# <span id="page-0-0"></span>The environment of pulsar halo progenitors

Lioni-Moana Bourguinat Carmelo Evoli, Pierrick Martin, Sarah Recchia





Geminga as seen by Chandra and Spitzer Credits: X-ray: NASA/CXC/PSU/B. Posselt et al; Infrared: NASA/JPL-Caltech

# TeV Halos



**FS** Stage 1 (t < 10 kvr) Stage 2 (t ~ 10 - 100 kvr)  $\overline{c}$ ້າເ pulsar velocity ∸ ISM density gradient SNR (in all 3 panels) **ICM ISM**  $-1$  supernova Stage 3 (t > 100 kvr) remnant halo pulsar pulsar wind term, shock **SNR** pulsar wind nebula **ISM** >10 TeV e trajectory > 1 TeV gamma-r

Figure: HAWC sky map of TeV emission from Geminga and its neighbour PSR B0656+14. Credits: HAWC Collaboration

Figure: Sketch of the main evolutionary stages of a pulsar wind nebula. Credits: Giacinti et al. [\(2020\)](#page-32-0)

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#### Standard assumption

Pulsar outside the SNR  $\rightarrow$  Low diffusion coefficient problem [Abeysekara et al.

[\(2017\)](#page-32-1)]

# Solving the diffusion coefficient problem

#### Theoretical explanations

- **Cosmic-ray induced turbulence** [Evoli, Linden, et al. [\(2018\)](#page-32-2), Mukhopadhyay et al. [\(2022\)](#page-33-0)]
- **Environment induced turbulence** [Fang et al. [\(2019\)](#page-32-3), Schroer et al. [\(2022\)](#page-34-0)]

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### Which medium are the leptons probing when we see a TeV halo?

# **Where is the pulsar at a given age?**

### Method

Computation of the escape time from the SNR of a population of pulsars using a Monte Carlo approach for 3 models:

- ISM (interstellar medium)
- CSM (circumstellar medium)
- SB (superbubble)

# Property of the pulsars: Kick velocity

#### Kick velocity distribution

Taken from Faucher-Giguère et al. [\(2006\)](#page-32-4), modulus of all components:

$$
f(v_k^{x,y,z}) = w \mathcal{N}(v_k, \sigma = 160 \text{ km/s}) + (1 - w) \mathcal{N}(v_k, \sigma = 780 \text{ km/s}) \quad (1)
$$

with  $w = 0.90$ .



Figure: PDF of the kick velocity of pulsars.

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# ISM model

### Assumptions

- **Constant interstellar medium** around the CC SN
- $\bullet$  Distributions of  $E_{SN}$  and  $n_{ISM}$

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- Distributions of  $E_{SN}$  and  $n_{ISM}$

### SNR evolution

Analytical solutions following Cioffi et al. [\(1988\)](#page-32-5), compared with the calculator by Leahy and Williams [\(2017\)](#page-33-1):

- Sedov-Taylor phase
- **•** Pressure-Driven Snowplough phase
- (Momentum Conserving Stage)
- Merger with the ISM

# ISM model: SN energy and ISM density



Figure: Lognormal distributions, following Leahy, Ranasinghe, et al. [\(2020\)](#page-33-2). Computed by assuming a constant ISM density surrounding each of 43 SNe.

### ISM model: Escape time



Figure: Probability of pulsars being inside the **SNR** as a function of time for the **ISM** model. Characteristic ages of pulsars are orders of magnitude, taken from the [catalog](https://www.atnf.csiro.au/research/pulsar/psrcat/) of Manchester et al. [\(2005\)](#page-33-3).

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### Assumptions

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#### **Process**

- Pick a random progenitor mass from a Galactic Initial Mass Function (IMF),
- **Star properties** [Seo et al. [\(2018\)](#page-34-1)],
- **Bubble properties** [Weaver et al.

[\(1977\)](#page-34-2), Härer et al. [\(2023\)](#page-33-4)].

Neglecting post-MS phases for the wind and bubble structure.

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Neglecting post-MS phases for the wind and bubble structure.



Figure: Density profile in the CSM, based on Weaver et al. [\(1977\)](#page-34-2).

# CSM model: Comparing the shell mass and the SNR mass

### Parameters for a star of  $M_{ZAMS} = 8 M_{\odot}$

- Bubble radius  $r_b = 20$  pc,
- Surrounding ISM density of  $n_{ISM} = 1$  cm<sup>-3</sup>,
- Mass lost in winds  $\Delta M_{MS} = 0.1 M_{\odot}$  and  $\Delta M_{RSG} = 3.4 M_{\odot}$
- **•** Ejecta mass is  $M_{\rm ZAMS} - \Delta M_{\rm MS} - \Delta M_{\rm RSG} M_{\text{pulsar}} = M_{\text{ei}} = 3.1 M_{\odot}$
- Mass swept in the bubble by the SNR is the mass lost in winds.

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#### **Computations**

$$
M_{\text{shell}} = \frac{4\pi}{3} \rho_{\text{ISM}} r_{\text{b}}^3 = 755 \text{ M}_{\odot} \quad (2)
$$

Mass ratio:

$$
\frac{M_{\text{shell}}}{M_{\text{ej}} + \Delta M} = 116\tag{3}
$$

Shell stops the expansion of the SNR

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Shell stops the expansion of the SNR

#### Conclusion

Boundary: bubble radius instead of the SNR

# SB model

#### **Assumptions**

- Point-like cluster surrounded by a superbubble Meaver et al. [\(1977\)](#page-34-2)]
- <code>Ambient density of  $\rm \textit{n}_{ISM} \sim 100 \text{ cm}^{-3}$  [Parizot et al. [\(2004\)](#page-33-5)]</code>
- The SNR is very fast or merges within the SB [Mac Low et al. [\(1988\)](#page-33-6)]

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#### Process

Pick a random cluster mass following a cluster  $IMF$   $[Postegies Zwart et al. (2010)]$  $[Postegies Zwart et al. (2010)]$  $[Postegies Zwart et al. (2010)]$ .

Populate with stars following the Galactic IMF.

Compute the **cluster luminosity** and SB radius  $[Weaver et al. (1977)]$  $[Weaver et al. (1977)]$  $[Weaver et al. (1977)]$ , Härer et al. [\(2023\)](#page-33-4)].

Pick a **random massive star** and find the associated MS time  $[See set al. (2018)]$  $[See set al. (2018)]$  $[See set al. (2018)]$ .

Creation of a pulsar at the MS time and propagation of both pulsar and SB radius.

# Comparing the probability of being inside the boundary



Figure: Probability of pulsars being inside the **bubble (SB)** as a function of time for the **CSM (SB) models** respectively.



 $^{\rm 1}$ of  $\rm O$  stars[de Wit et al. [\(2005\)](#page-32-6)]



### More on Geminga

Hints that Geminga is in a hot ionized medium:

- $\bullet$  No H<sub>o</sub> lines in the near vicinity [Caraveo et al. [\(2003\)](#page-32-7)]
- **•** Proximity to Gemini  $H_{\alpha}$  Ring bubble [Knies et al. [\(2018\)](#page-33-8)]

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### Comparing the probability of being inside the boundary Changing the maximum star mass



Figure: Probability of pulsars being inside the **bubble (SB)** as a function of time for the **CSM (SB)** models respectively.

Two curves are added by changing the maximum mass of massive stars that create pulsars from 120 M $\odot$  to 40 M $\odot$  following Sukhbold et al. [\(2016\)](#page-34-3).

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### Comparing the probability of being inside the boundary Special case: exiting the SNR inside the bubble



Figure: Probability of pulsars being inside the **bubble (SB)** as a function of time for the **CSM (SB)** models respectively. Max mass 40 M<sub>☉</sub>.

The green curve corresponds to the escape time of pulsars from the SNR inside the CSM, and the orange inside the SB.



Figure: Evolution of the available energy of a pulsar as a function of time. Towards the later ages there are integration artifacts.  $P_0 = 100$  ms,  $v_k = 280$  km/s as in Evoli, Amato, et al. [\(2021\)](#page-32-8).

# Energy available for escaping pulsars





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Figure: Distribution of available energies after escape. The initial period distribution comes from *'*-ray observations in Watters et al. [\(2011\)](#page-34-4).

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Figure: Distribution of available energies after escape. The initial period distribution comes from *'*-ray observations in Watters et al. [\(2011\)](#page-34-4).

Pulsars **DO NOT** have much energy left + leptons represent only a percentage of this energy

# **Summary**

#### Main questions

Which medium are the leptons probing when we see a TeV halo? Where is the pulsar at a given age?

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Which medium are the leptons probing when we see a TeV halo? Where is the pulsar at a given age?

#### **Conclusions**

- Typically assumed:  $\sim$  50 kyr and probe the ISM.
- We find instead a majority of  $\gtrsim$  100 kyr pulsars are inside the CSM/SB.
- Are Geminga and PSR  $B0656+14$  in a **hot and turbulent** environment?
- How are CSM/SB connected to TeV halos?
- How about similar pulsars in radio?

#### In the same project

- Add the OB star association as a possible model for the evolution of the system
- Create a **Galactic statistic** assuming probabilities of pulsars being born in one or another region

### New projects: looking at the injection

- Investigate the contribution of **millisecond pulsars** to the CR lepton spectrum
- Work on the injection of leptons in the **interaction between the** PWN and the SNR using MHD simulations

### Events attended

### Conference

Talk in person at RICAP-2024 (Roma International Conference on Astro-Particle Physics), Roma Tre, Frascati

#### Workshop

- **•** Participation in person to the **Workshop on Numerical** Multi-Messenger Modelling by Astroparticule et Cosmologie, Paris
- Participation in person to the **Conference in memory of Veniamin** Berezinskii, GSSI, L'Aquila

### Summer School

• Participation in person to the MPIK-CDY School on the Future of Gamma-Ray Astronomy by the Max Planck Institute fur Kernphysik, Heidelberg

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### CSM model Theoretical framework for the SNR shock

### Time (Numerically integrated)

$$
t(R_{\rm s})=\int_0^{R_{\rm s}}\frac{1}{u_{\rm s}(r)}{\rm d}r\tag{4}
$$

### Speed (Analytical)

$$
u_{\rm s}(R_{\rm s})=\frac{\gamma+1}{2}\left[\frac{2\alpha E_{\rm SN}}{M^2(R_{\rm s})R_{\rm s}^\alpha}\times\int_0^{R_{\rm s}}r^{\alpha-1}M(r){\rm d}r\right]
$$
(5)  
6 $(\gamma-1)/(\gamma+1)$ .

### Mass (Analytical)

with  $\alpha =$ 

$$
M(r)=M_{\rm ej}+4\pi\int_0^r r'^2\rho(r'){\rm d}r'
$$

(6)

### The numbers (model from Weaver et al. [\(1977\)](#page-34-2))

Wind region  $(R_s < r_w)$ :

$$
\rho_{\rm w}(R_{\rm s})=\frac{\dot{M}}{4\pi\,\mu_{\rm w}R_{\rm s}^2}
$$

Bubble region  $(r_w < R_s < r_b)$ :

$$
\rho_{\rm b}(R_{\rm s})=\rho_{\rm b}
$$

Shell region  $(r_b < R_s < r_{ISM})$ :

$$
\rho_{\text{shell}} = \frac{M_{\text{shell}}}{V_{\text{shell}}} = \frac{\frac{4\pi}{3}r_{\text{b}}^3 \rho_{\text{ISM}}}{\frac{4\pi}{3} \left(r_{\text{ISM}}^3 - r_{\text{b}}^3\right)}
$$

ISM region  $(r_{\rm ISM} < R_{\rm s})$ :

$$
\rho_{\text{ISM}}=1\ \text{cm}^{-3}
$$



Figure: Luminosity distribution.



Figure: Mass loss distribution.



Figure: SNR ejecta mass distribution.



Figure: Wind speed distribution.



Figure: Wind radius distribution.



Figure: Main sequence time distribution.



#### Figure: Bubble radius distribution.

#### Formula

From Weaver et al. [\(1977\)](#page-34-2) and Härer et al. [\(2023\)](#page-33-4):

$$
r_b = 21\ \textrm{pc}\ \zeta_b^{1/5} L_{36}^{1/5} n_{\textrm{ISM},1}^{-1/5} t_6^{3/5}\ \ (7)
$$



Figure: Shell mass/SNR mass distribution. We show for both the ejecta mass and the swept mass. Naturally, the swept mass is higher than the ejecta mass, resulting in a lower (by less than an order of magnitude) ratio. The shape in two parts of the orange curve is linked to the shape of the bubble radius (which is the determining factor for the parameter).

### CSM model Density profile



Figure: Density profile in the CSM, based on Weaver et al. [\(1977\)](#page-34-2).

## CSM model Mass profile



Figure: Accumulated mass profile in the CSM, analytically computed from the density profile



Figure: Accumulated speed profile in the CSM, analytically computed from the mass profile

### CSM model Conditions

### Radiative phase

$$
t_{\text{rad}} = \frac{3}{2} \frac{k_{\text{b}} T}{n \Lambda(T)}
$$

with  $\mathsf{\Lambda}(\mathcal{T})=1.6\times10^{-19}$   $\mathcal{T}^{-1/2}$  erg/cm $^3/$ s. We always go radiative when reaching the shell.

### Merger with the bubble shell

$$
u_s(R_s) = \beta c_{sound}(T(R_s))
$$

with  $\beta = 3$  and the speed of sound  $c_{\text{sound}}$  depending on the temperature profile found in Weaver et al. [\(1977\)](#page-34-2). Since the SNR stops inside the shell, it merges there.



Figure: Superbubble radius distribution.