sim 10$ TV and $R \sim 10^2$ TV (GRAPES-3).
- Discrepancy of proton flux measurements between ground-based experiments.

Aartsen et al., 2019 (IceTop),
Antoni et al., 2005 (KASCADE),
Finger, 2011 (KASCADE)

LHAASO Coll., 2025



- **Heavy component** ($A > 4$) added by comparison between all-particle spectrum and sum of proton and helium spectra, assuming spectral shape conserved in rigidity.

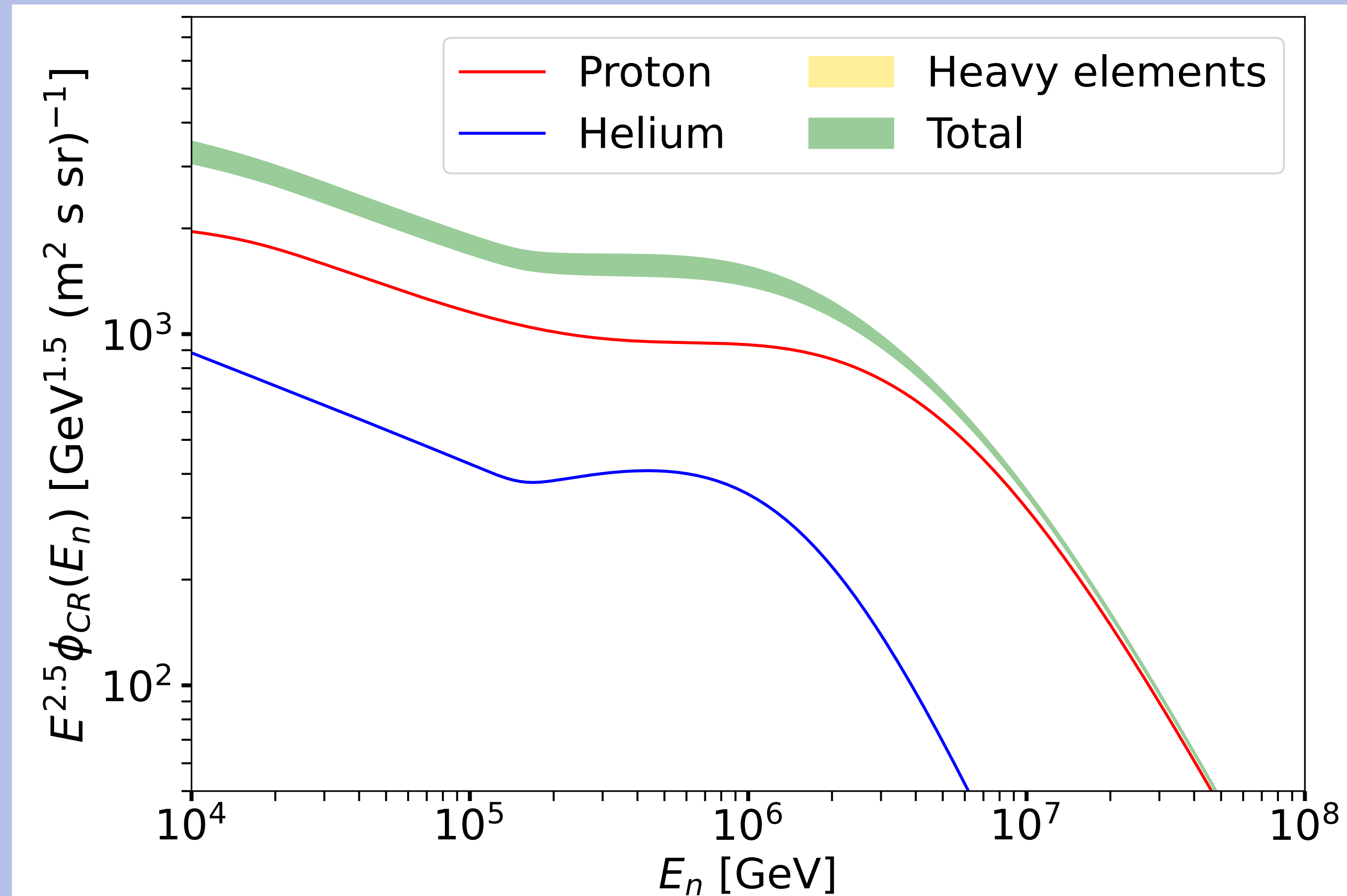
Relevant flux is in energy per nucleon, for which **proton component is dominant**

$$\phi_{\text{CR}}(E_n) = \sum_A A^2 \phi_A(AE_n)$$

$$\phi_{\text{CR},\odot}(E_n) = \phi_p(E_n) + (1 + k) \phi_{\text{He,CR}}(E_n)$$

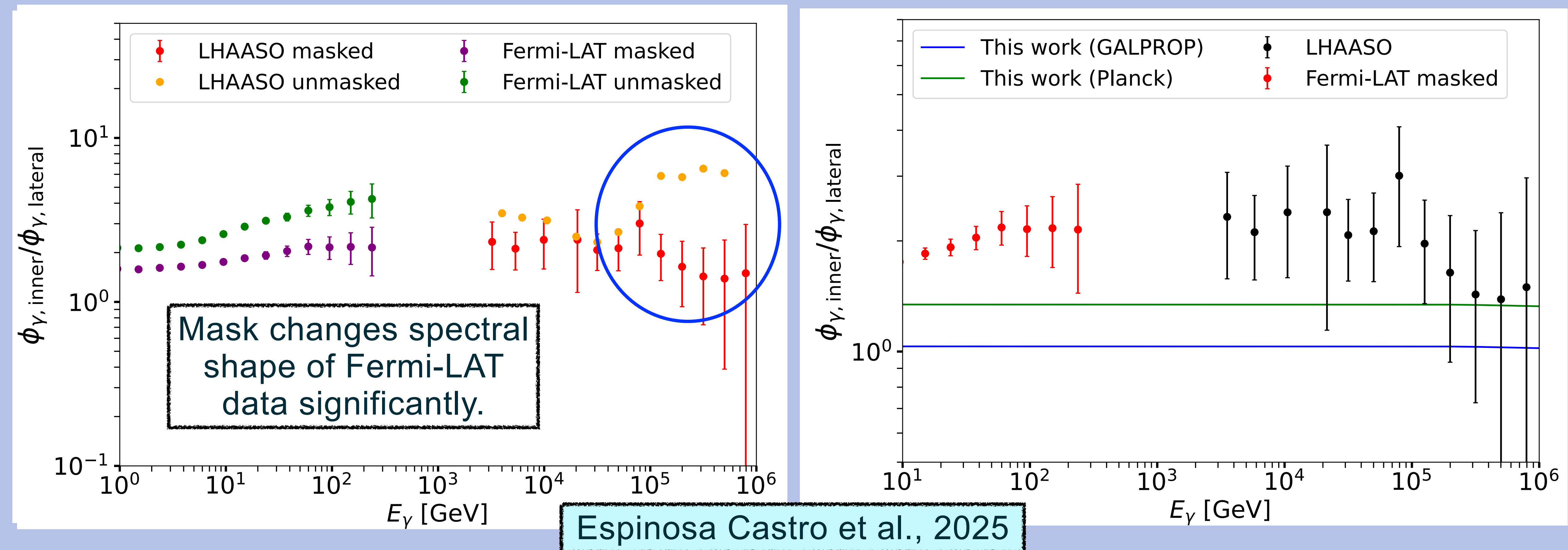
$$\text{with } k = \frac{\phi_{\text{heavy}}(E)}{\phi_{\text{He}}(E)} \left(\frac{A}{A_{\text{He}}} \right)^{2-\alpha_1(\text{He})}$$

Take-home message:
Diffuse gamma-rays probe
the proton flux at the knee



Approximately energy independent ratio, determined by **number of targets** and **cosmic ray density distribution**.

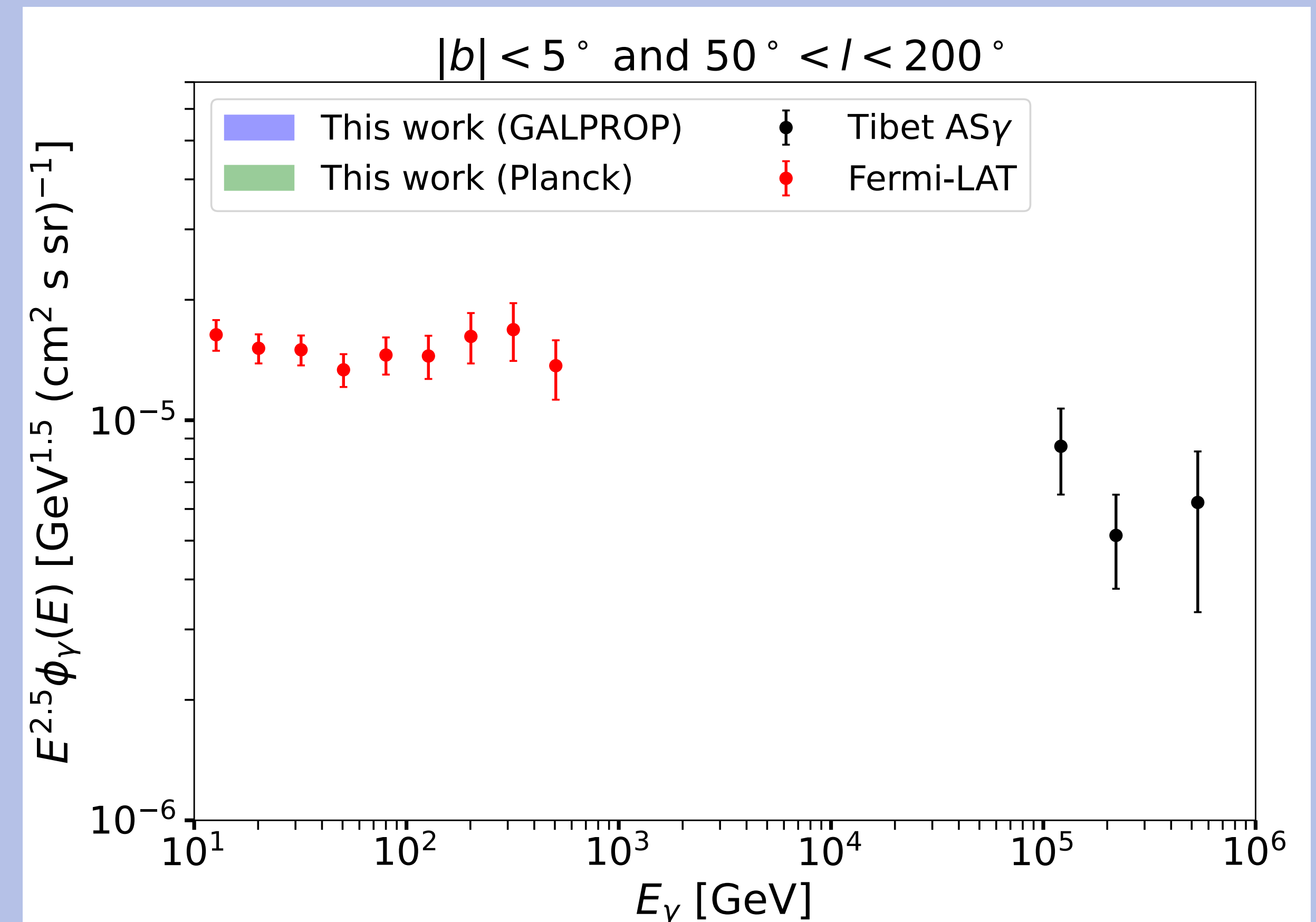
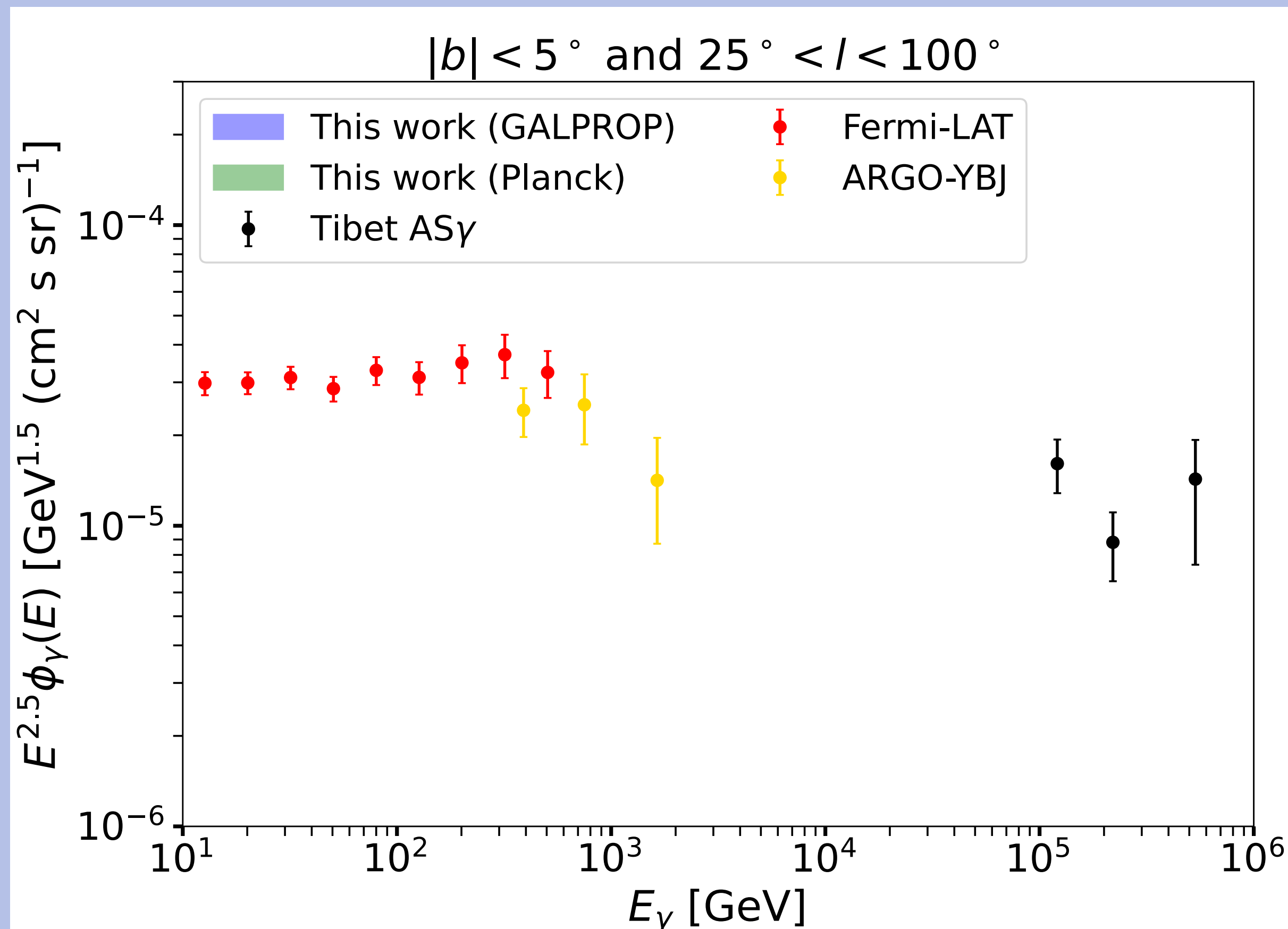
- Hardening expected from Fermi-LAT data extrapolated to higher energies is incompatible with VHE measurements.
- No distinction from space-dependent to space-independent spectrum in LHAASO regions, possibly due to mask.

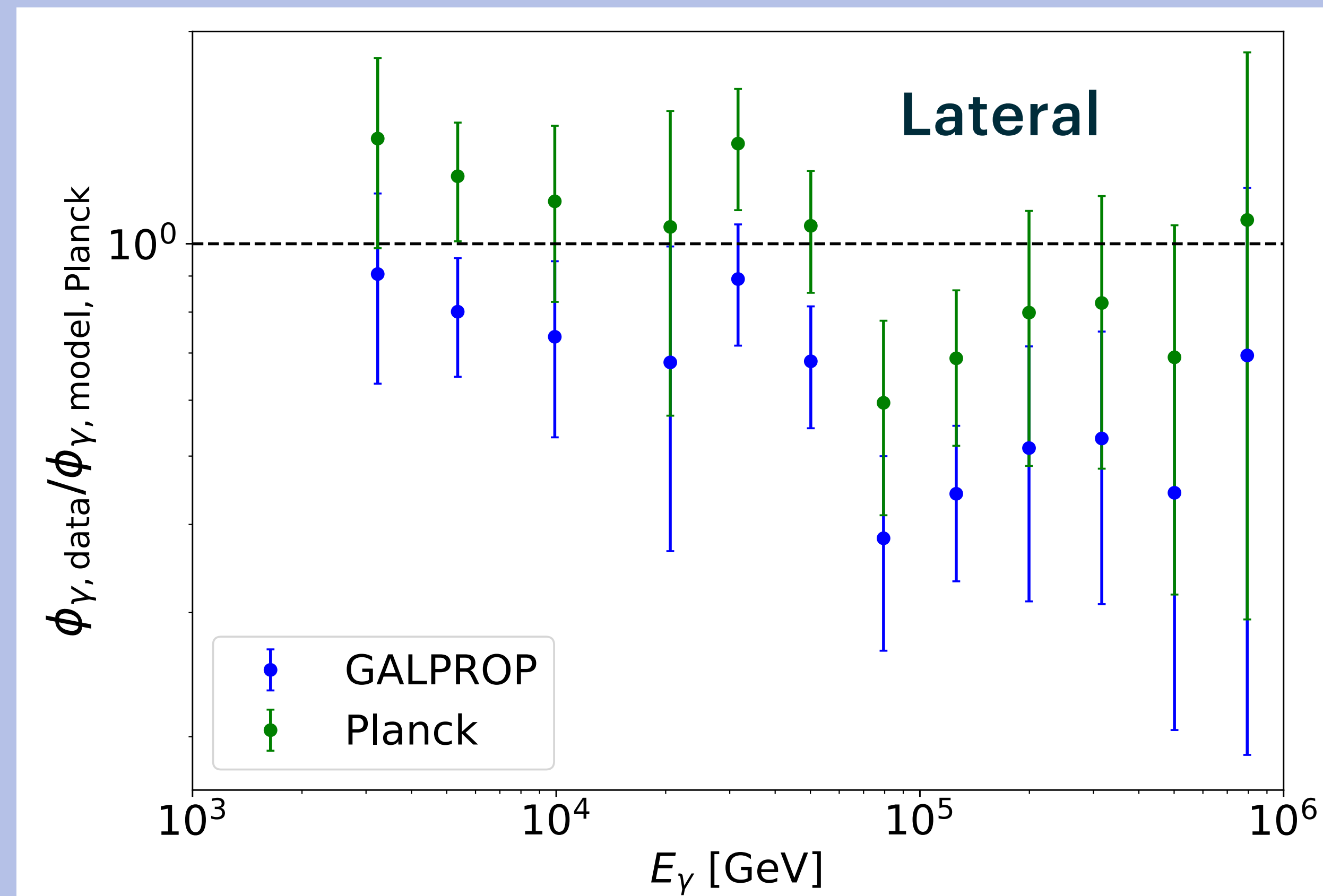
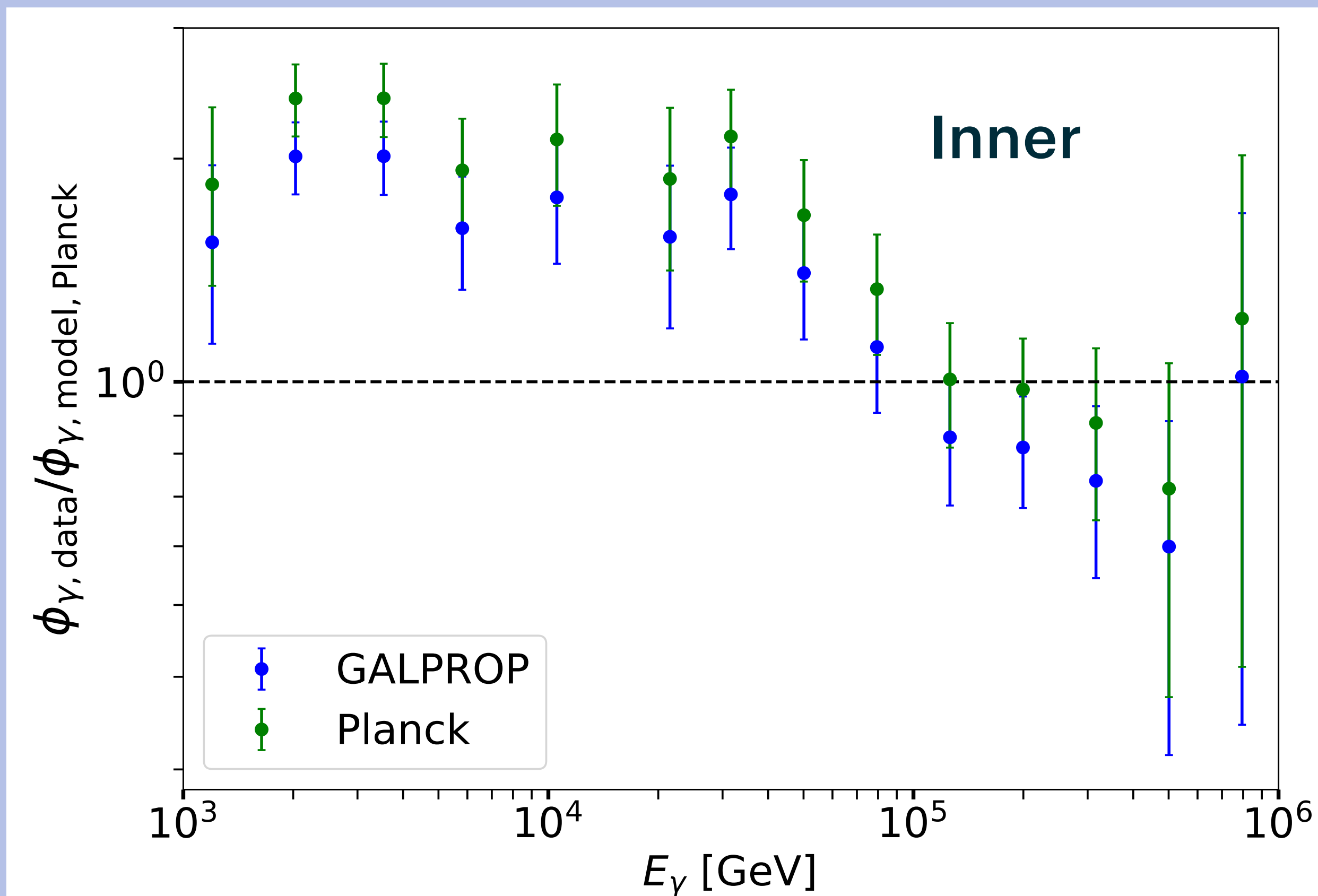


Gamma-ray Diffuse Emission: Comparison with Tibet AS γ

- Underestimation of flux in both regions. Possible contribution of unresolved component.
- Planck column density template $\sim 20\%$ lower in inner region and $\sim 25\%$ lower in lateral region.

(See also Vecchiotti et al., 2022)





Espinosa Castro et al., 2025

Approximately energy independent ratio, determined by **number of targets** and **cosmic ray density distribution**.

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