

## Searching for the most stable switching laws of linear switched systems via antinorms

Friday, 21 June 2019 09:15 (45 minutes)

We deal with discrete-time *linear switched system* of the form  $x(n+1) = A_{\sigma(n)} x(n)$ ,  $\sigma : \mathbf{N} \rightarrow \{1, 2, \dots, m\}$ , where  $x(0) \in \mathbf{R}^k$ , the matrix  $A_{\sigma(n)} \in \mathbf{R}^{k \times k}$  belongs to a finite family  $\text{cal } F = \{A_i\}_{1 \leq i \leq m}$  associated to the system and  $\sigma$  denotes the *switching law*.

It is known that the *most stable switching laws* are associated to the so-called *spectrum-minimizing products* of the family  $\text{cal } F$ . Moreover, for a family  $\text{cal } F$  of matrices that share an invariant cone  $K$  and is normalized (i.e., its *lower spectral radius*  $\tilde{\rho}(\text{cal } F)$  is equal to 1), for any initial value  $x(0)$  in the interior of  $K$  the *most stable trajectories* lie on the boundary of the *unit antiball* of a so-called *invariant Barabanov antinorm*. Under suitable conditions, a canonical constructive procedure for Barabanov antinorms of polytope type has been recently proposed by Guglielmi & Z. (2015).

Still for families sharing an invariant cone  $K$ , in this talk we first show how to provide lower bounds to  $\tilde{\rho}(\text{cal } F)$  by a suitable adaptation of the Gelfand limit to the setting of antinorms, which could be of some practical interest when the above mentioned constructive procedure fails.

Then we consider a family of matrices  $\text{cal } F$  that share an *invariant multicone*  $K_{mul}$  (see the recent papers by Brundu & Z. (2018, 2019)) and show how to generalize some of the known results on antinorms from the case of families sharing an invariant cone. These generalizations are of interest because invariant multicones may well exist when invariant cones do not.

This is a joint work with N. Guglielmi, Gran Sasso Science Institute, Italy

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