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Abstract

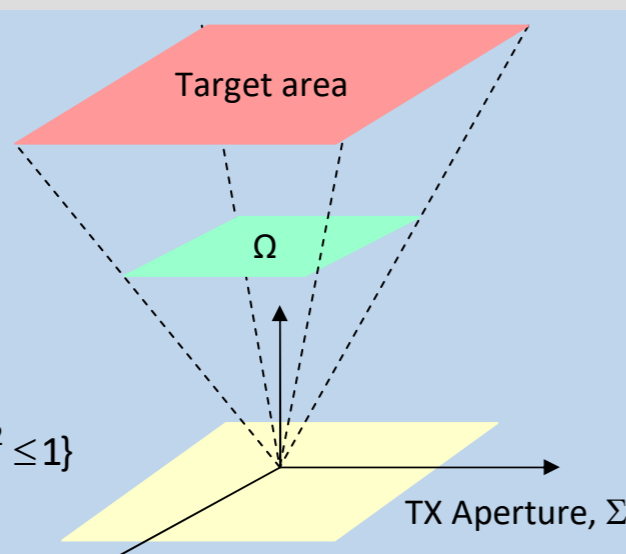
Abstract — Long-range wireless power transmission (WPT) systems comprise a transmitting (TX) device capable of focusing the beam towards a desired region, usually consisting of a phased array (PA) antenna, and a receiving (RX) device, namely a rectenna, converting the electromagnetic power of the impinging microwave radiation into direct current. To maximize the end-to-end transmission efficiency, the transmitter must be able to focus the power on a limited spatial region, possibly just as large as the rectenna aperture. This imposes non-negligible challenges in the design of the transmitting antenna system, further highlighted when the TX and RX antennas are located far away. Additionally, conventional PAs allow for highly flexible beam-forming but they are extremely expensive and difficult to realize if large antennas are needed. In this context, the proposed research activity focuses on the study of innovative unconventional PA solutions based on modular architectures able to offer optimal trade-offs between antenna complexity and transmission efficiency.

Beam Collection Efficiency (BCE) Maximization

Beam Collection Efficiency

$$BCE = \frac{\int_{\Omega} |AF(u,v)|^2 dudv}{\int_{\Gamma} |AF(u,v)|^2 dudv}$$

Visible range:
 $\Gamma = \{(u,v) : u^2 + v^2 \leq 1\}$



For **fully-populated array**:

$$AF(u,v) = \sum_{m=1}^M \sum_{n=1}^N w_{m,n} e^{jk(x_n u + y_m v)}$$

$$\text{with: } \begin{cases} w_{m,n} = \alpha_{m,n} e^{j\beta_{m,n}} \\ u = \sin \theta \cos \phi \\ v = \sin \theta \sin \phi \end{cases}$$

$$\text{Steering vector: } \underline{v}(u,v) = [e^{-jk(x_0 u + y_0 v)}, \dots, e^{-jk(x_{N-1} u + y_{M-1} v)}]$$

$$AF(u,v) = \underline{w}^H \underline{v}(u,v) \rightarrow BCE = \frac{\underline{w}^H \underline{A} \underline{w}}{\underline{w}^H \underline{B} \underline{w}}$$

$$\underline{w}^{(opt)} = \arg \left\{ \max_{\underline{w}} [BCE] \right\}$$

BCE measures the capability of the TX array of focusing the power in the angular region where it is the aperture of the RX rectenna

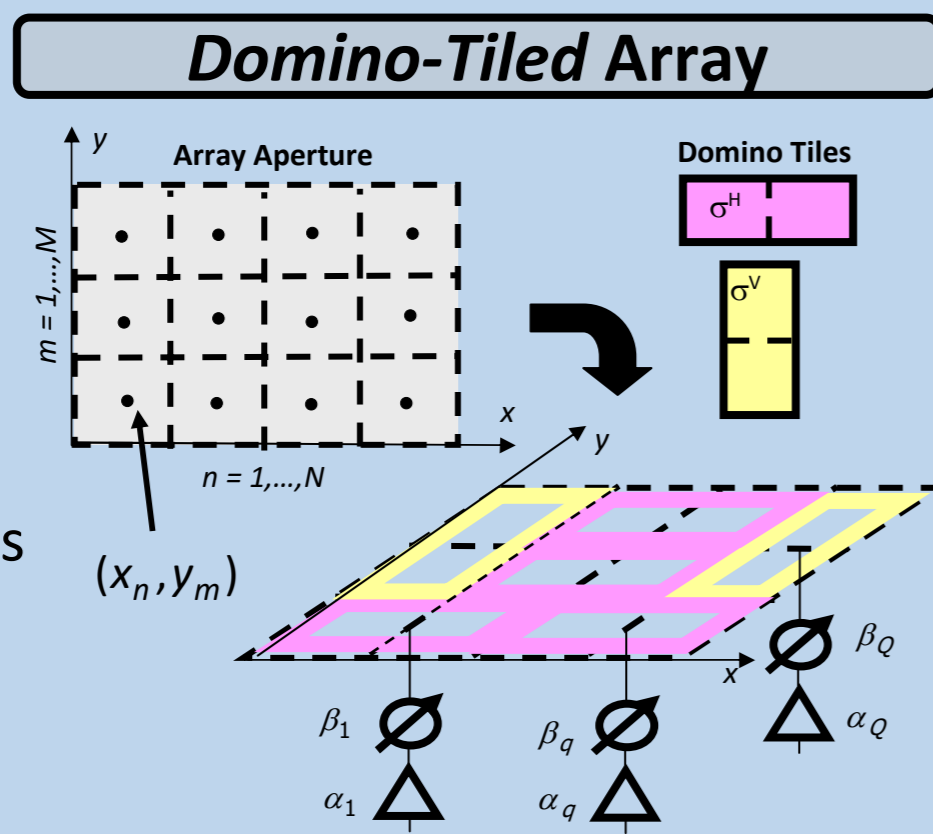
Fully-populated array architectures are very expensive!

How to deal?

Unconventional PA Solution

Problem Statement

Find the optimal tiling/clustering configuration \underline{C}^{opt} and the corresponding sub-array weights, $\underline{\alpha}^{opt}$ and $\underline{\beta}^{opt}$, such that the radiated pattern fits user-requirements, and maximizes the BCE



$$(\underline{C}^{opt}; \underline{\alpha}^{opt}, \underline{\beta}^{opt}) = \arg \left\{ \min_{\underline{C}, \underline{\alpha}, \underline{\beta}} \{ \Psi(\underline{C}; \underline{\alpha}, \underline{\beta}) \} \right\}$$

Questions:

- How to tile the antenna aperture
- How to define the weights $\underline{\alpha}$ and $\underline{\beta}$ for each tile to fit radiated pattern requirements

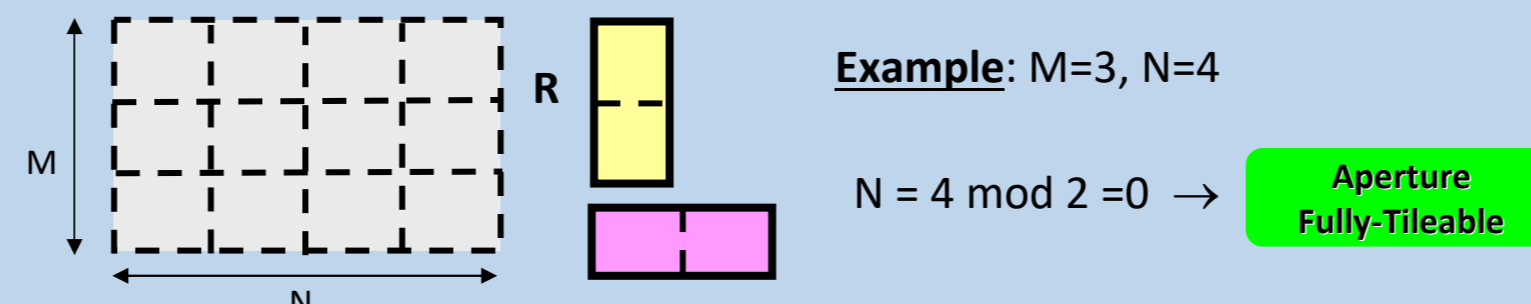
Domino-Tiled Array Synthesis with BCE Maximization

1 Array Aperture Coverage

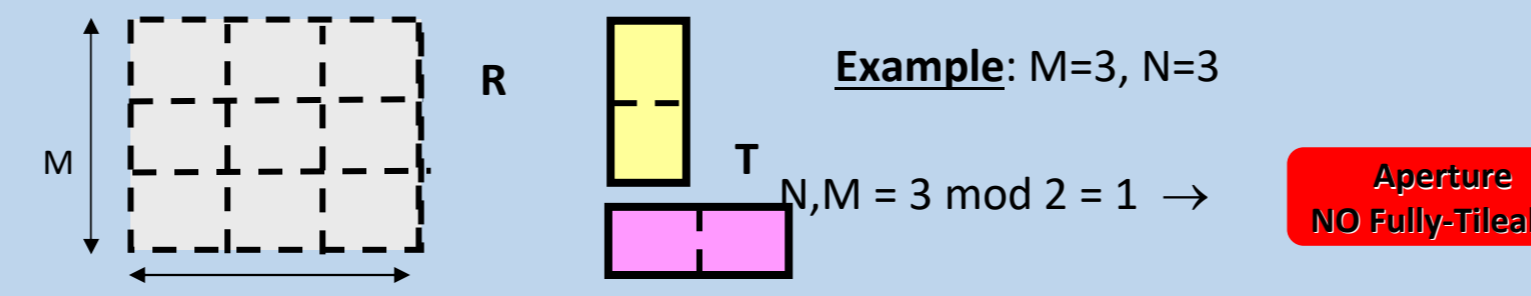
Objective Given a rectangular aperture R of size $M \times N$, **fully cover** it with **domino tiles**

Covering Theorem [1]

- A rectangular aperture R of size $M \times N$ is **fully covered by domino tiles**, if and only if **M or N are even**.



- Otherwise**, the **empty area** extends to a **square pixel**



2 Complete Tiling Configuration

Cardinality Theorem [2]

The **number T of domino-tile configurations** that **fully cover** an array aperture R of dimension $M \times N$ is:

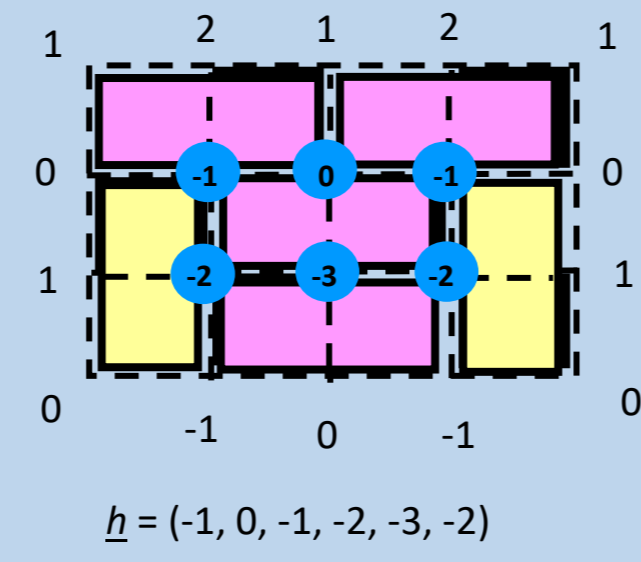
$$T = 2^{\frac{MN}{2}} \prod_{m=1}^M \prod_{n=1}^N \left[\cos^2 \left(\frac{\pi m}{M+1} \right) + \cos^2 \left(\frac{\pi n}{N+1} \right) \right]^{1/4}$$

3 Tiling Coding

Height Function [3]

Definition

- Univocally** define a tiling configuration $\underline{C} \rightarrow \{h_{mn} = h(v_{mn}) \mid v_{mn} \notin \partial \Sigma\}$
- Analytically-defined** on the **lattice vertexes** $h_{mn} = h(v_{mn}) \quad m = 0, \dots, M; \quad n = 0, \dots, N$
- Integer** values function $h_{mn} \in \mathbb{Z}$
- Efficient tiling coding** (h -values internal nodes) $\dim(h) = (M-1) \times (N-1)$ vs. $\dim(\underline{C}) = M \times N$



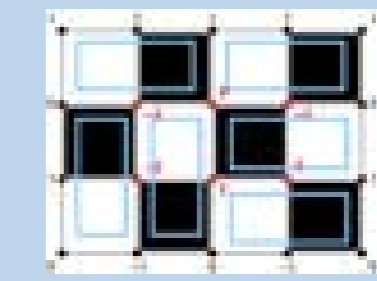
Tiling Wording [4]

Height Function

$$h^{(t)} = \{h_{mn}^{(t)}; \forall v_{mn} \notin \partial A\}$$

$$\tau_l^{(t)} = \frac{h_{mn}^{(t)} - h_{mn}^{(1)}}{4}$$

$$l = m + (n-1) \times (M-1)$$



Tiling Word

$$\tau^{(t)} = \{\tau_l^{(t)}; l = 1, \dots, L\}$$

$$L = (M-1) \times (N-1)$$

4 Optimization Tiling Method

Binary Genetic Algorithm (GA) [6,7]

Objective Choose the best possible complete tiled configuration to fit the requirements

Tiling Word

$$\tau^{(t)} = \{1 \ 1 \ 2 \ 2 \ 1 \ 1\}$$

$$L = (M-1) \times (N-1)$$

Binary Coding

GA Chromosome

$$010101101010101$$

$$B_w = L \times \log_2(w^{\max})$$

$$\tau^{\max} = \max_{l=1, \dots, L} \{\tau_l^{(t)}\}$$

5 Excitation Definition

BCE Maximization

Apply **BCE maximization** to retrieve the best set of reference weights.

$$\underline{w}^{(ref)} = \arg \left\{ \max_{\underline{w}} [BCE] \right\}$$

Compute the **sub-array** optimal set of weights applying:

$$\underline{w}^{(opt)} = \frac{1}{2} \sum_{m=1}^M \sum_{n=1}^N \delta_{C_{nm}, q} \underline{w}_{mn}^{(ref)}$$

The best arrangement is selected by evaluating all the T' tiling configurations ($T' \subset T$ subset of sol. explored by the GA):

$$\underline{C}^{(opt)} = \min_{t=1, \dots, T} \left[\Psi(\underline{C}^{(t)}, \underline{w}^{(opt)}) \right]$$

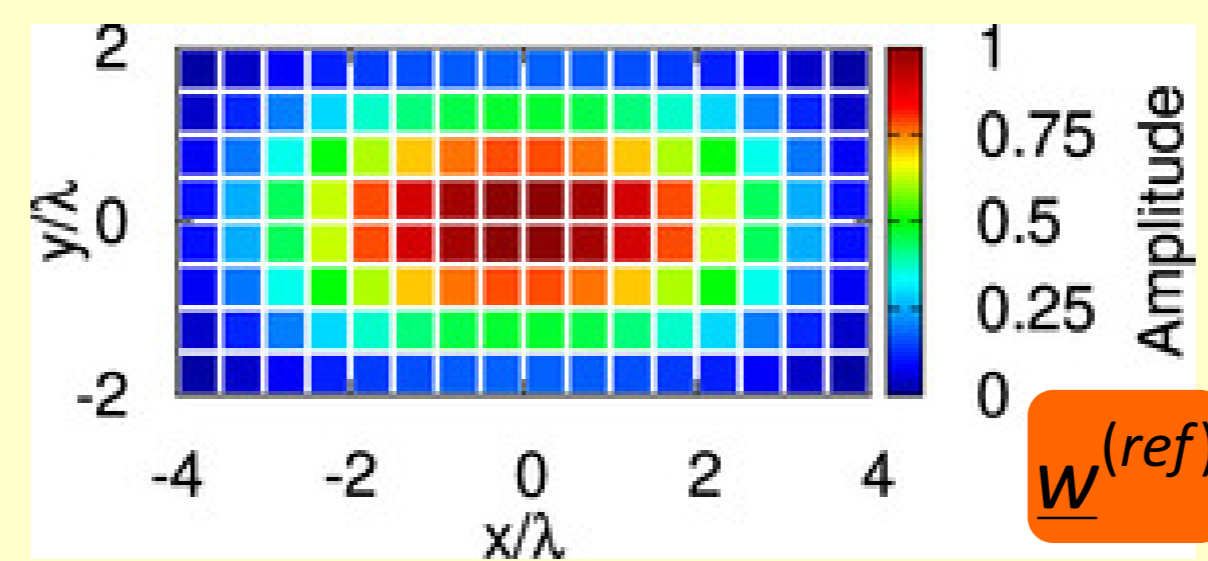
$$\Psi(\underline{C}, \underline{w}) = BCE^{(ref)} - BCE(\underline{C}, \underline{w})$$

Numerical Results

Configuration

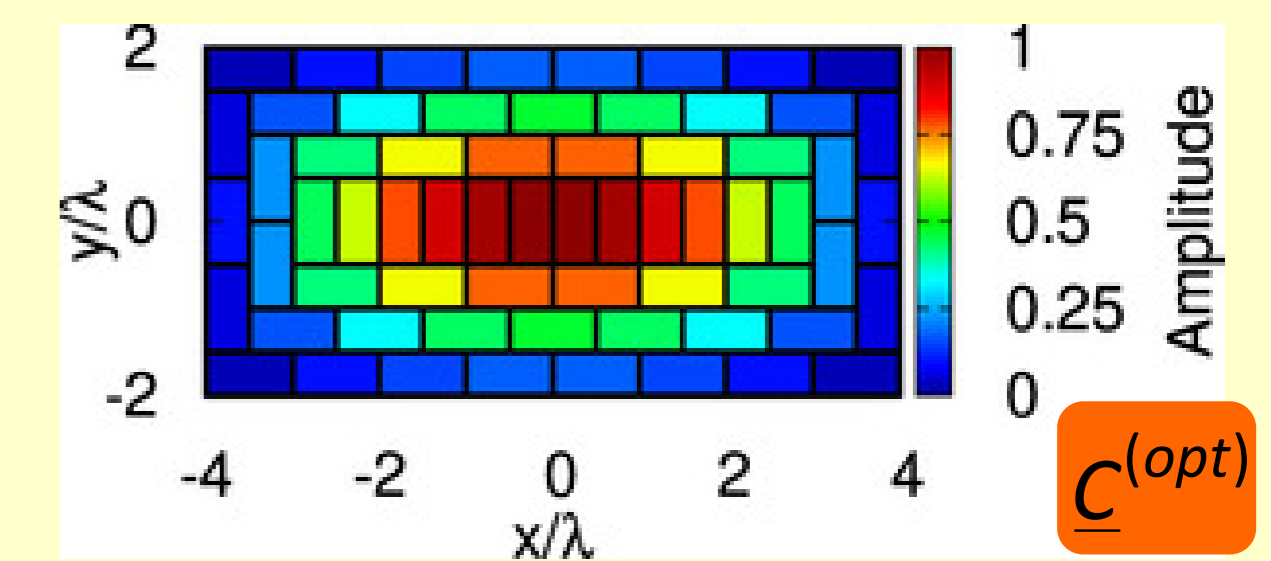
Benchmark Configuration

- $N = 16$
- $M = 8$
- $Q = 64$
- $\theta_s = [0^\circ, 45^\circ]$
- $\phi_s = [0^\circ, 360^\circ]$
- $\Omega = \{u_0 = 0.4; v_0 = 0.4\}$



Reference fully/populated array

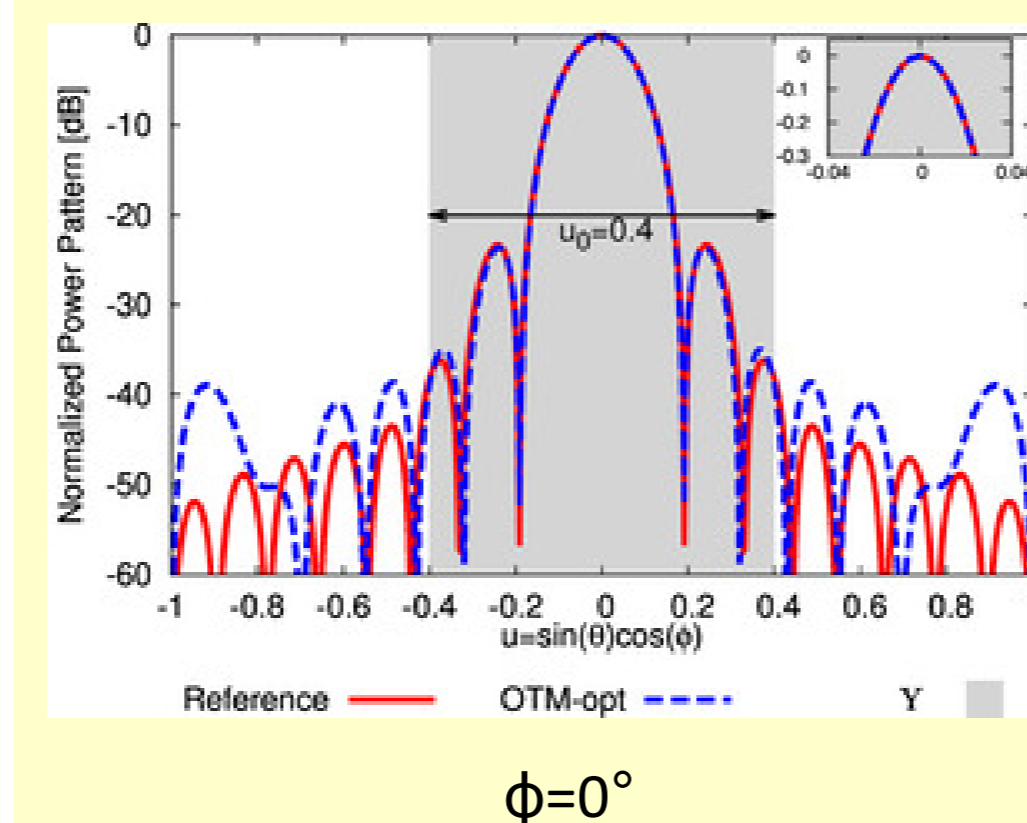
$$BCE^{(ref)} = 99.93\%$$



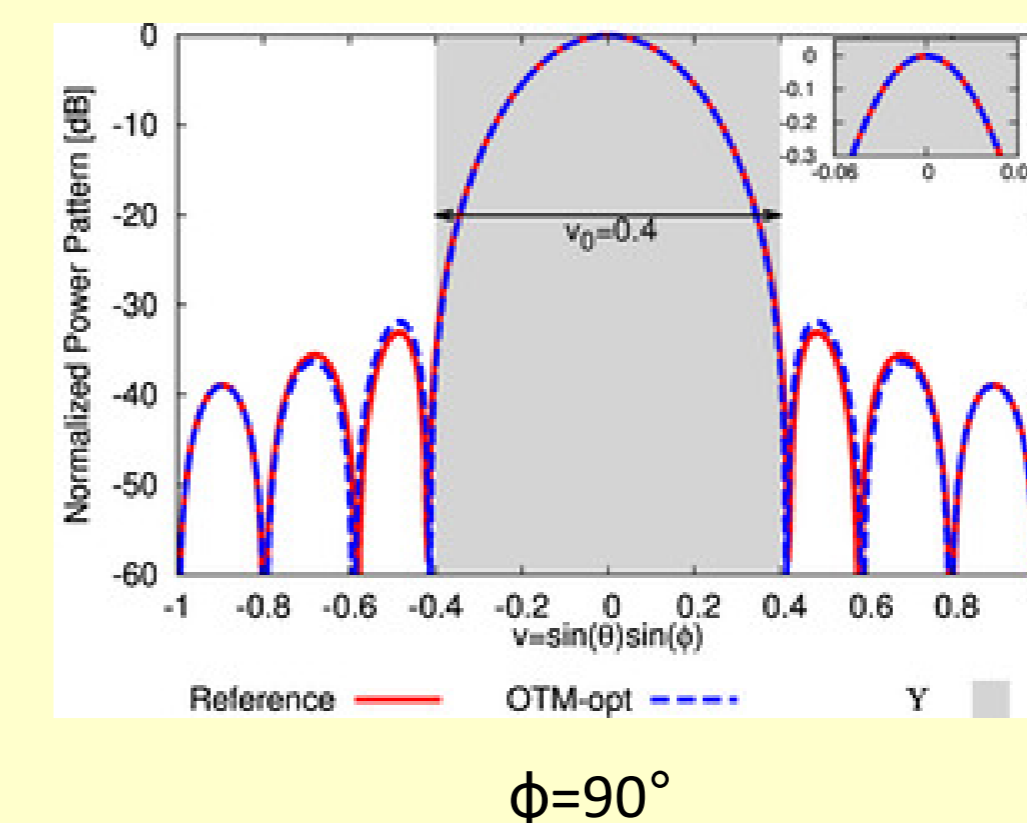
Best tiled array configuration

Control point reduced by 50%!

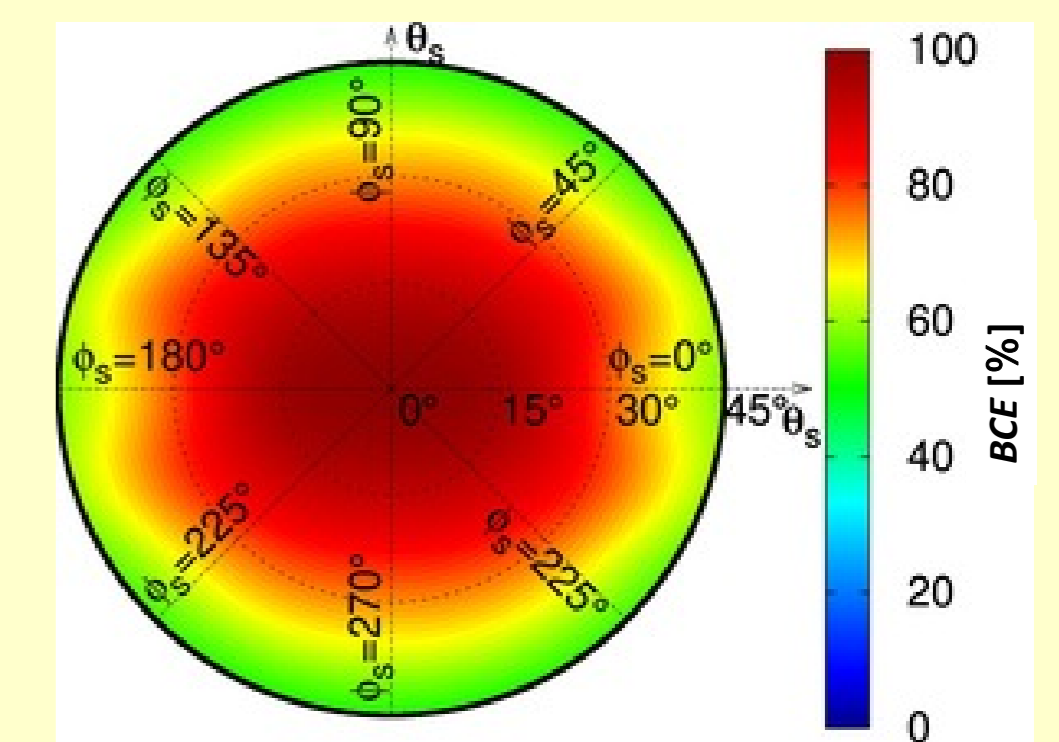
Tiled Array Configuration Results



$\phi = 0^\circ$



$\phi = 90^\circ$



$$\beta_q = -\frac{2\pi}{\lambda} (x_q \sin \theta_s \cos \phi_s + y_q \sin \theta_s \sin \phi_s)$$

$$(x_q) = \sum_{m=1}^M \sum_{n=1}^N \delta_{C_{mq}, a} (x_m)$$

$$(y_q) = \sum_{m=1}^M \sum_{n=1}^N \delta_{C_{mq}, b} (y_m)$$

$BCE^{(opt)} = 99.83\%$
 $\Psi^{(opt)} = 0.1\%$

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