

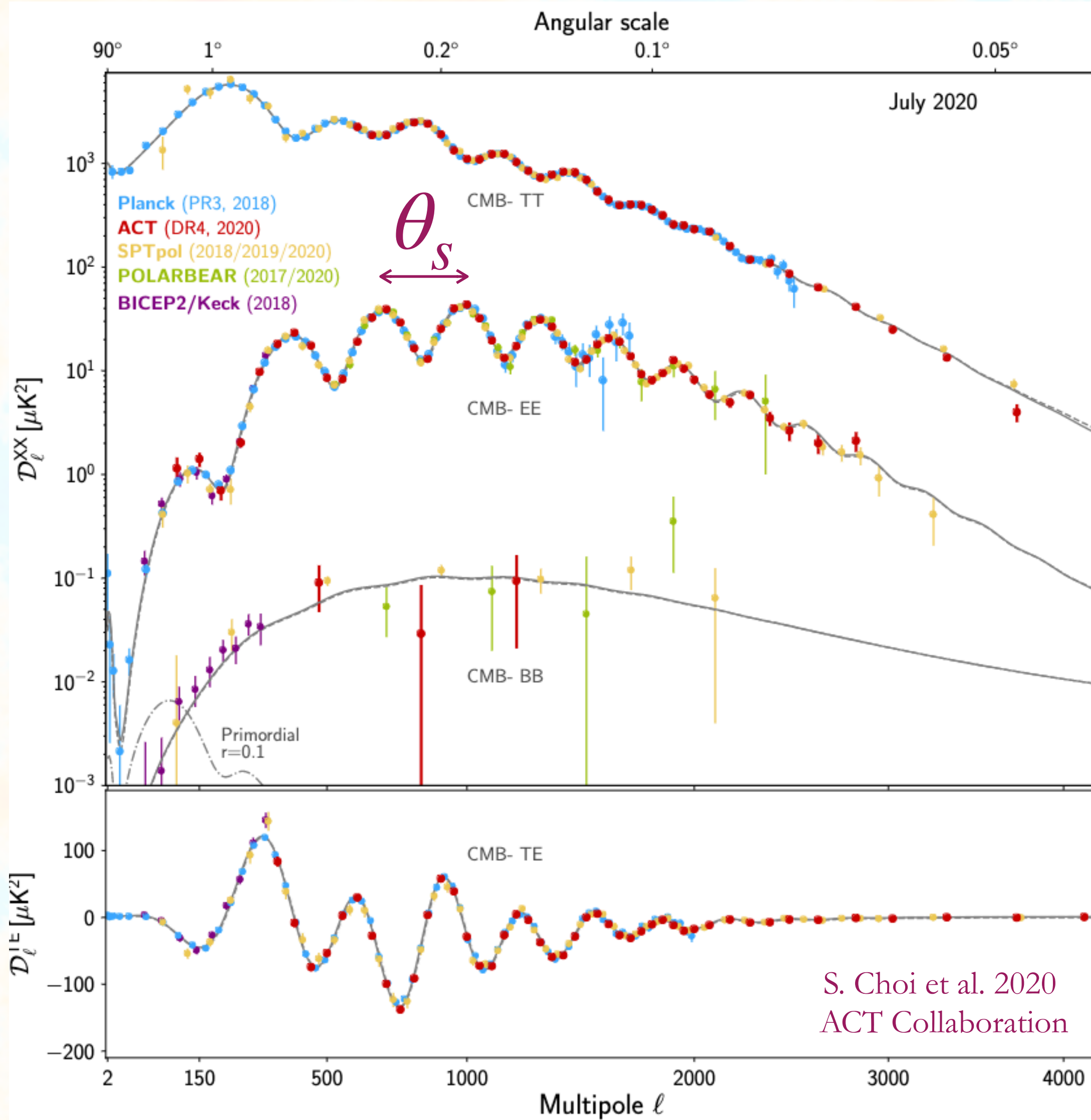
Model-independent Cosmology: summary talk

Rodrigo Calderón

IFPU, Trieste
16/05/2024



Status of Modern Cosmology



Λ CDM : Remarkably accurate description of CMB anisotropies
+ many more

$$\{\theta_s, \omega_c, \omega_b, \tau\}$$

Energy Content

$$\{n_s, A_s\}$$

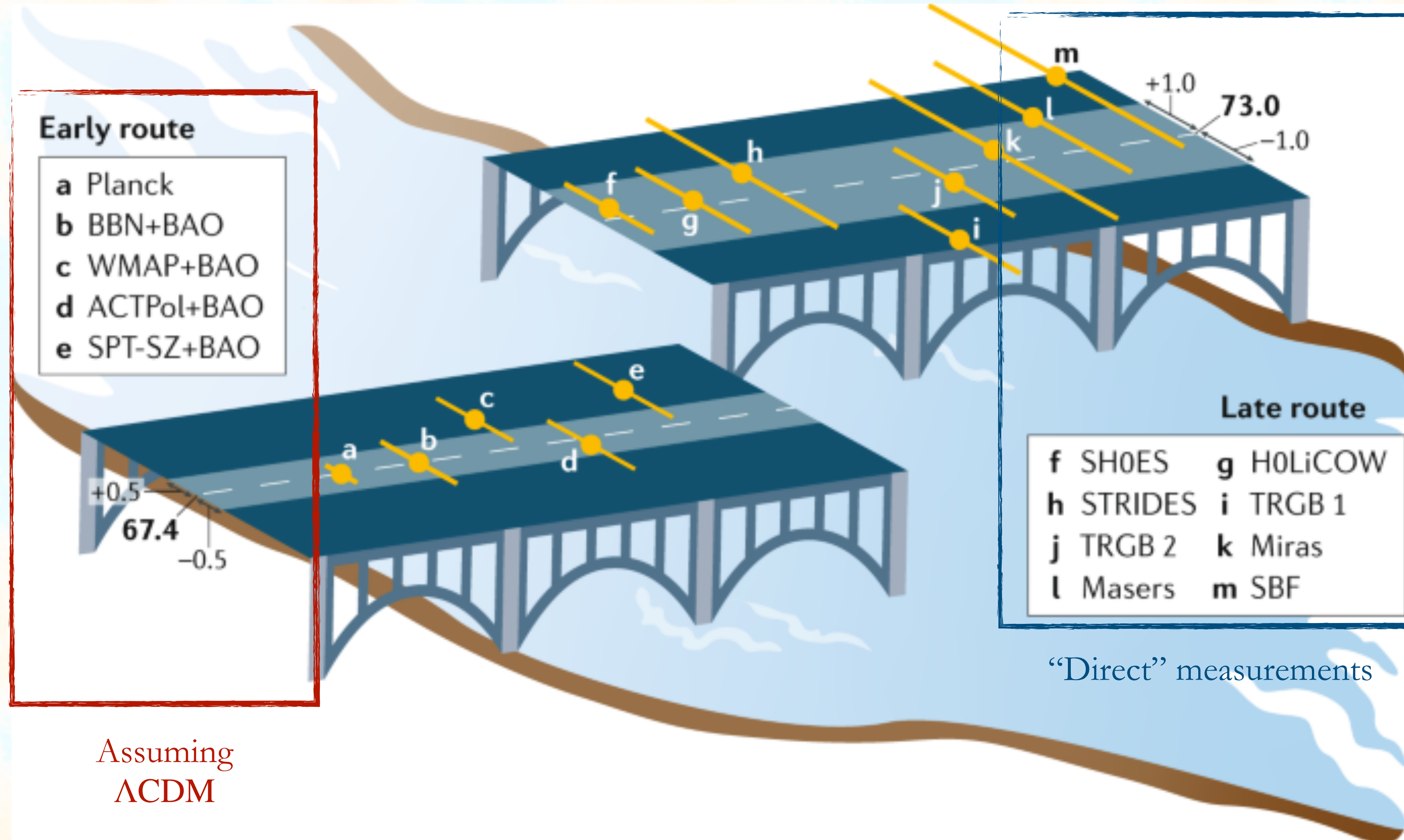
Initial Conditions

Although successful, still **phenomenological**

► Collection of (reasonable) assumptions:

- Flat FLRW : (Isotropy + Homogeneity)
- Gravity = GR
- Dark Energy = Λ
- (Cold) Dark Matter
- Nearly Adiabatic / Scale-invariant fluctuations spectrum

The H_0 tension



Indirect

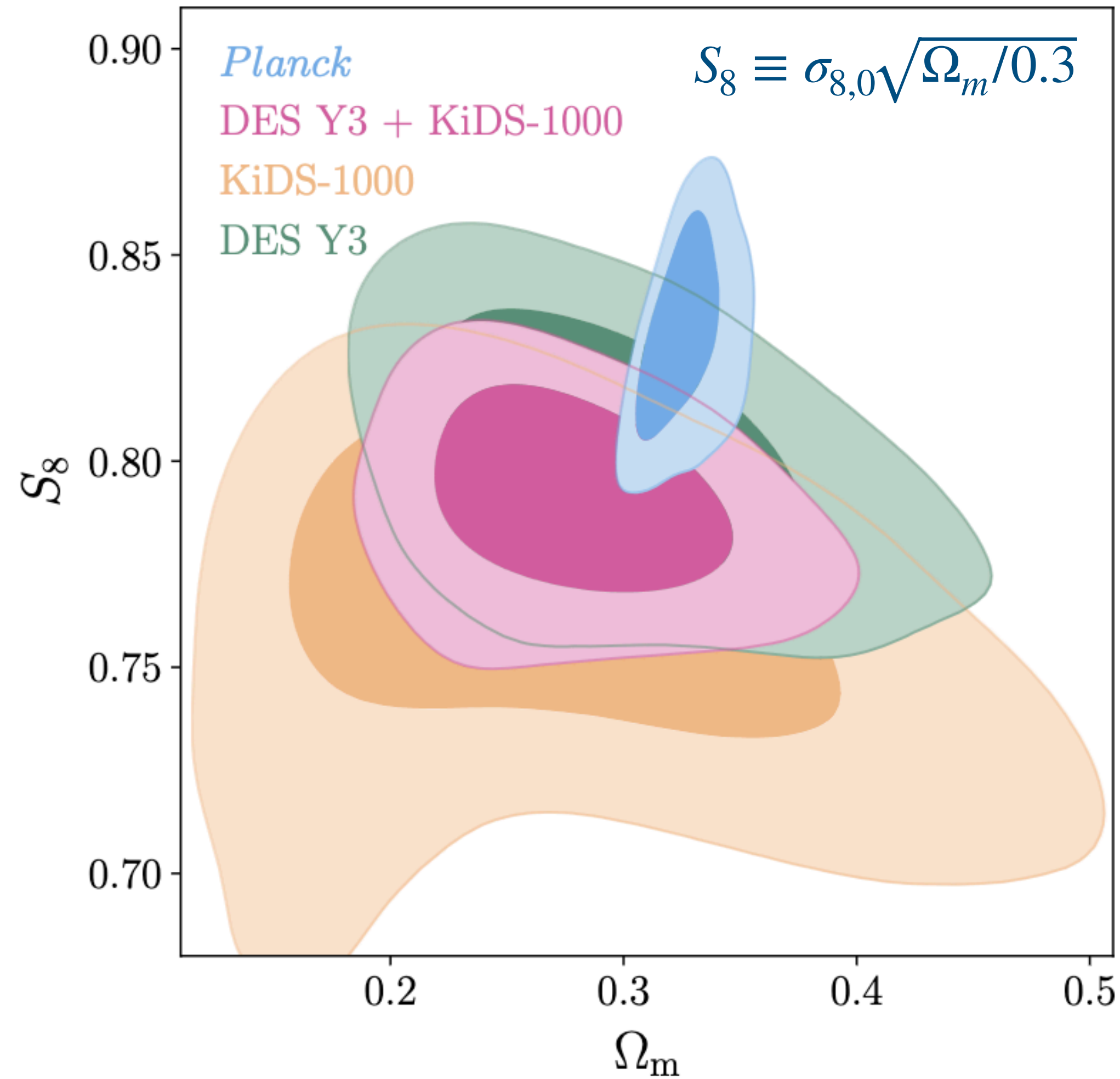
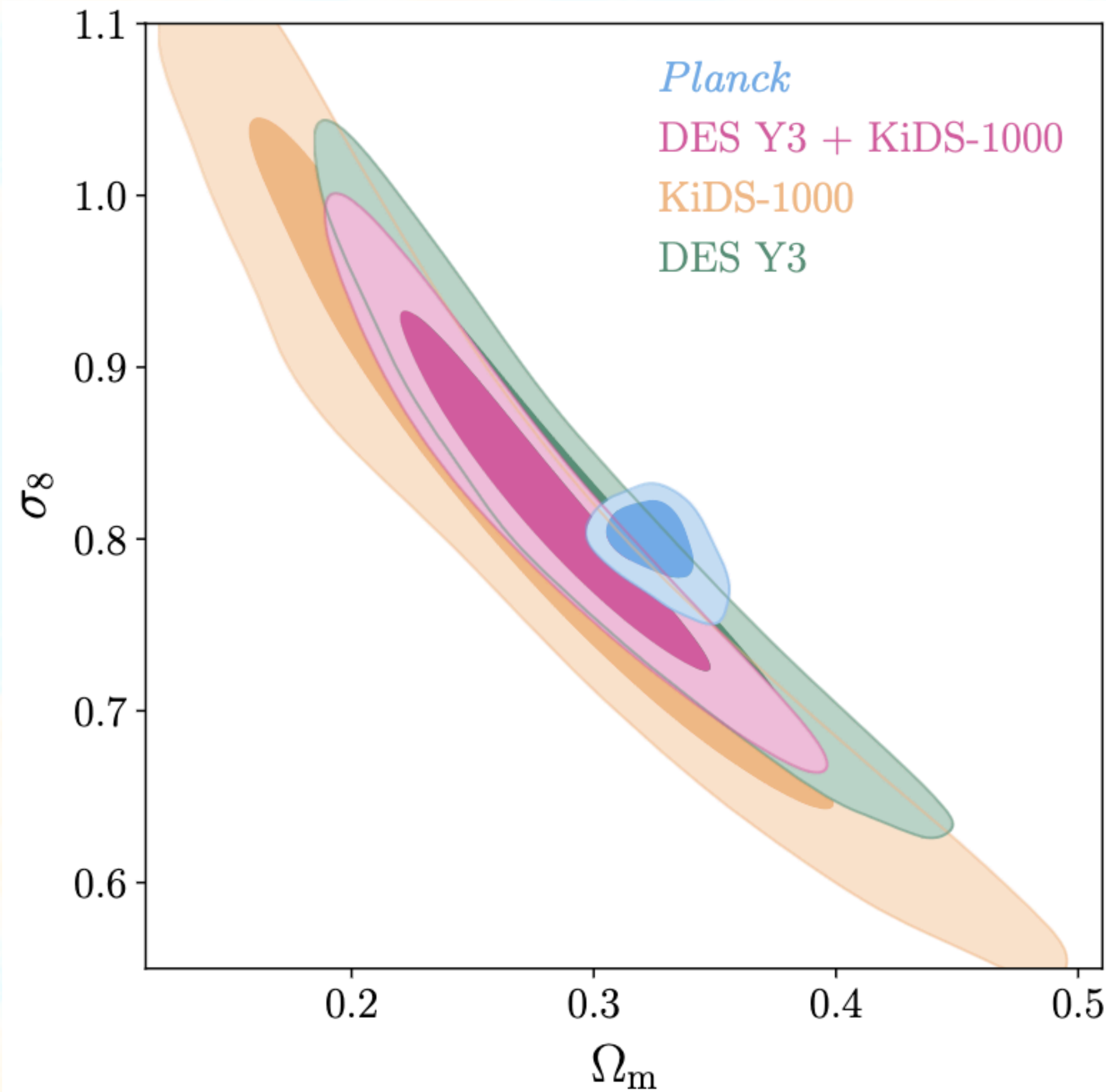
- Model-dependent:
Acoustic scale $\theta_s = \frac{r_s}{d_A}$
- Relies on well-understood (linear) physics

Direct

- Model-independent
- Relies on astrophysics

Riess, Nat. Rev. Phys. 2 (2020) 10

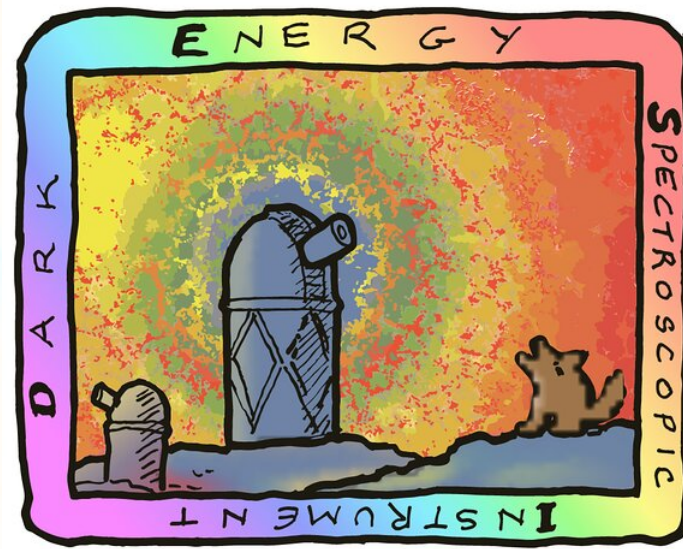
The S_8 anomaly



$\sim 2 - 3\sigma$
Tension/Agreement
with CMB

[DES Y3+KiDS-1000 \[2305.17173\]](#)

Part I: DESI



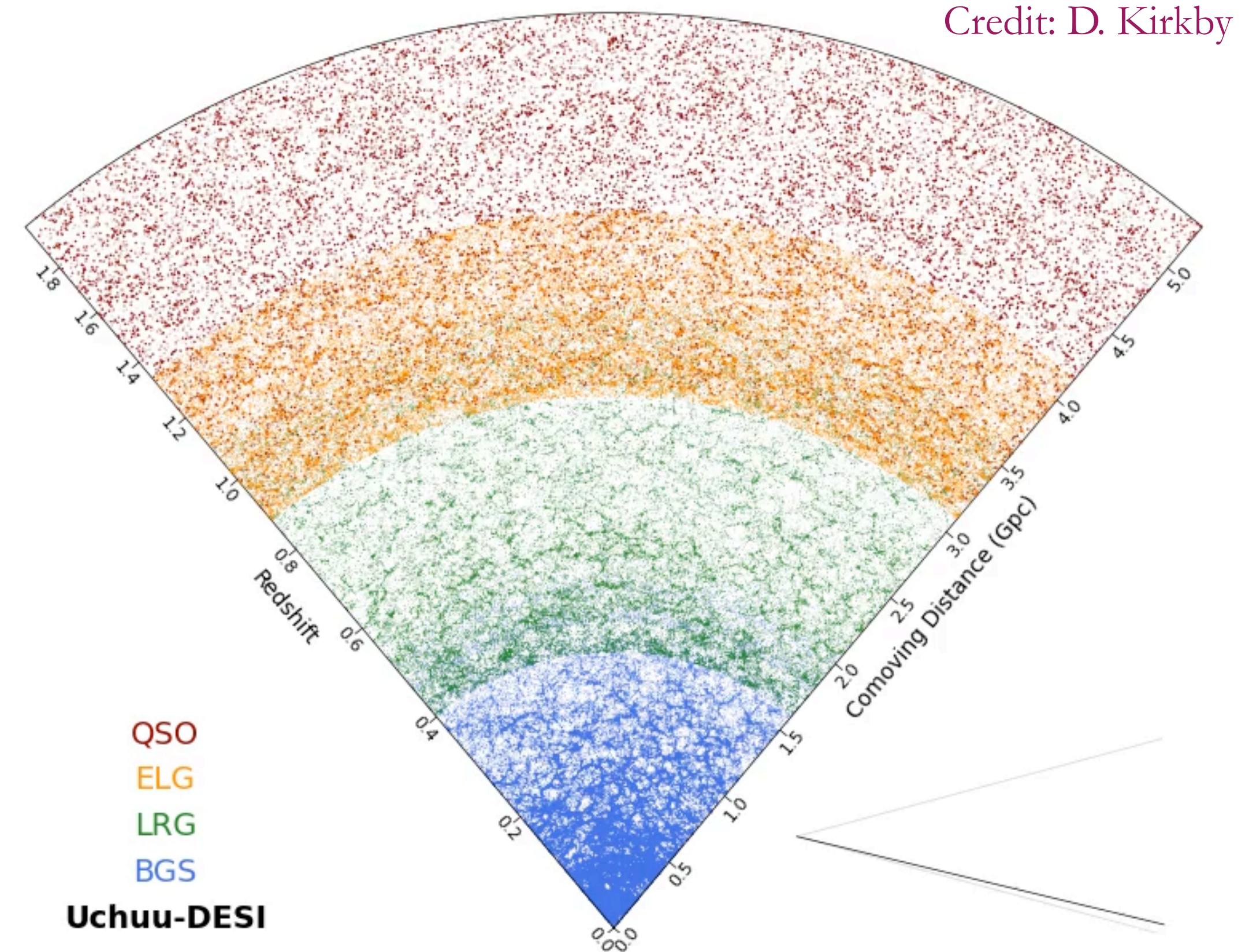
**DARK ENERGY
SPECTROSCOPIC
INSTRUMENT**

U.S. Department of Energy Office of Science

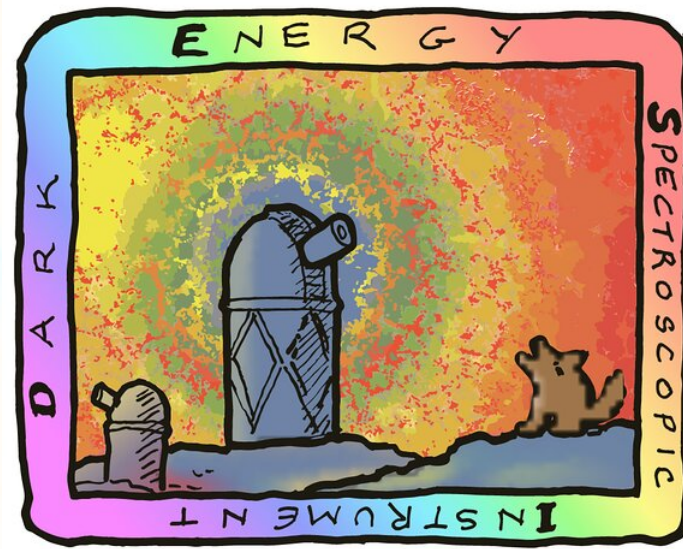


DESI: Mayall 4m Telescope @ Kitt-peak (Arizona)

- 30 Million Galaxies ~ 5000 Spectra with each exposure !
- Accurate z -estimates
- $(z, \phi, \theta) \rightarrow$ Compute n -point statistics
- Derive constraints on your favorite cosmological model !



Part I: DESI



DARK ENERGY SPECTROSCOPIC INSTRUMENT

U.S. Department of Energy Office of Science



DESI: Mayall 4m Telescope @ Kitt-peak (Arizona)

- 30 Million Galaxies ~ 5000 Spectra with each exposure !
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- $(z, \phi, \theta) \rightarrow$ Compute n -point statistics
- Derive constraints on your favorite cosmological model !

Sensitive to new physics in mainly two ways:

Modified Expansion

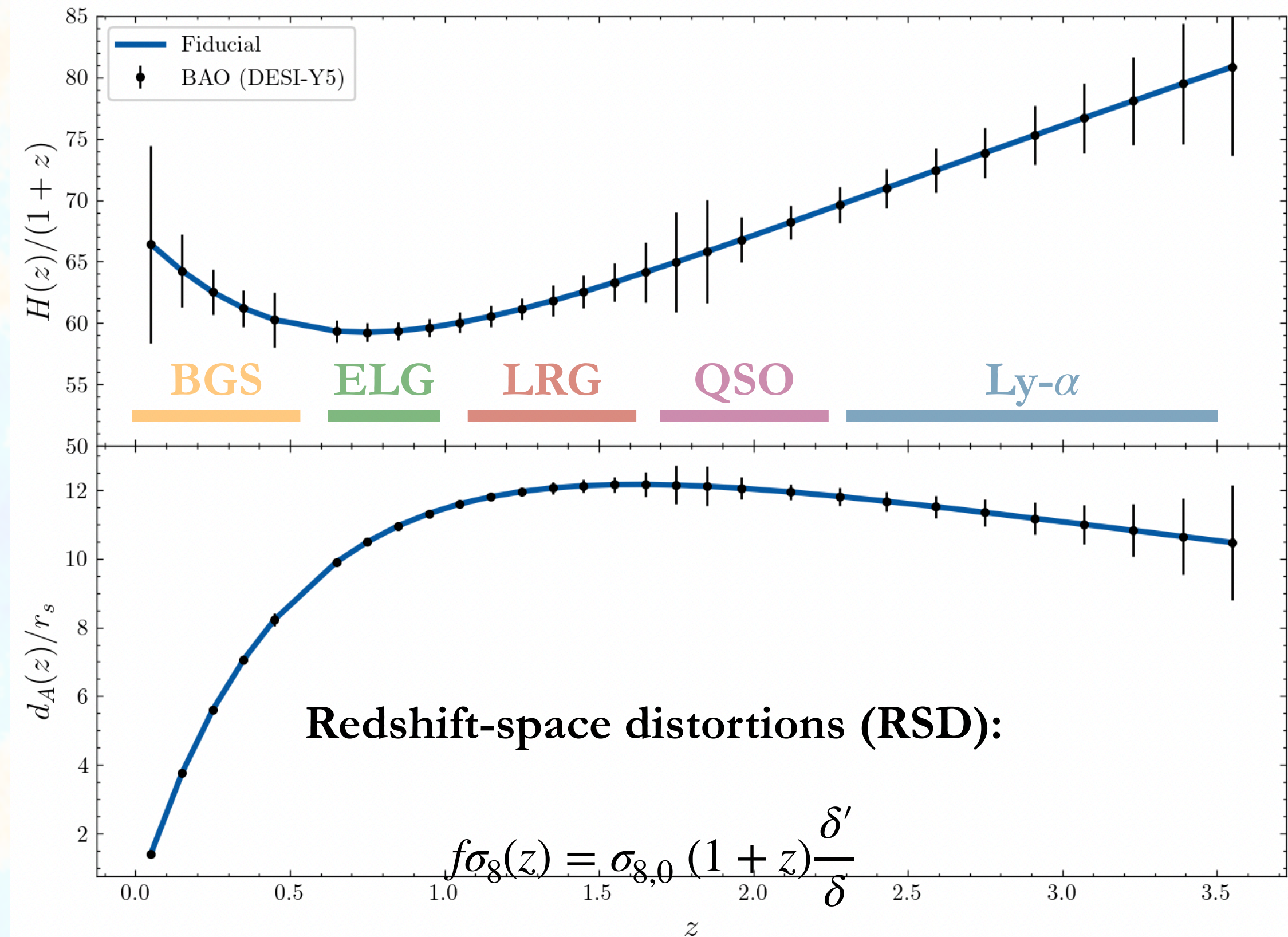
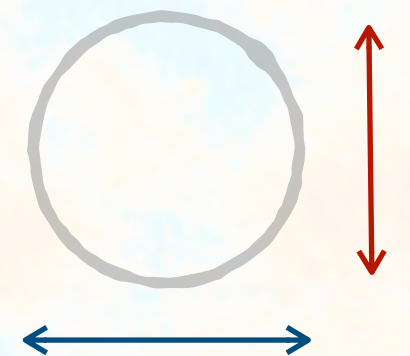
$$\frac{H^2(z)}{H_0^2} = \Omega_m a^{-3} + (1 - \Omega_m)$$

Modified Growth

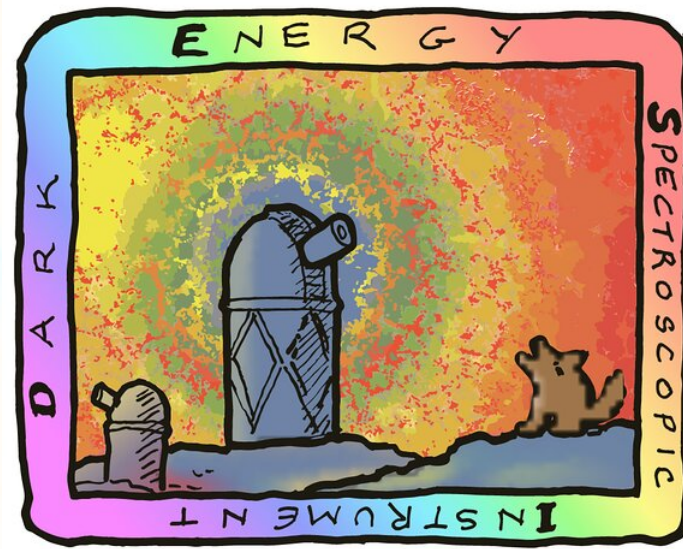
$$f' + \left(f + 2 + \frac{h'}{h} \right) f = \frac{3}{2} \Omega_m(z)$$

Clustering measurements :

- Transversal $d_A(z)/r_s$
- Radial $H(z) r_s$

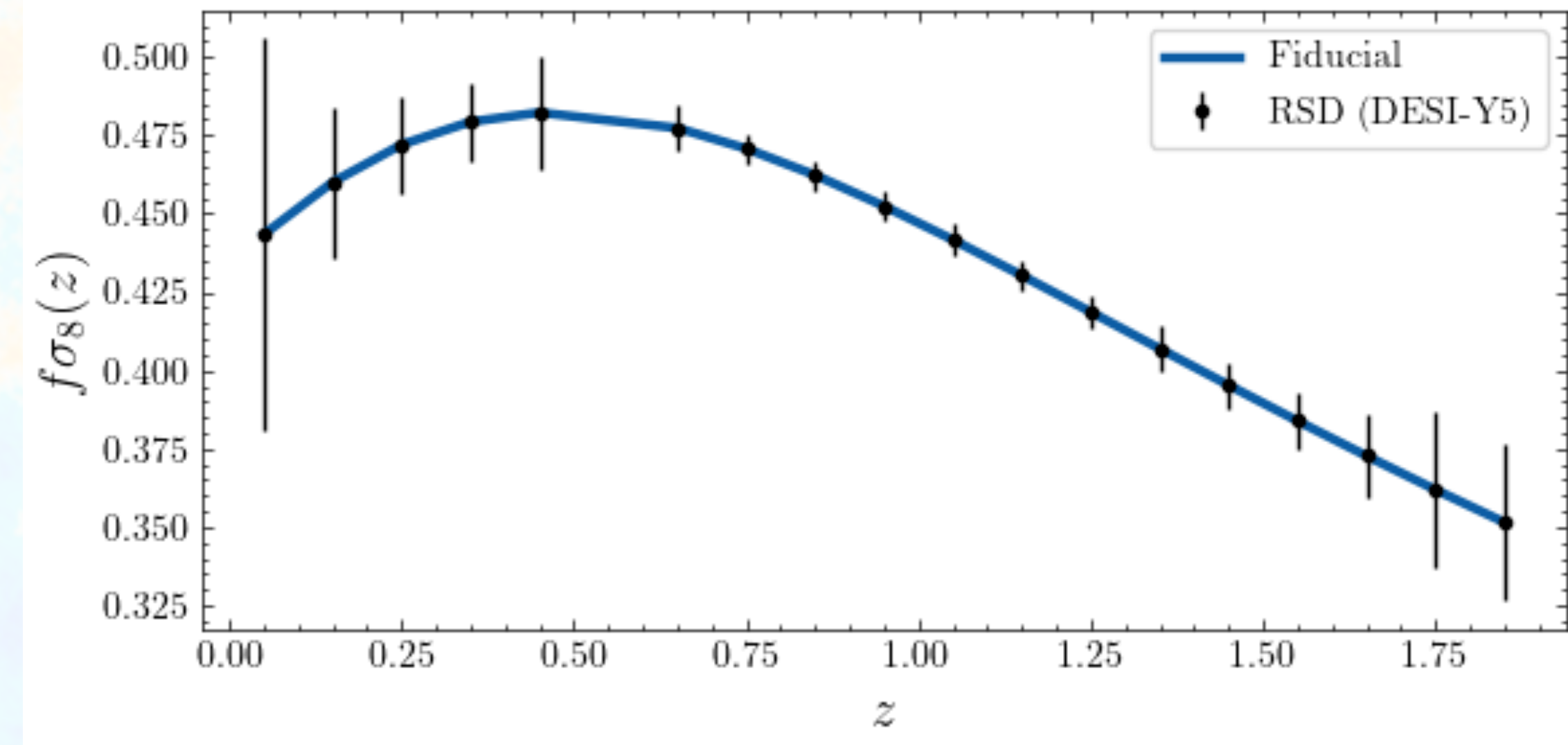


Part I: DESI



**DARK ENERGY
SPECTROSCOPIC
INSTRUMENT**

U.S. Department of Energy Office of Science



DESI: Mayall 4m Telescope @ Kitt-peak (Arizona)

- 30 Million Galaxies ~ 5000 Spectra with each exposure !
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Sensitive to new physics in mainly two ways:

Modified Expansion

$$\frac{H^2(z)}{H_0^2} = \Omega_m a^{-3} + (1 - \Omega_m) f_{DE}(z)$$

Modified Growth

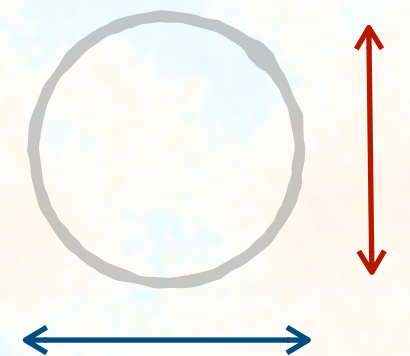
$$f' + \left(f + 2 + \frac{h'}{h} \right) f = \frac{3}{2} \Omega_m(z) \mu(z)$$

Redshift-space distortions (RSD):

$$f\sigma_8(z) = \sigma_{8,0} (1+z) \frac{\delta'}{\delta}$$

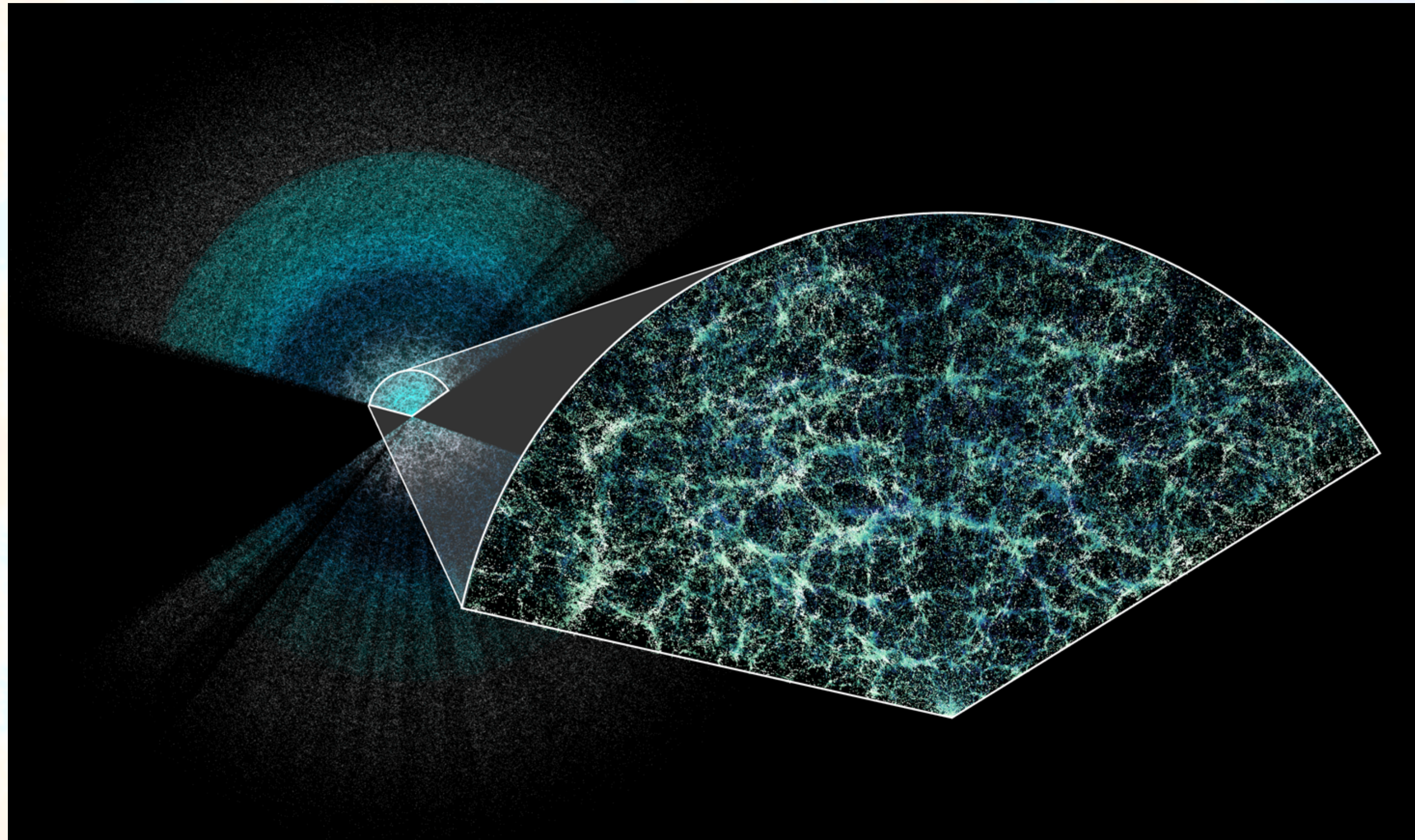
Clustering measurements :

- Transversal $d_A(z)/r_s$
- Radial $H(z) r_s$

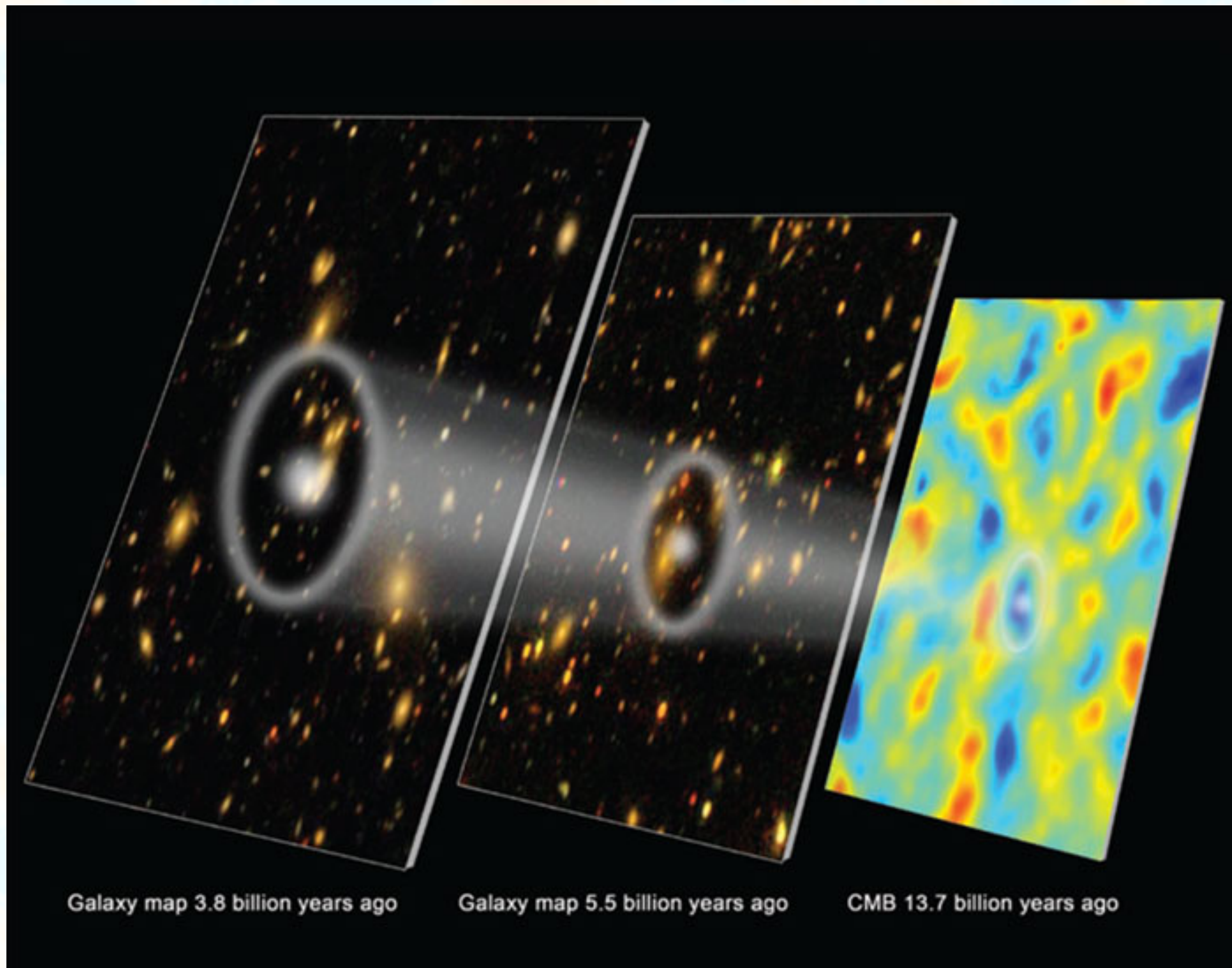


Part II: Baryon Acoustic Oscillations

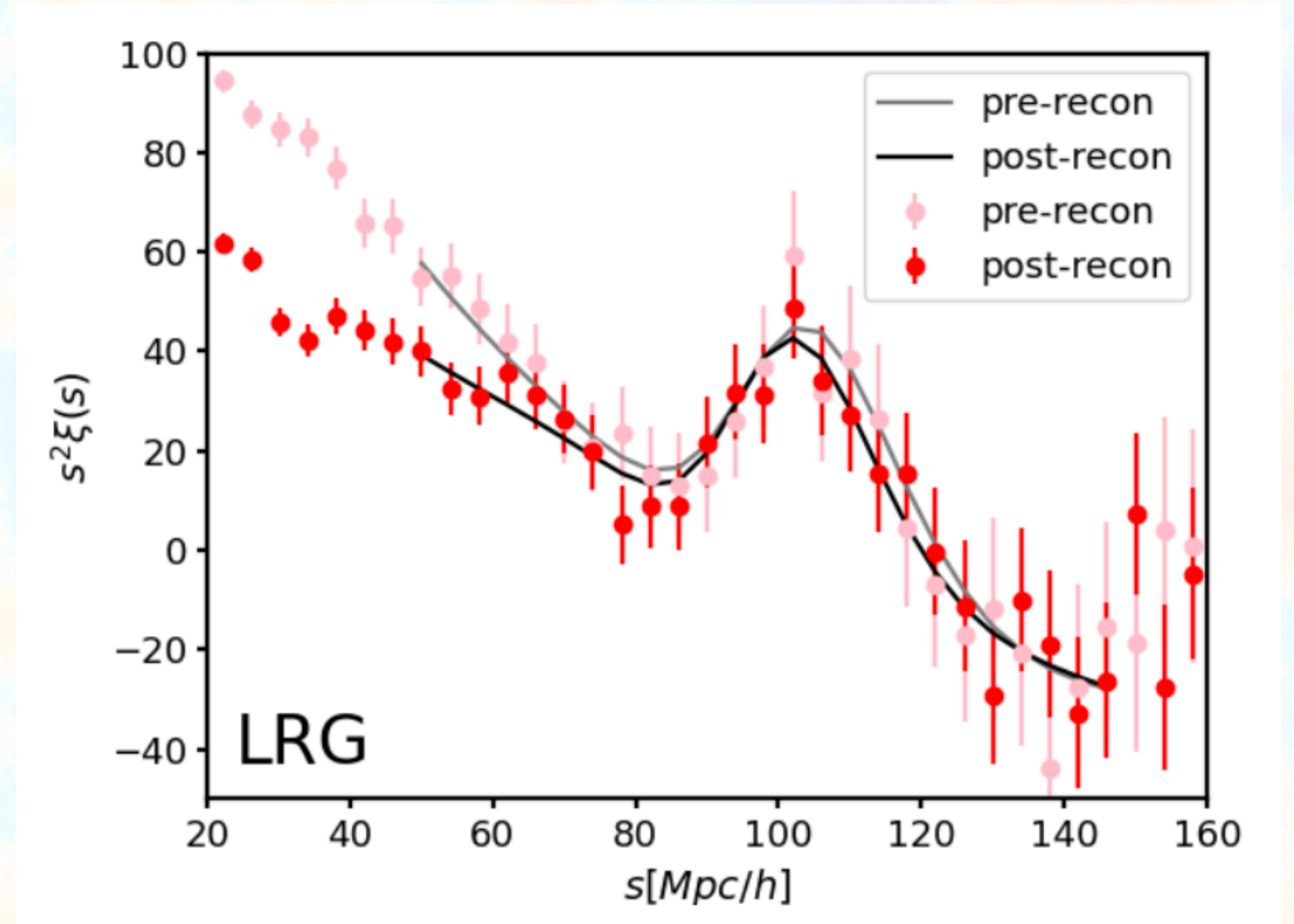
From the distribution of galaxies & quasars, to cosmological constraints



Baryon Acoustic Oscillations

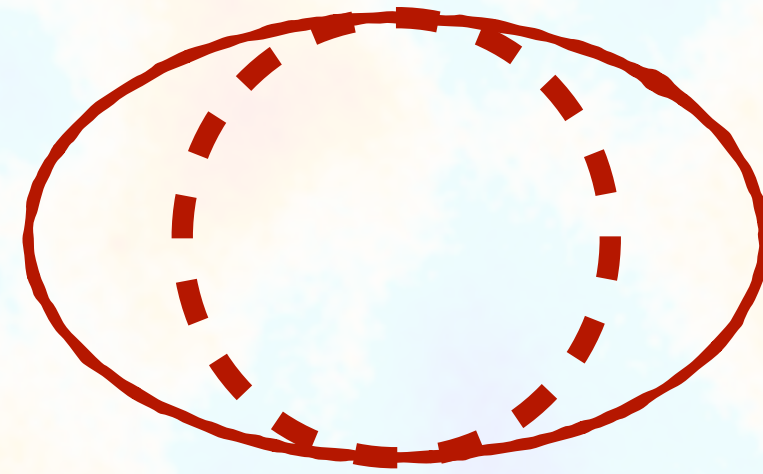


Credit: E. M. Huff & SPT team



J. Moon et al. (2023) - First Detection of the BAO Signal from Early DESI Data

“Compressed Parameters”



Transverse direction

“Alcock-Paczyński”
Parameters



Line of sight direction

$$\frac{D_M}{r_d} = \alpha_{\perp} \frac{D_M^{\text{fid}}}{r_d^{\text{fid}}}$$

$$D_M(z) \propto \int \frac{dz}{H(z)}$$

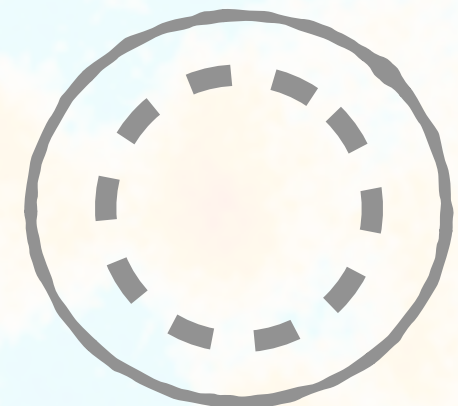
$$\frac{D_H}{r_d} = \alpha_{\parallel} \frac{D_H^{\text{fid}}}{r_d^{\text{fid}}}$$

$$D_H(z) \propto \frac{1}{H(z)}$$

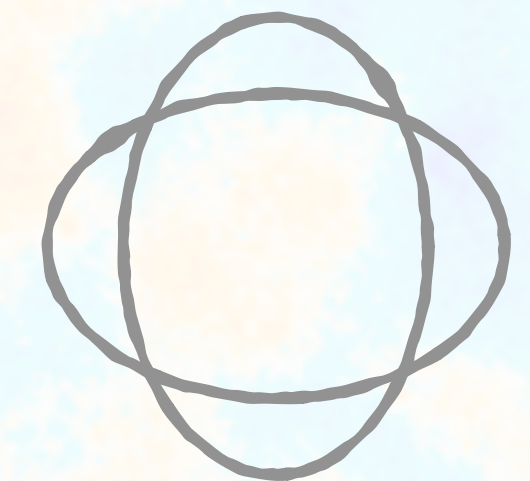
Alternatively,

$$\alpha_{\text{iso}} = (\alpha_{\perp}^2 \alpha_{\parallel})^{1/3}$$

$$\alpha_{\text{AP}} = \frac{\alpha_{\parallel}}{\alpha_{\perp}} = \frac{D_H D_M^{\text{fid}}}{D_M D_H^{\text{fid}}}$$

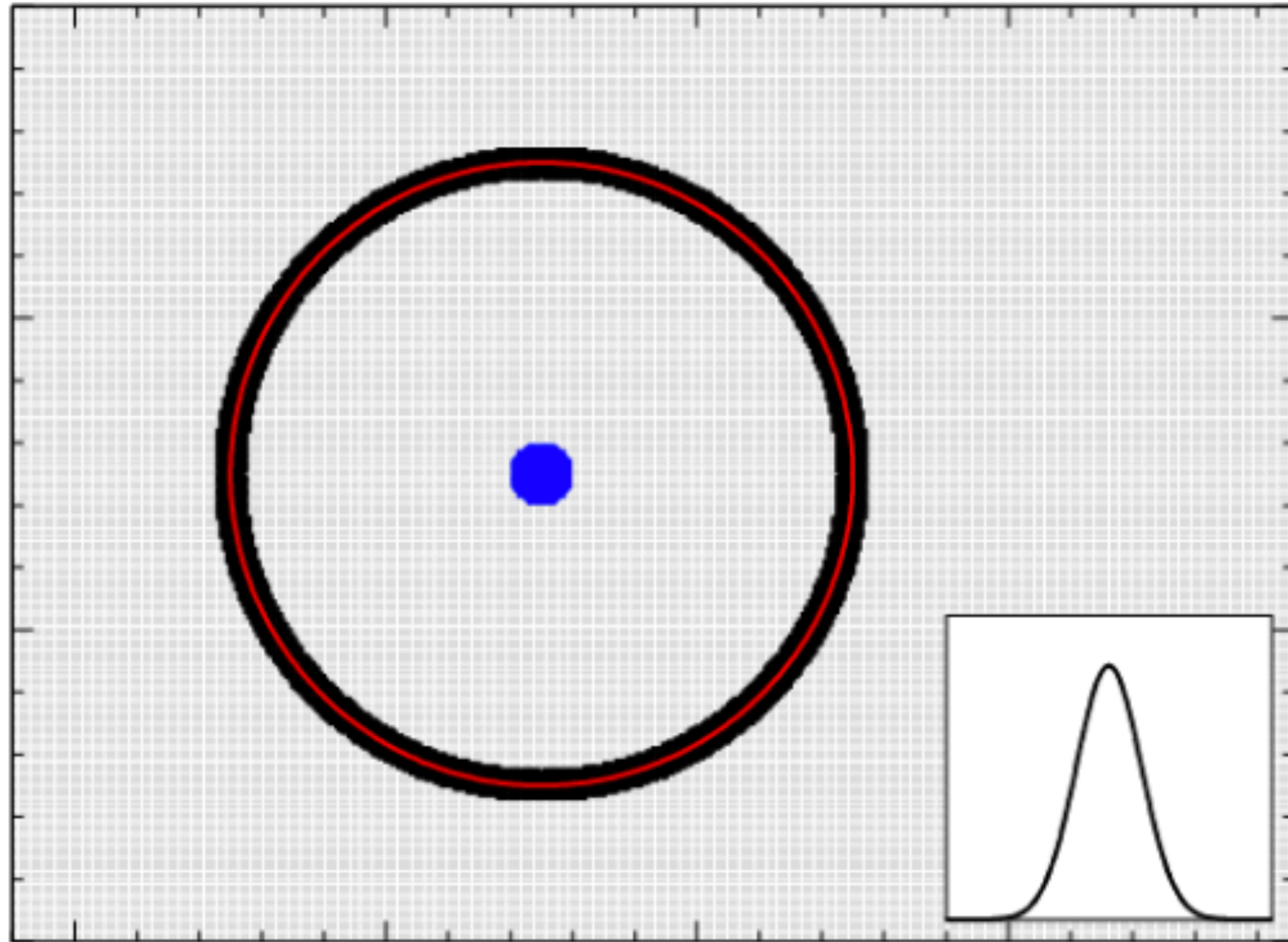


Isotropic scaling
of the BAO



Anisotropy
of the BAO

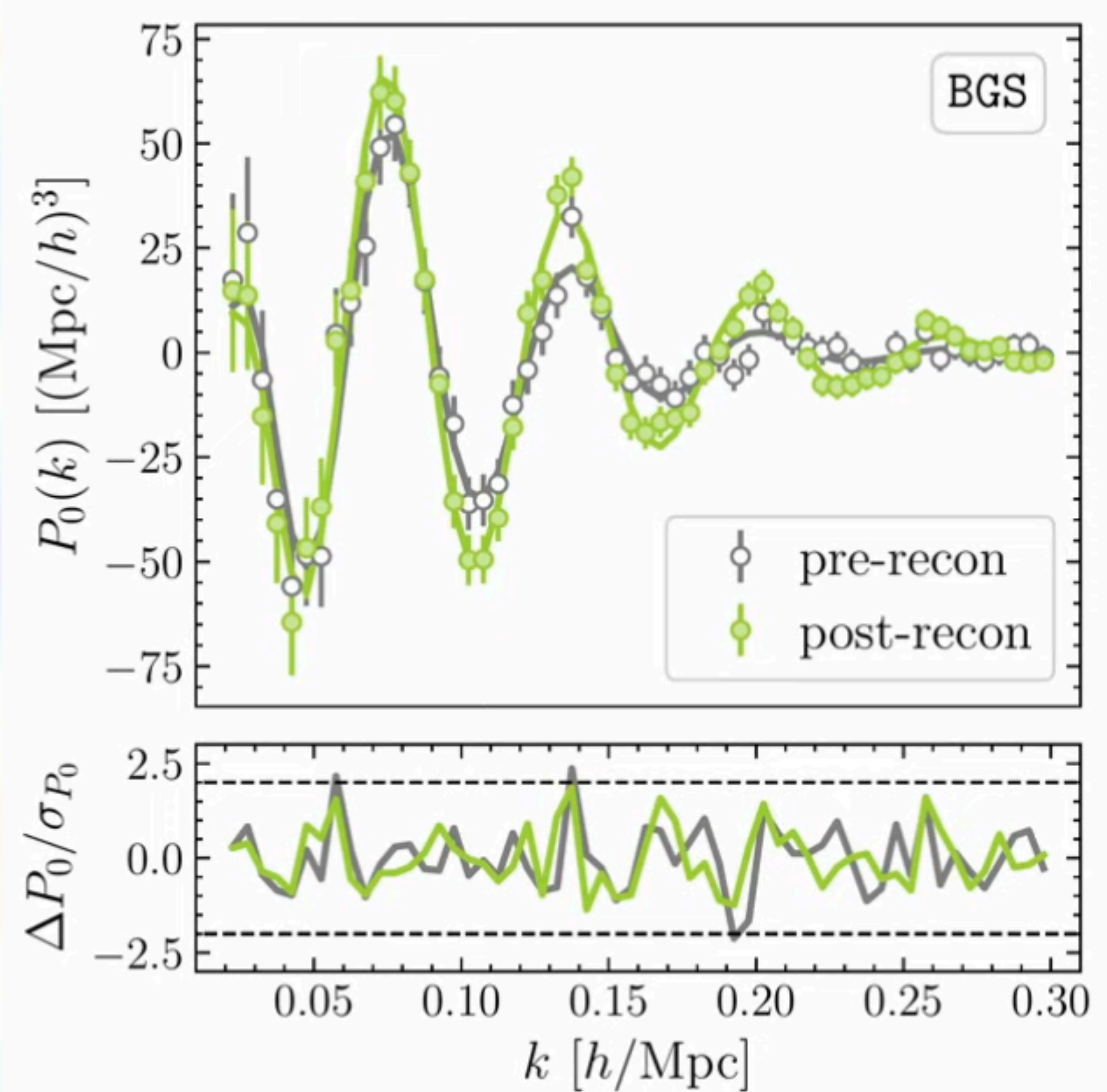
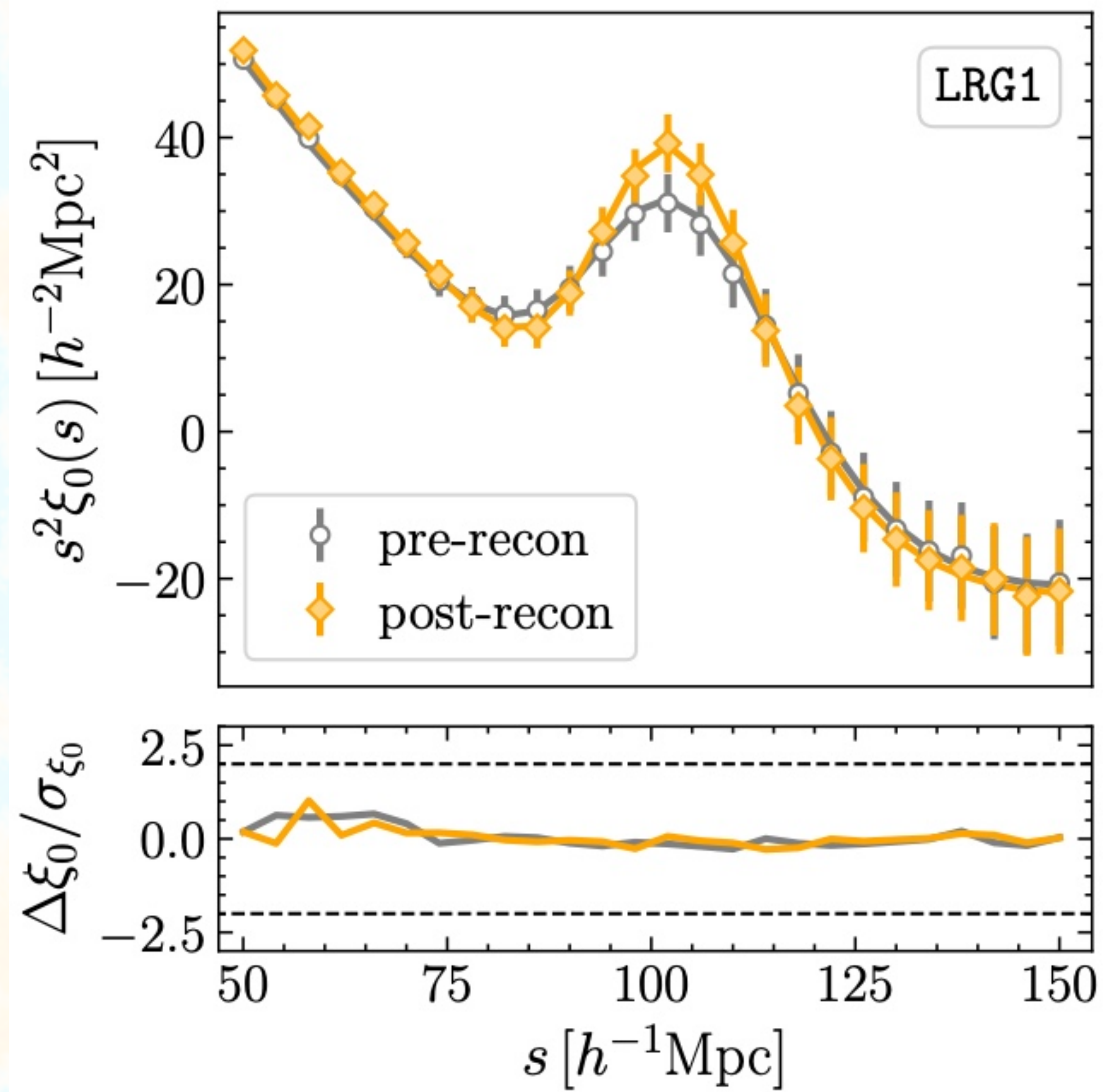
Baryon Acoustic Oscillations



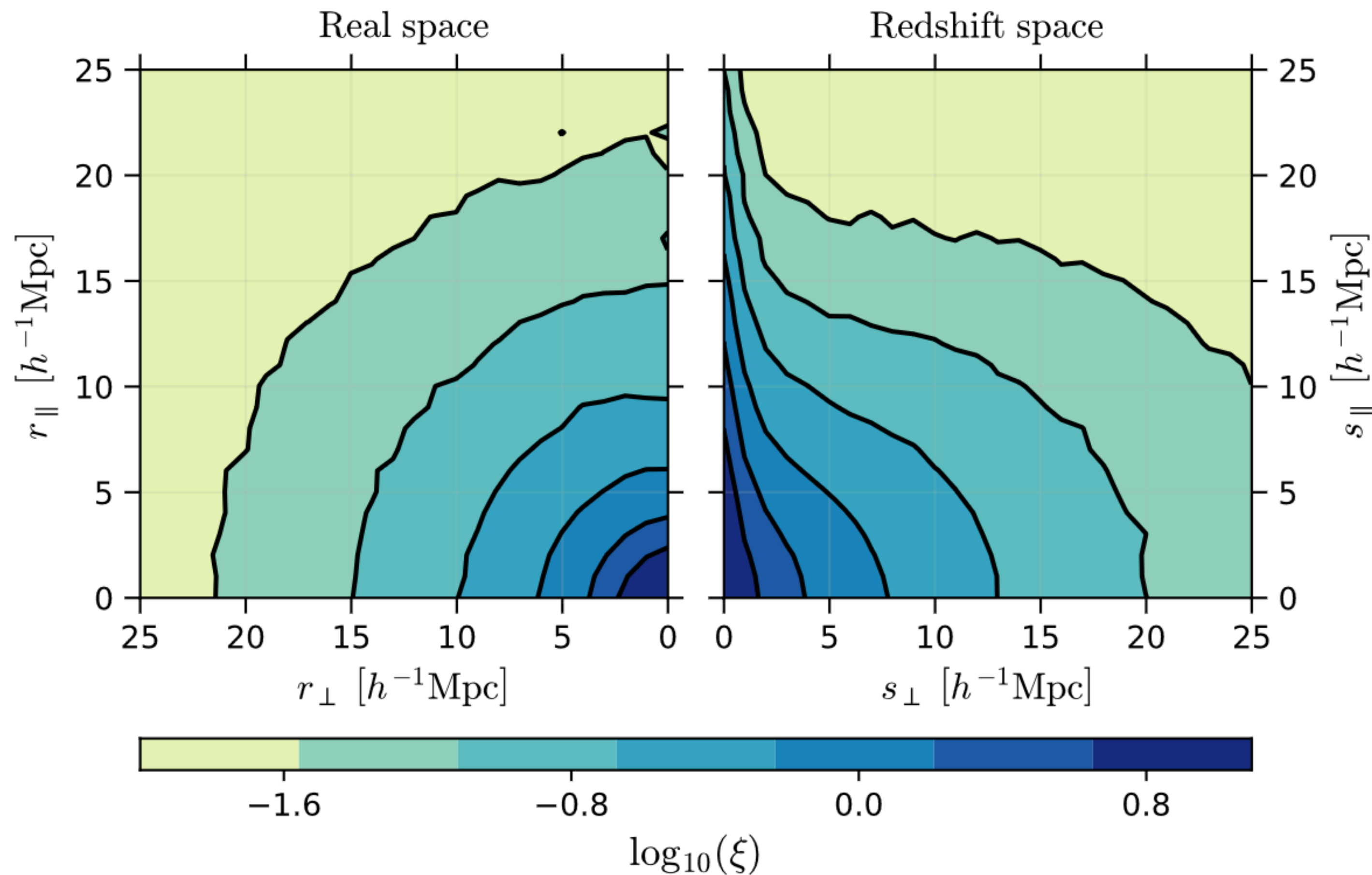
Padmanabhan et al. (2012) MNRAS

- The BAO feature is expected to be **isotropic** !
- Non-linear **gravitational evolution** introduce **anisotropies** along longitudinal/transversal directions
 - Broadening of the BAO peak in 2pt correlation function
- By reconstructing the velocity field, we can “**undo**” the effect of gravity/non-linearities.
 - Increase significance of the detection !

Pre vs post-reconstruction

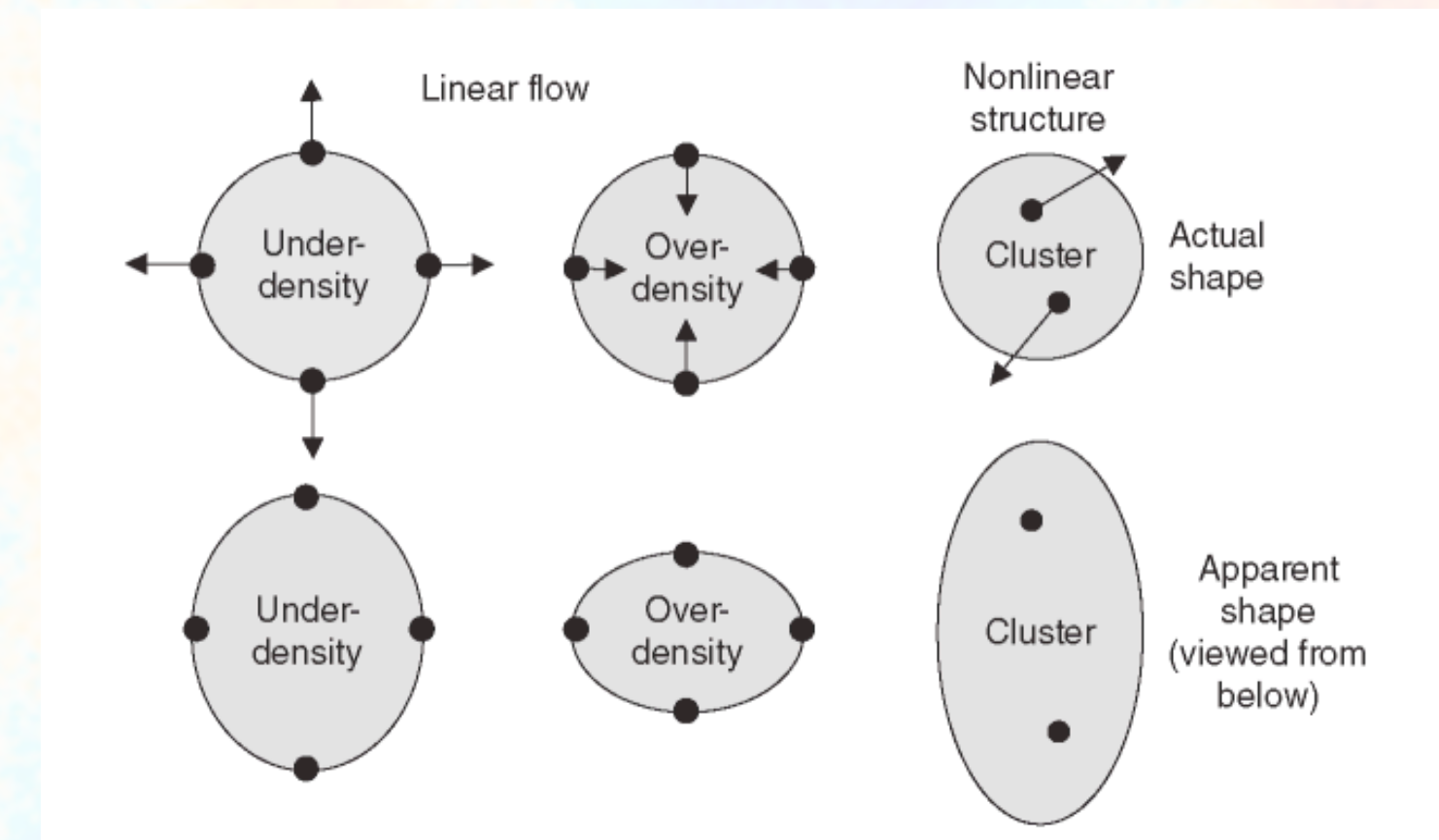


Redshift Space Distortions



J. Kuruvilla, C. Porciani - MNRAS (2018)

- Observations are done in **redshift-space**



- Introduce additional **anisotropies** in 2PCF

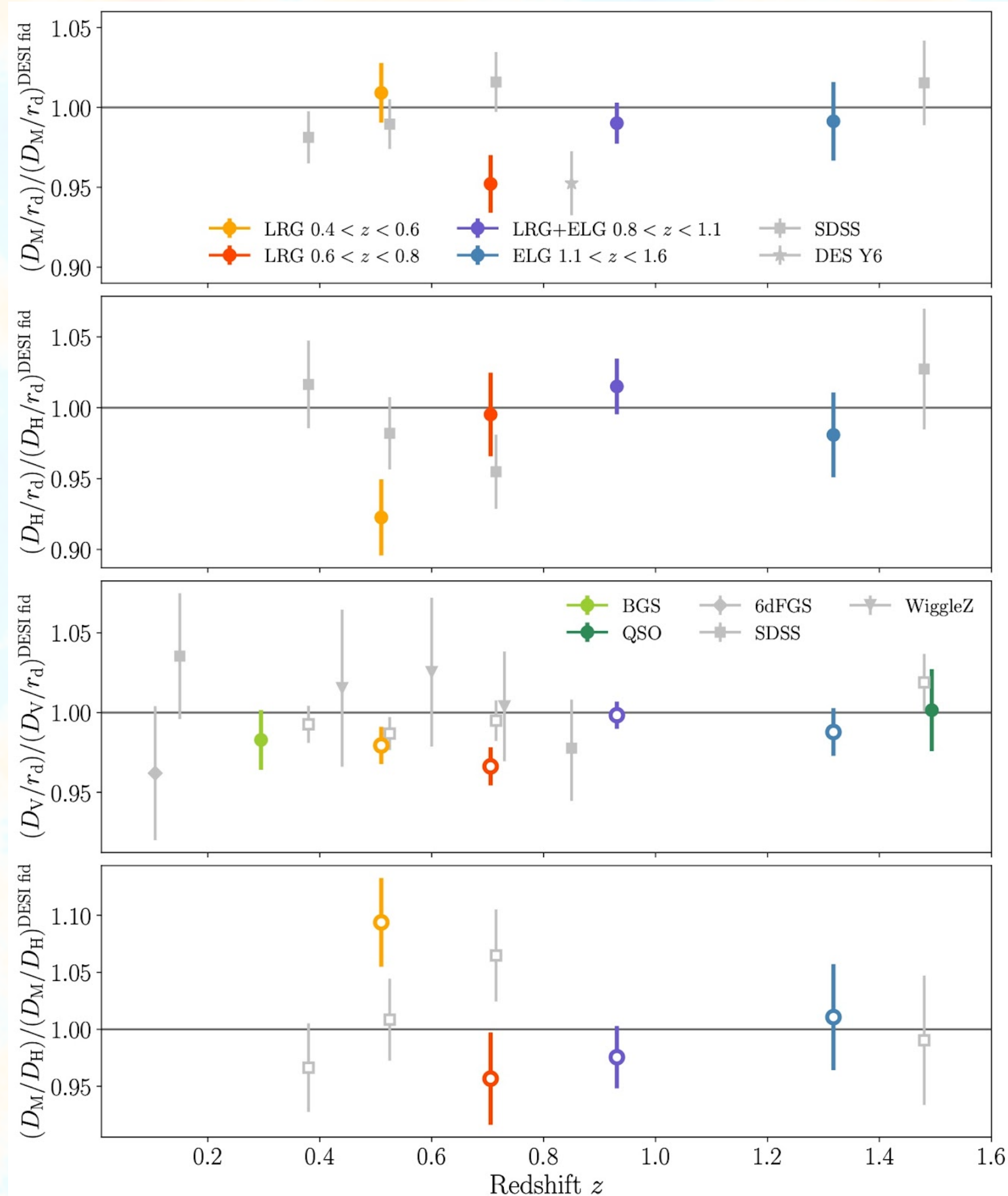
→ Large-scales: “Kaiser” effect

→ Small-scales : “Finger-of-god” effect

- Can be used a probe of gravity !

→ Measurements of growth: $f\sigma_8(z)$

DESI vs SDSS



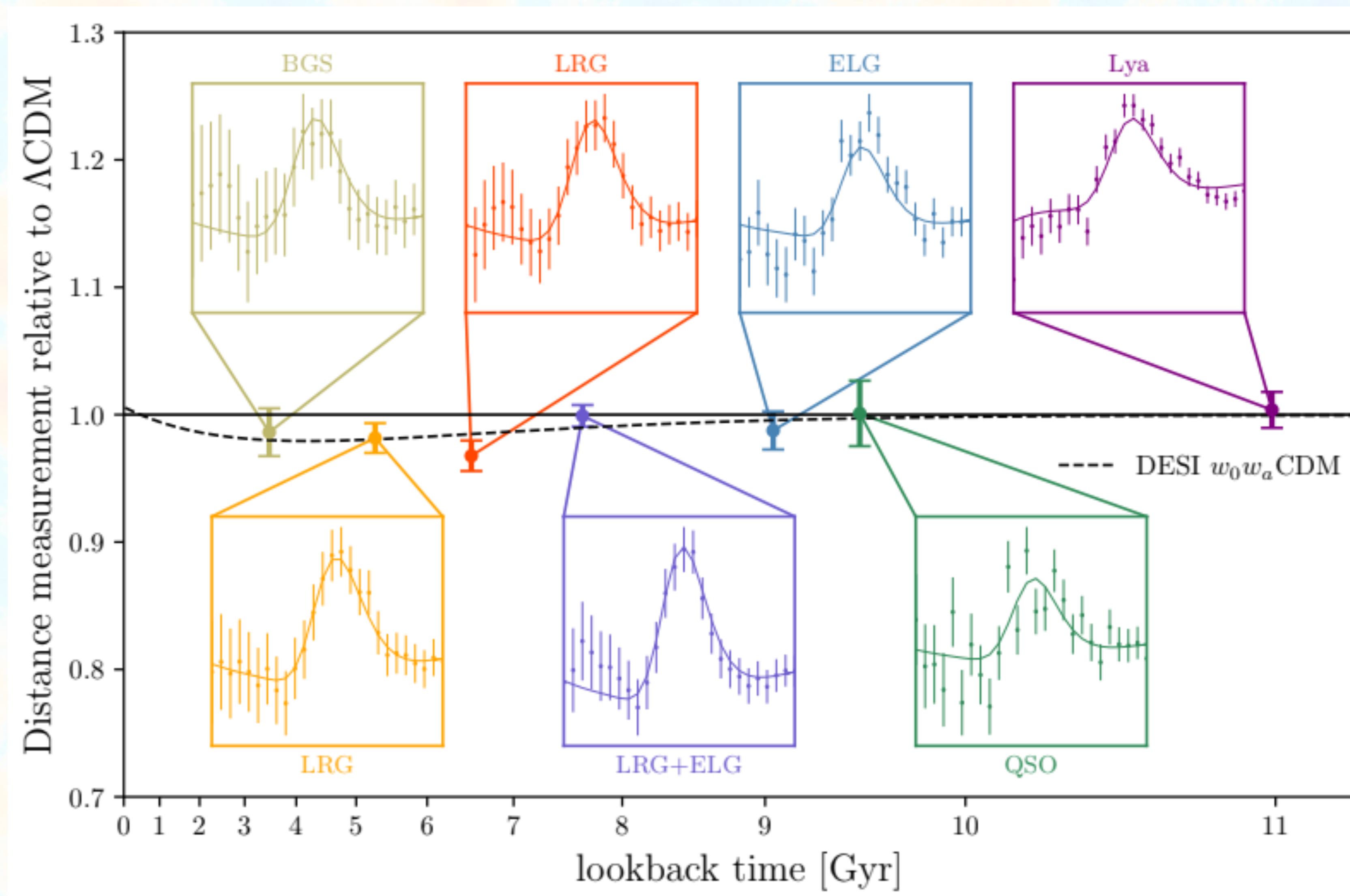
Already the largest BAO dataset ever !

- **5.7 Million** individual redshifts
- Effective cosmic volume $V_{\text{eff}} = 18 \text{ Gpc}^3$
- **~3x bigger** than SDSS

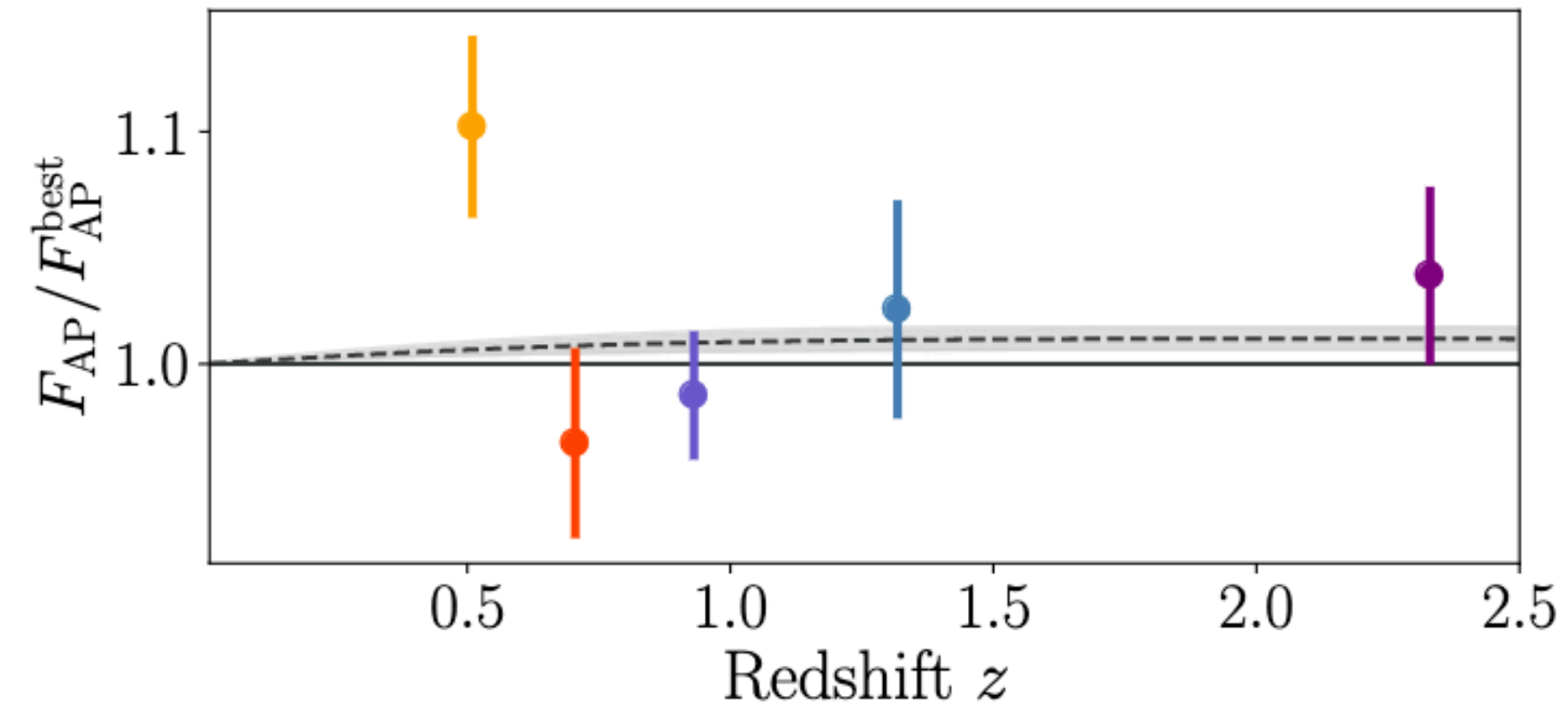
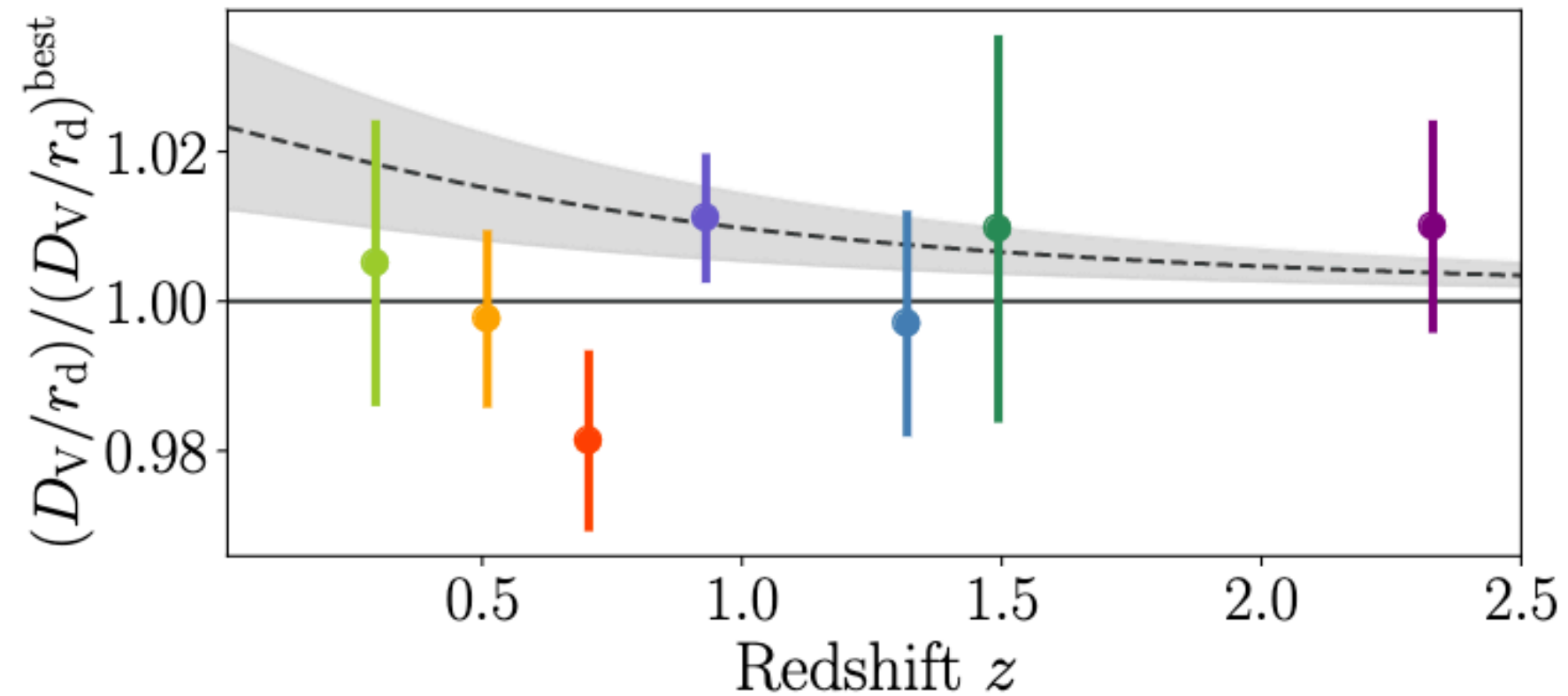
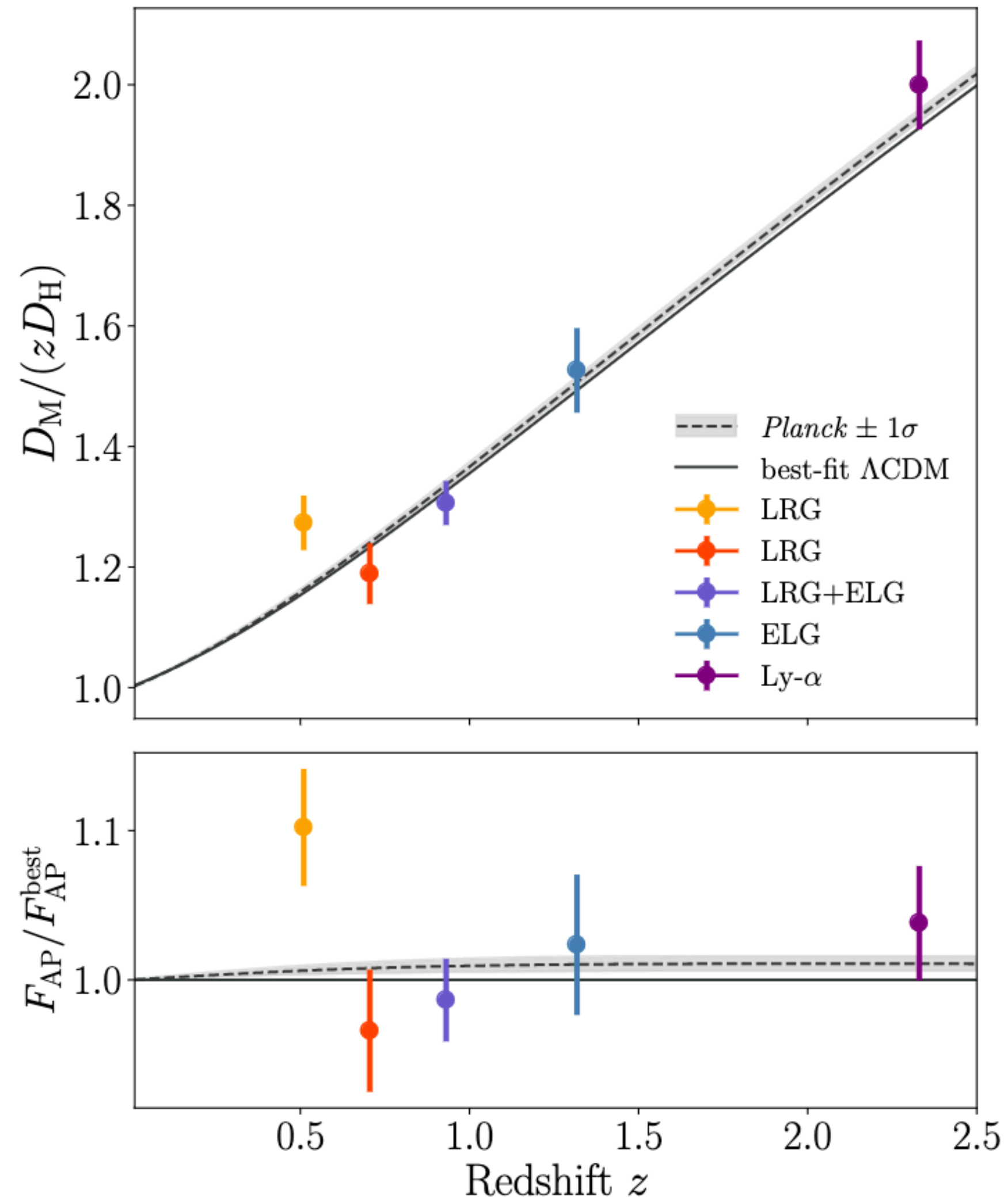
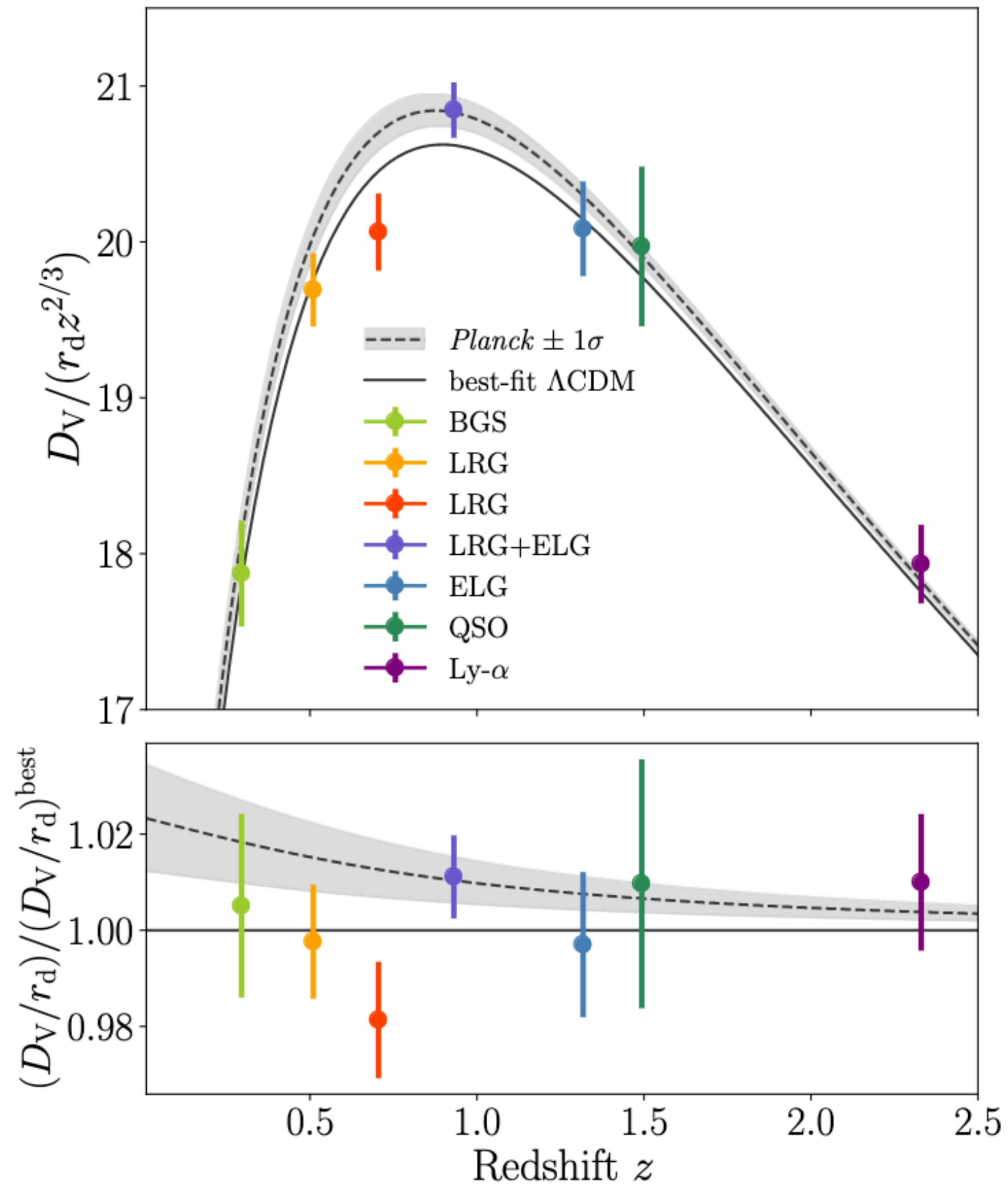
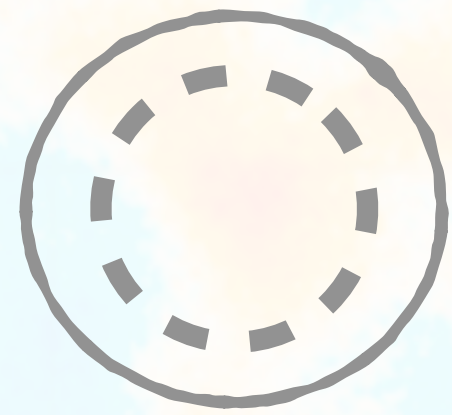
Merely first year of data

First blind analysis !
(At the catalogue level)

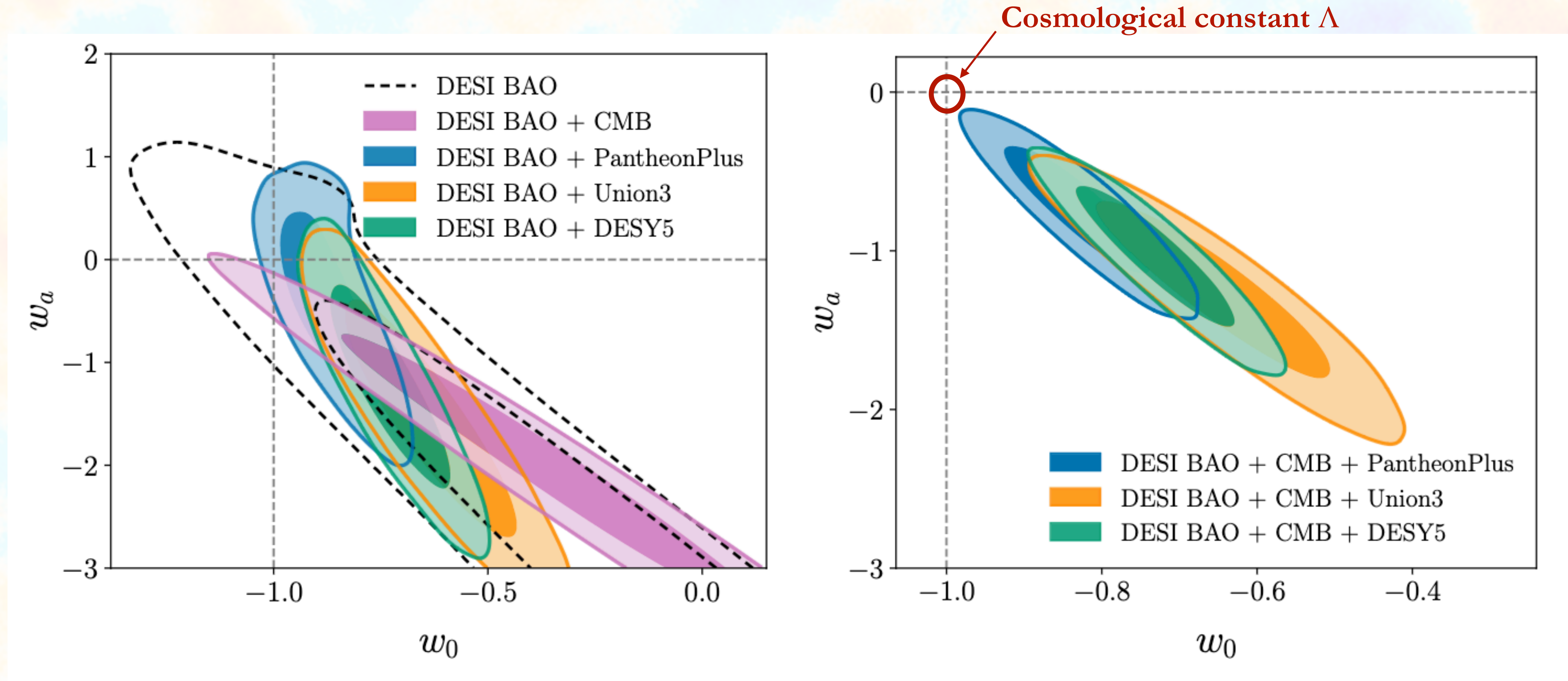
Part III: Cosmological Implications



Distance measurements



Varying equation of state $w(a) = w_0 + w_a(1 - a)$



2.5 σ DESI+CMB+PantheonPlus

3.5 σ DESI+CMB+Union3

3.9 σ DESI+CMB+DESY5

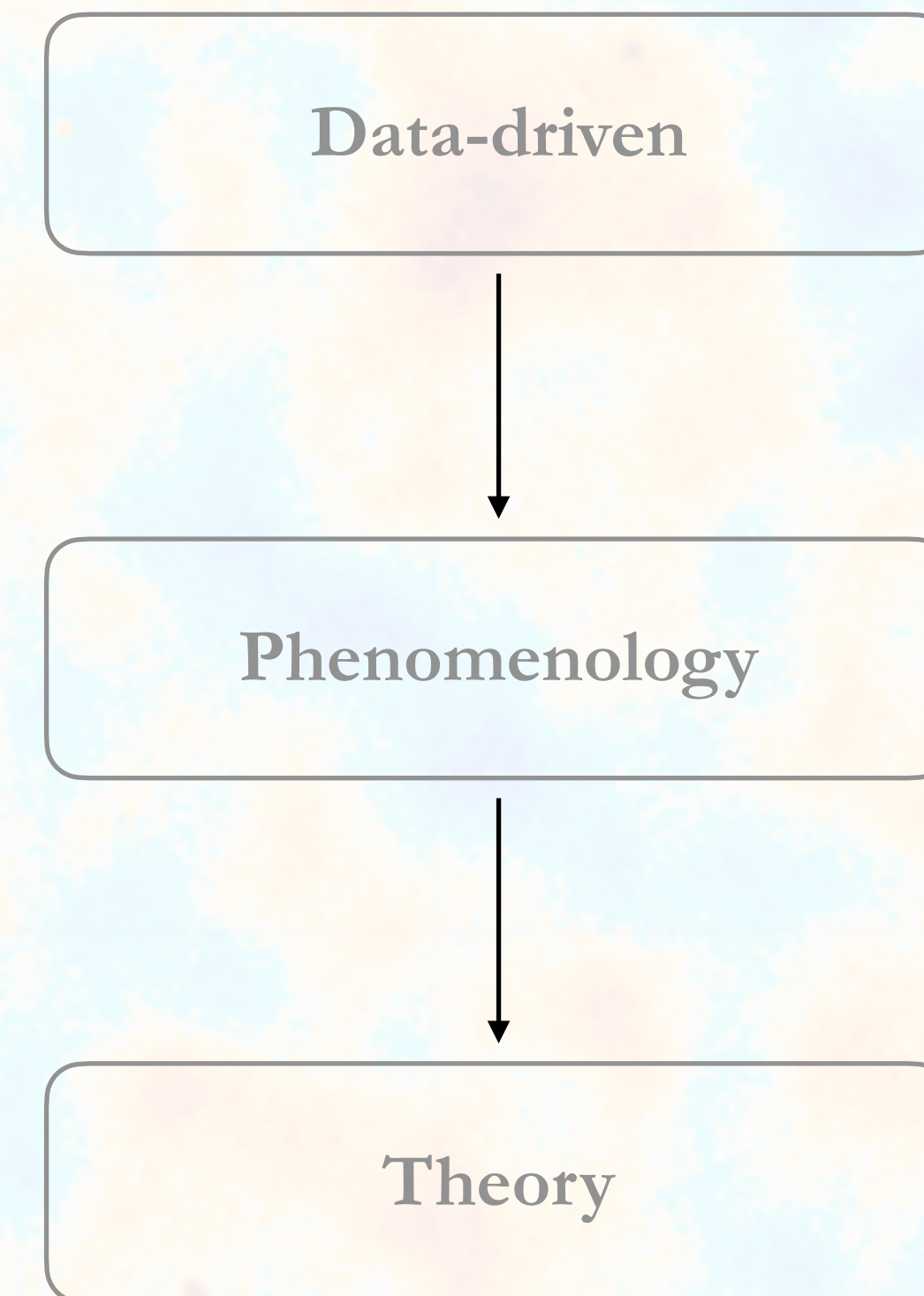
Part IV: Beyond w_0w_a CDM

DESI 2024: Reconstructing Dark Energy using Crossing Statistics with DESI DR1 BAO data

R. Calderon¹, K. Lodha^{1,2}, A. Shafieloo^{1,2}, E. Linder^{3,4,5},
W. Sohn¹, A. de Mattia⁶, J. L. Cervantes-Cota⁷, R. Crittenden⁸,
T. M. Davis⁹, M. Ishak¹⁰, A. G. Kim³, W. Matthewson¹,
G. Niz^{11,12}, S. Park^{1,2}, J. Aguilar³, S. Ahlen¹³, S. Allen^{14,15},
D. Brooks¹⁶, T. Claybaugh³, A. de la Macorra¹⁷, A. Dey¹⁸,
B. Dey¹⁹, P. Doel¹⁶, J. E. Forero-Romero^{20,21},
E. Gaztañaga^{22,8,23}, S. Gontcho A Gontcho³, K. Honscheid^{24,25,26},
C. Howlett⁹, S. Juneau¹⁸, A. Kremin³, M. Landriau³,
L. Le Guillou²⁷, M. E. Levi³, M. Manera^{28,29}, R. Miquel^{30,29},
J. Moustakas³¹, J. A. Newman¹⁹, N. Palanque-Delabrouille^{6,3},
W. J. Percival^{32,33,34}, C. Poppett^{3,4,5}, F. Prada³⁵, M. Rezaie³⁶,
G. Rossi³⁷, V. Ruhlmann-Kleider⁶, E. Sanchez³⁸, D. Schlegel³,
M. Schubnell^{39,40}, H. Seo⁴¹, D. Sprayberry¹⁸, G. Tarlé⁴⁰,
P. Taylor²⁶, M. Vargas-Magaña¹⁷, B. A. Weaver¹⁸, P. Zarrouk²⁷,
H. Zou⁴²

Affiliations are in Appendix F

E-mail: calderon@kasi.re.kr, shafieloo@kasi.re.kr



Modeling of $w(z)$

Chebyshev Polynomial expansion

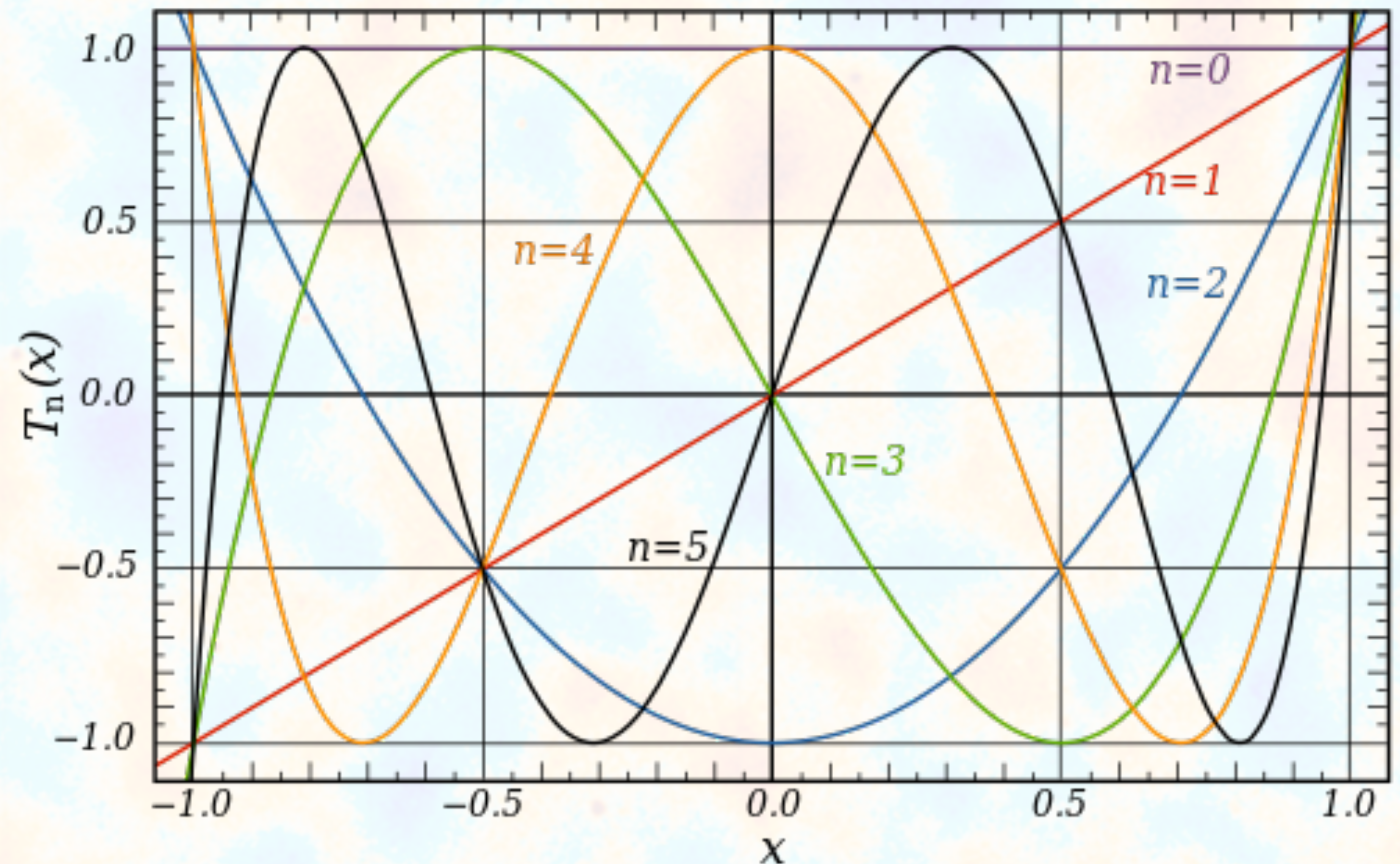
$$w(z) \equiv - \sum_{n=0}^N C_n T_n(x)$$

Form an (orthogonal) basis spanning the space of functions

$$x \equiv 2 \frac{z}{z_{\max}} - 1 \in [-1, 1]$$

$$T_0 = 1, T_1 = x$$

$$T_2 = 2x^2 - 1, T_3 = 4x^3 - 3x$$



Modeling of $w(z)$

R. Calderon, K. Lodha, A. Shafieloo, E. Linder et al - arXiv: [2405.04216](https://arxiv.org/abs/2405.04216)

Chebyshev Polynomial expansion

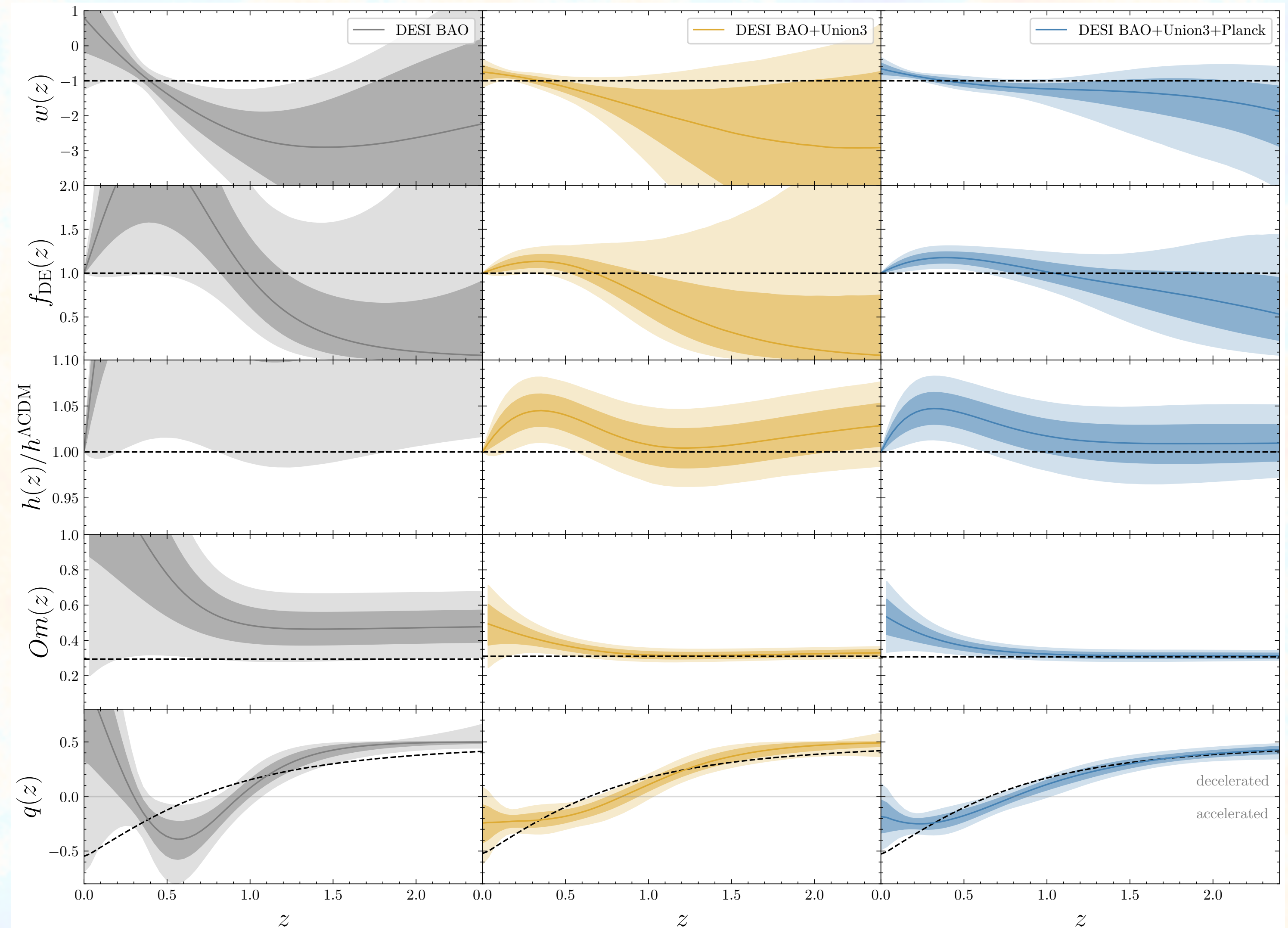
$$w(z) \equiv - \sum_{i=0}^{N=3} C_i T_i(x)$$

$$f_{\text{DE}}(z) \equiv \exp \left(\int_0^z 3[1 + w(z')] d \ln(1 + z') \right)$$

V. Sahni, A. Shafieloo and A. A. Starobinsky (2008)

$$Om(z) \equiv \frac{h^2(z) - 1}{(1 + z)^3 - 1}$$

$$q(z) \equiv - \frac{\ddot{a}a}{\dot{a}^2} = - \frac{\dot{H}}{H^2} - 1 = \frac{d \ln H}{d \ln(1 + z)} - 1$$



Modeling of $f_{\text{DE}}(z) \equiv \rho_{\text{DE}}(z)/\rho_{\text{DE},0}$

R. Calderon, K. Lodha, A. Shafieloo, E. Linder et al - arXiv: 2405.04216

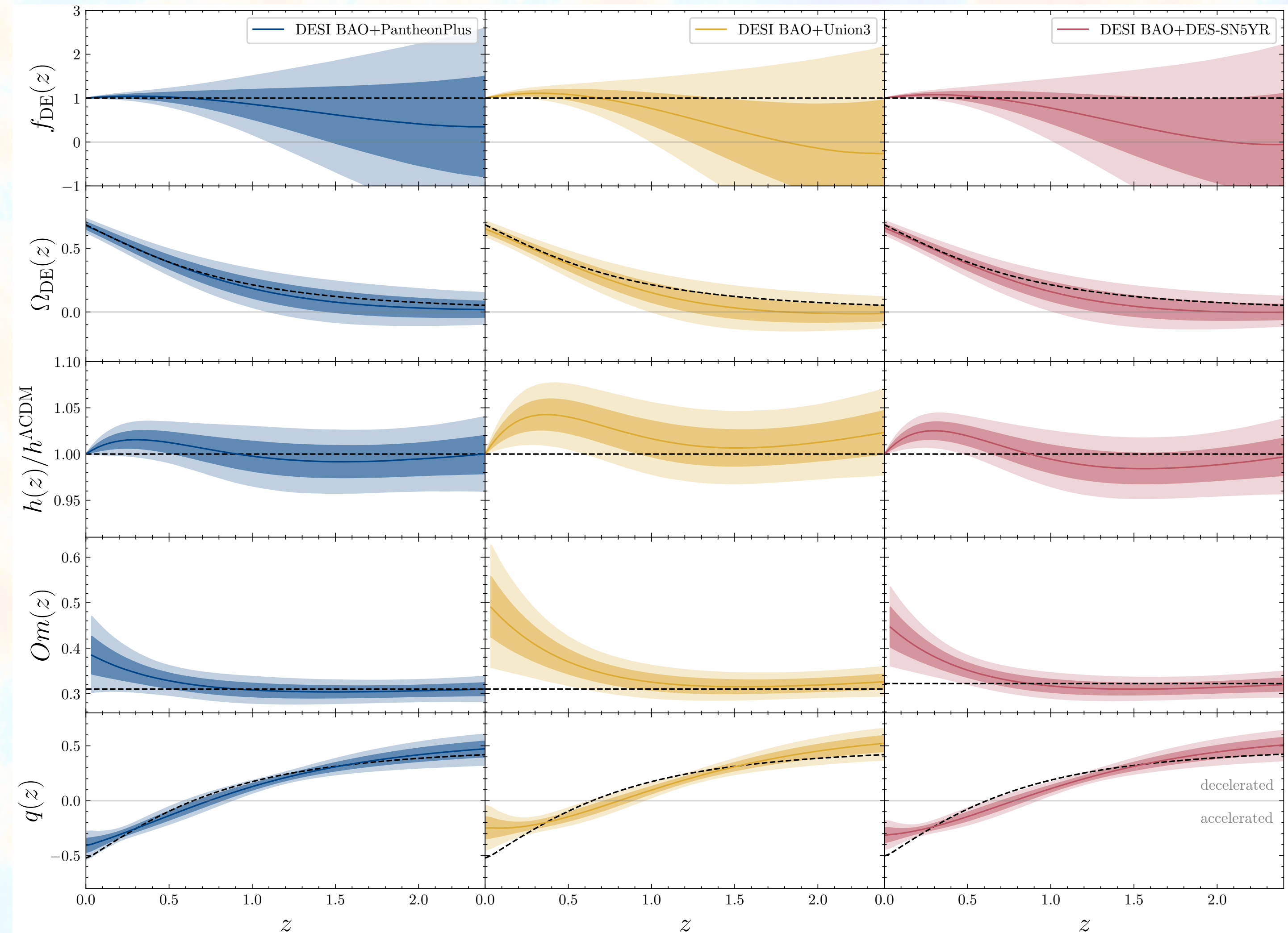
Chebyshev Polynomial expansion

$$f_{\text{DE}}(z) \equiv \sum_{i=0}^N C_i T_i(x)$$

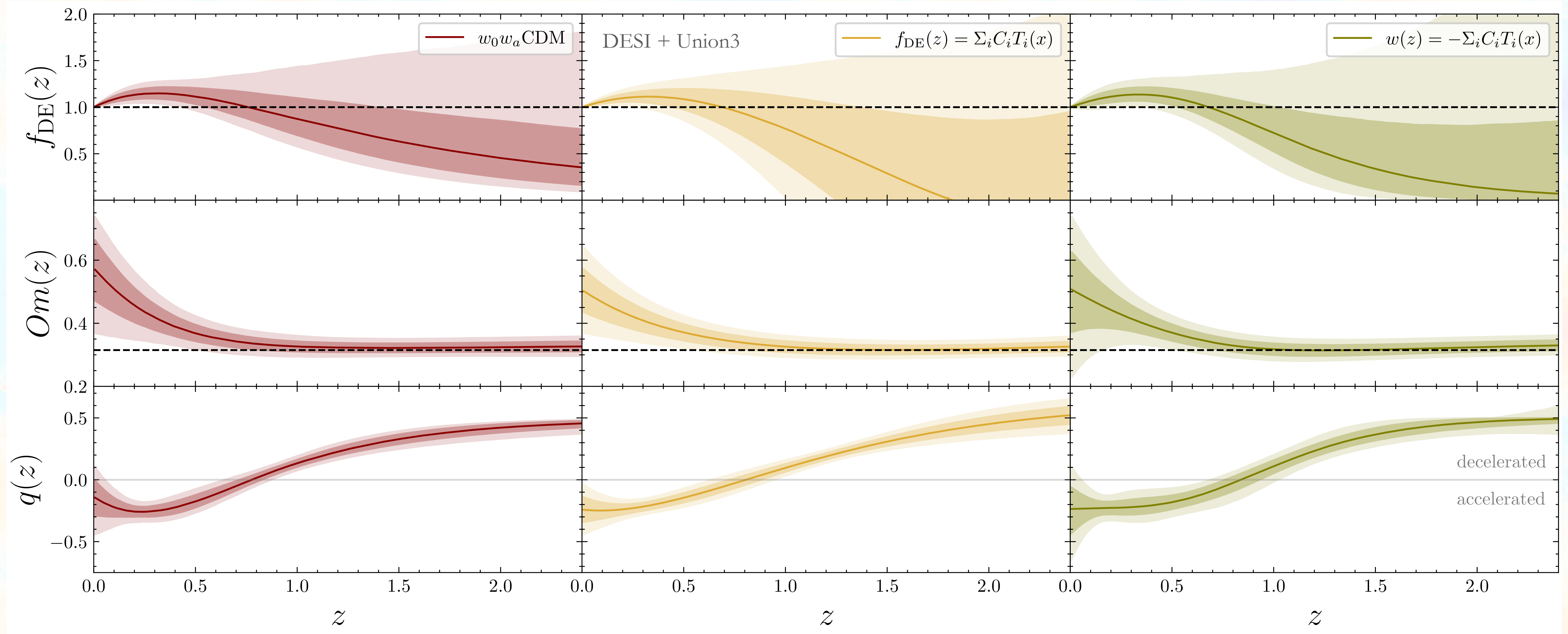
$$C_0 = 1 - \sum_{i=1}^{N=3} C_i T_i(x = -1)$$

$$= 1 - \sum_{i=1}^{N=3} C_i \times (-1)^i$$

$$q(z) \equiv -\frac{\ddot{a}a}{\dot{a}^2} = -\frac{\dot{H}}{H^2} - 1 = \frac{d \ln H}{d \ln(1+z)} - 1$$



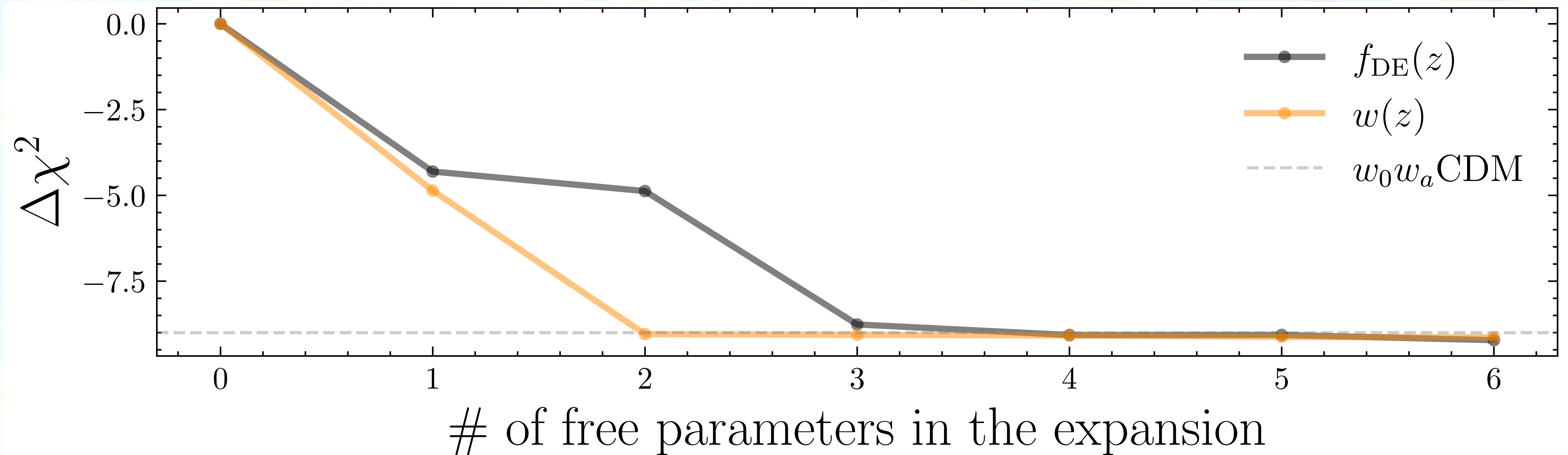
Comparison with w_0w_a CDM



R. Calderon, K. Lodha, A. Shafieloo, E. Linder et al - arXiv: [2405.04216](https://arxiv.org/abs/2405.04216)

Seems w_0w_a CDM is good enough

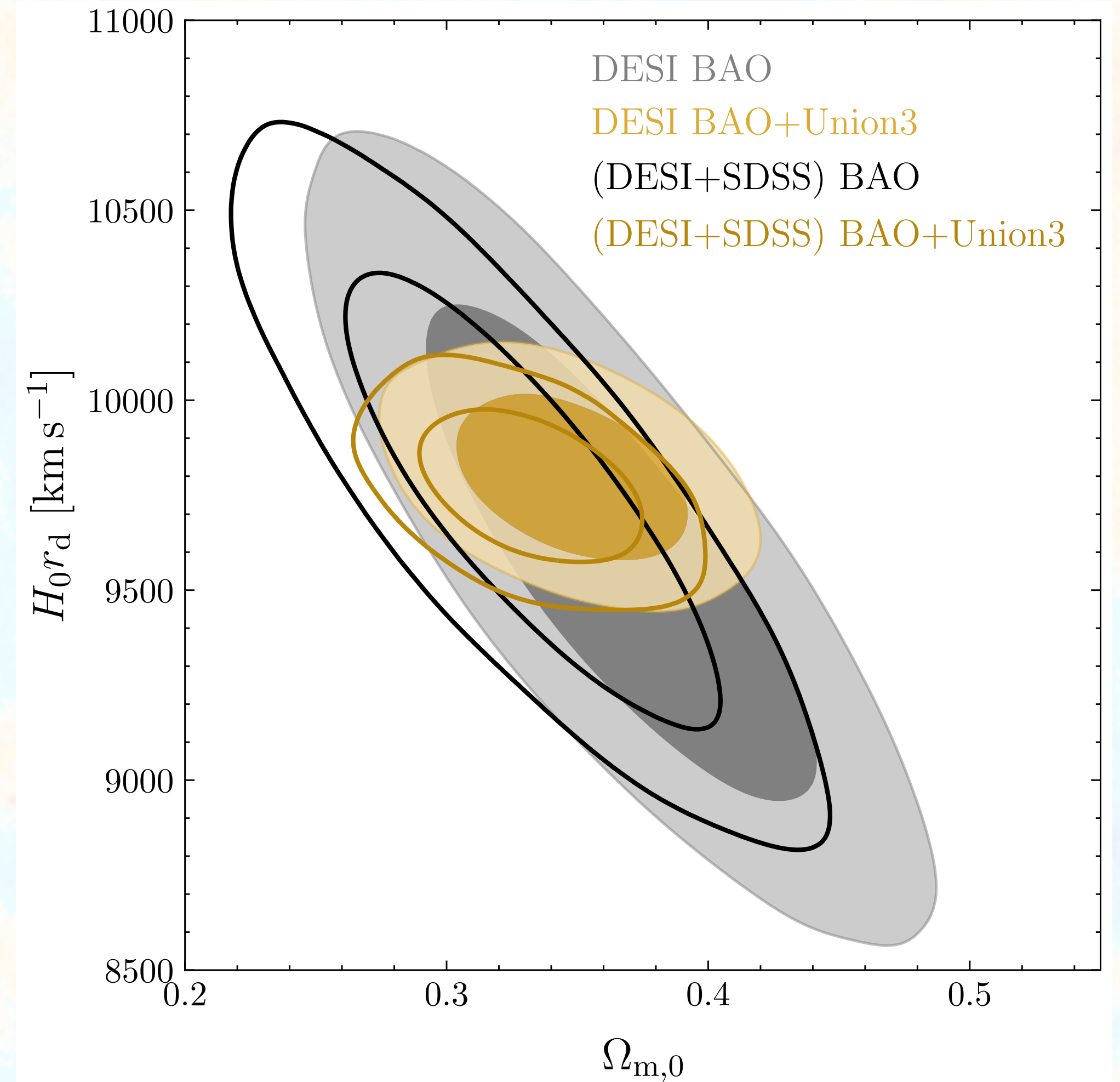
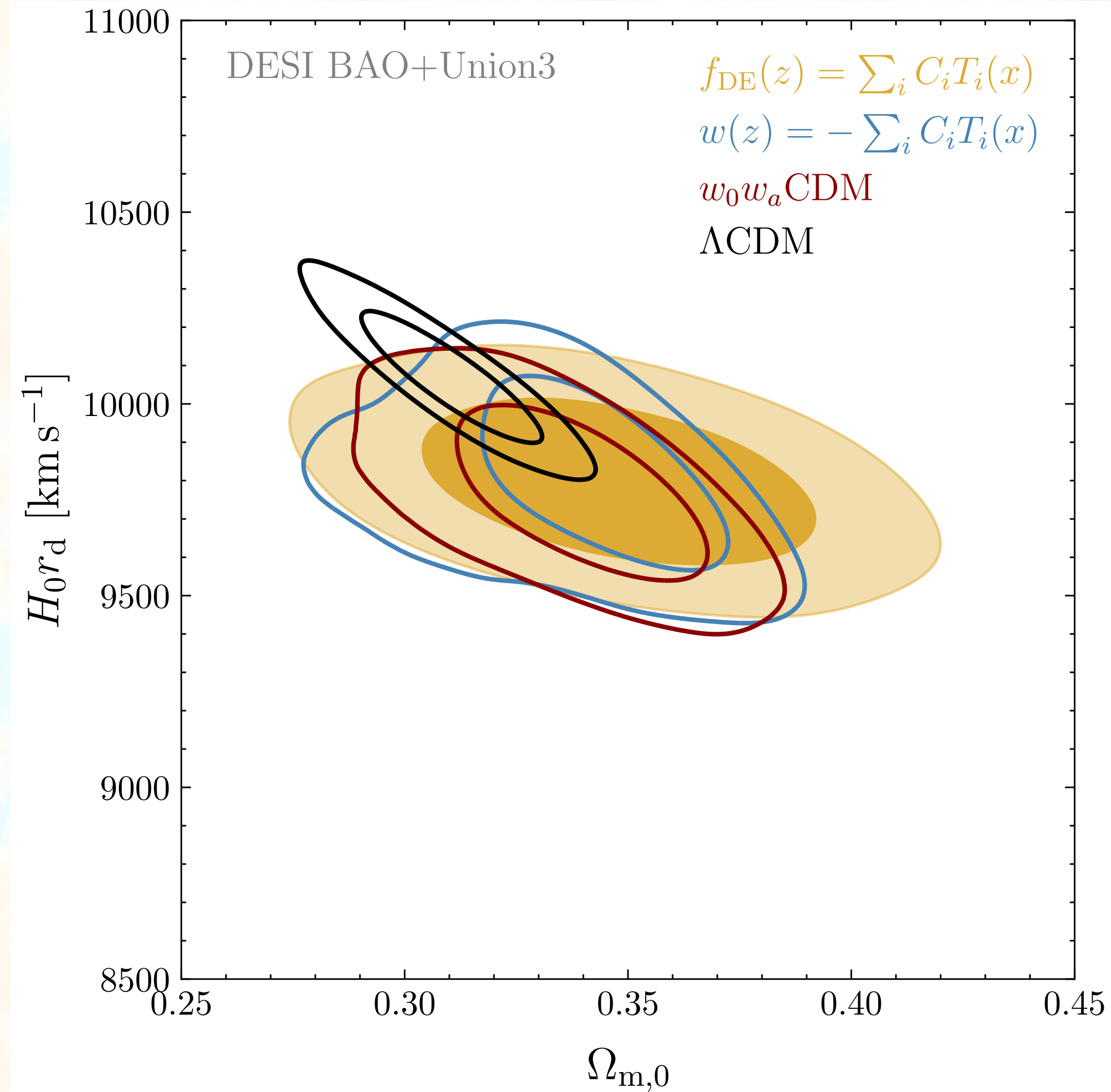
DESI + Union3



R. Calderon, K. Lodha, A. Shafieloo, E. Linder et al - arXiv: [2405.04216](https://arxiv.org/abs/2405.04216)

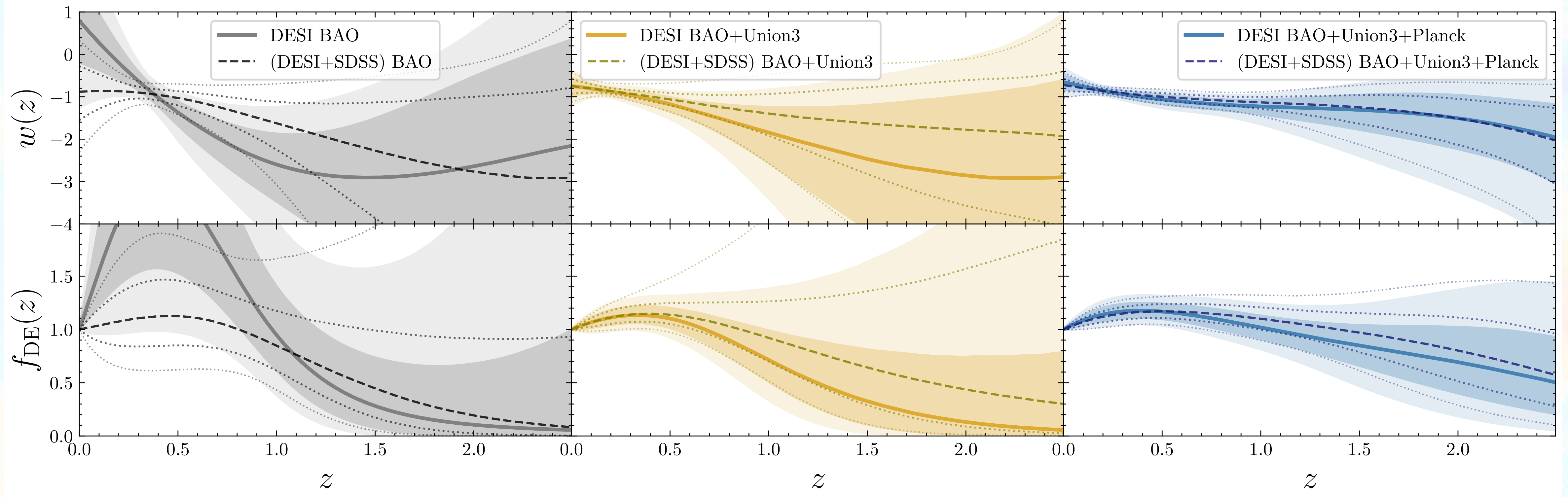
χ^2 “saturates” at 2 d.o.f

Constraints on $H_0 r_d$



R. Calderon, K. Lodha, A. Shafieloo, E. Linder et al - arXiv: [2405.04216](https://arxiv.org/abs/2405.04216)

Comparison with (SDSS+DESI) BAO



R. Calderon, K. Lodha, A. Shafieloo, E. Linder et al - arXiv: [2405.04216](https://arxiv.org/abs/2405.04216)

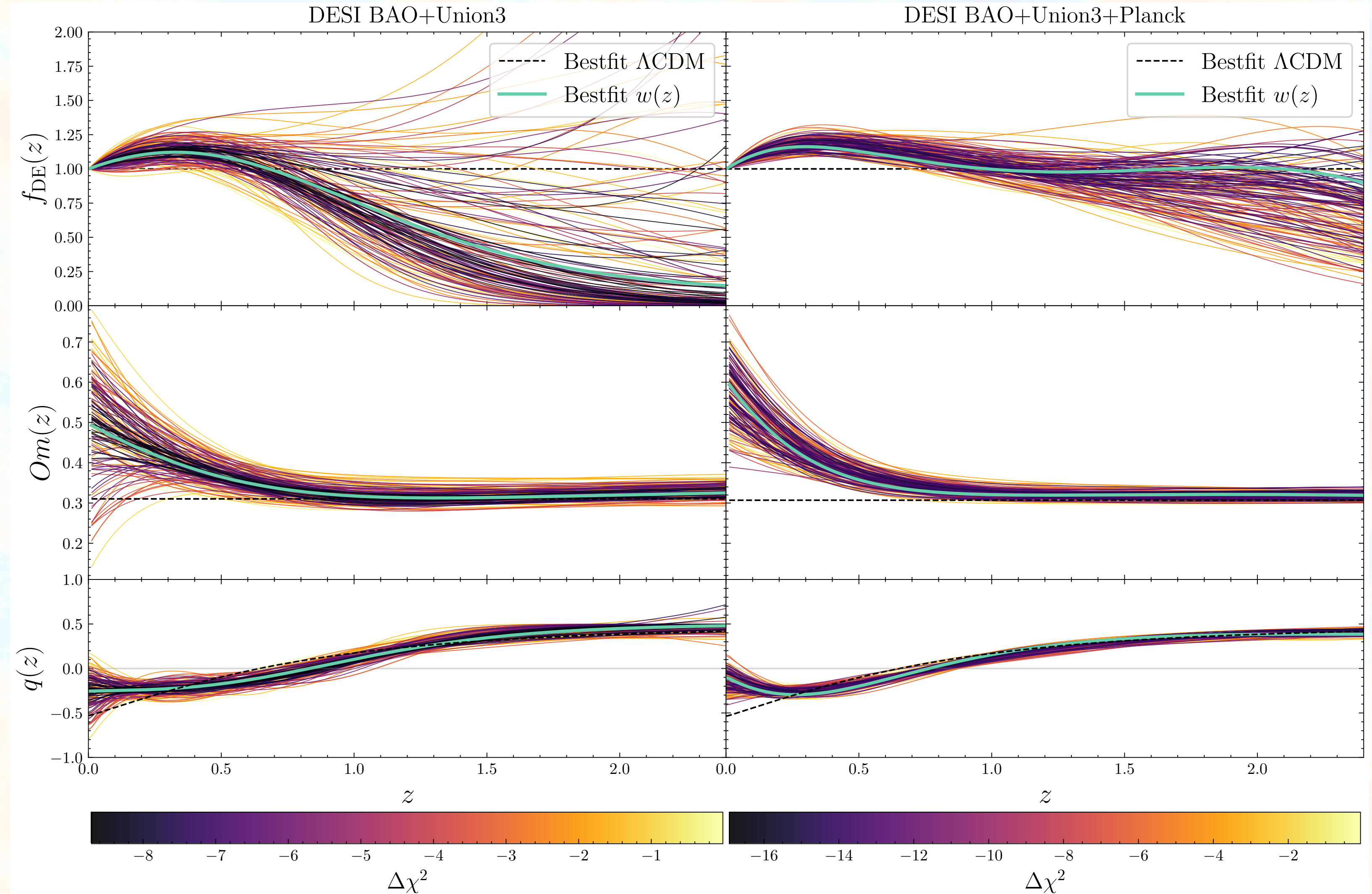
**Overall trends remain !
In particular +Planck**

Improvement in fit

R. Calderon, K. Lodha, A. Shafieloo, E. Linder et al - arXiv: 2405.04216

Individual expansion histories
Improving over Λ CDM

$$\Delta\chi^2 \equiv \Delta\chi^2_{w(z)} - \Delta\chi^2_{\Lambda\text{CDM}}$$



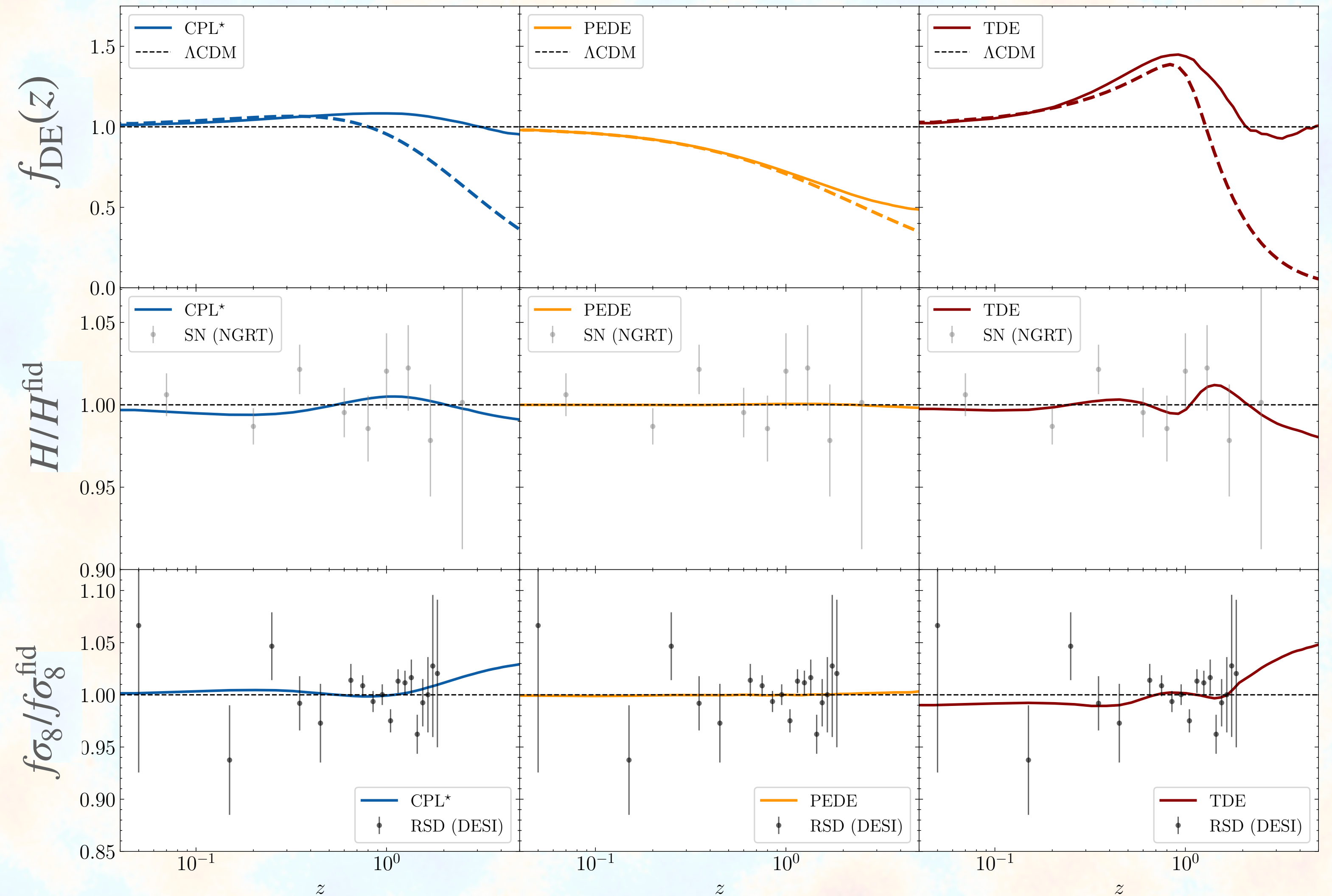
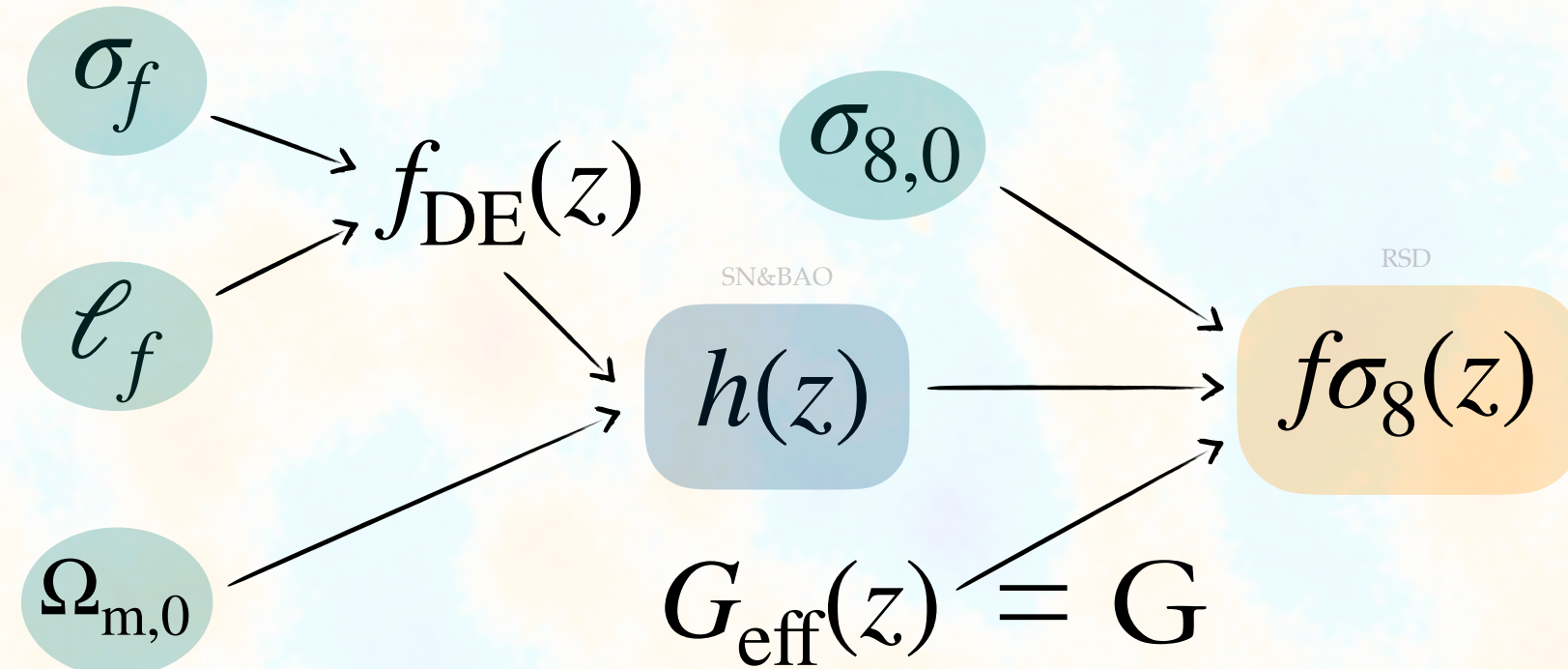
Expansion History (GR)

$$f_{\text{DE}}(z) \equiv \frac{\rho_{\text{DE}}(z)}{\rho_{\text{DE},0}} \sim \mathcal{N}(\bar{f} = 1, K = k(\sigma_f, \ell_f))$$

$$\frac{H^2(z)}{H_0^2} = \Omega_m a^{-3} + (1 - \Omega_m) f_{\text{DE}}(z)$$

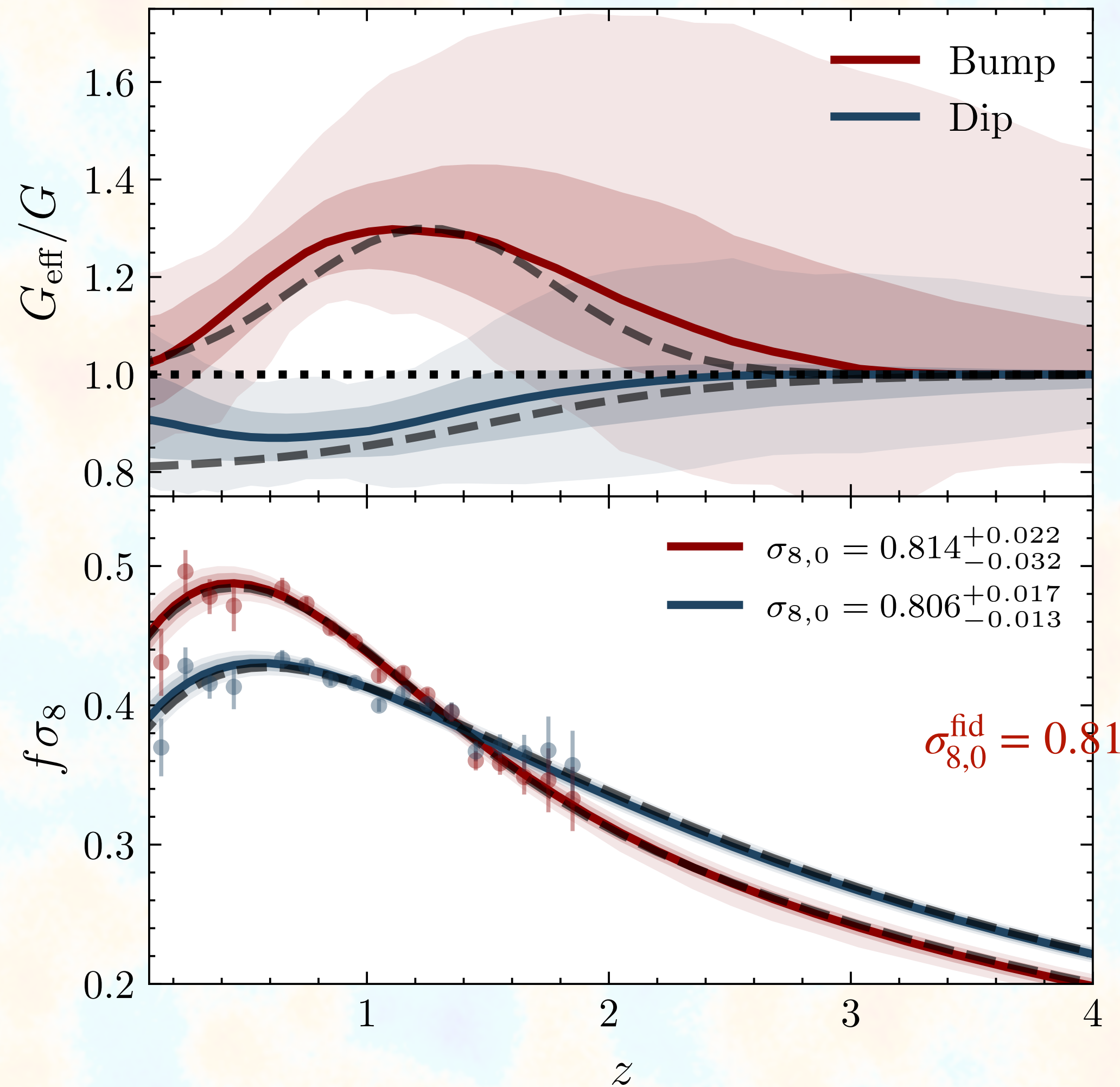
Captures any additional (unknown) component!

$f_{\text{DE}} \neq 1 \Rightarrow$ New physics beyond ΛCDM



Calderón, L'Huillier, Polarski, Shafieloo & Starobinsky - Phys. Rev. D 106 (2022) 8, 083513

Modified Growth



Modified Poisson Equation

$$-\frac{k^2}{a^2}\phi = 4\pi G_{\text{eff}}(z)\rho_m\delta_m$$

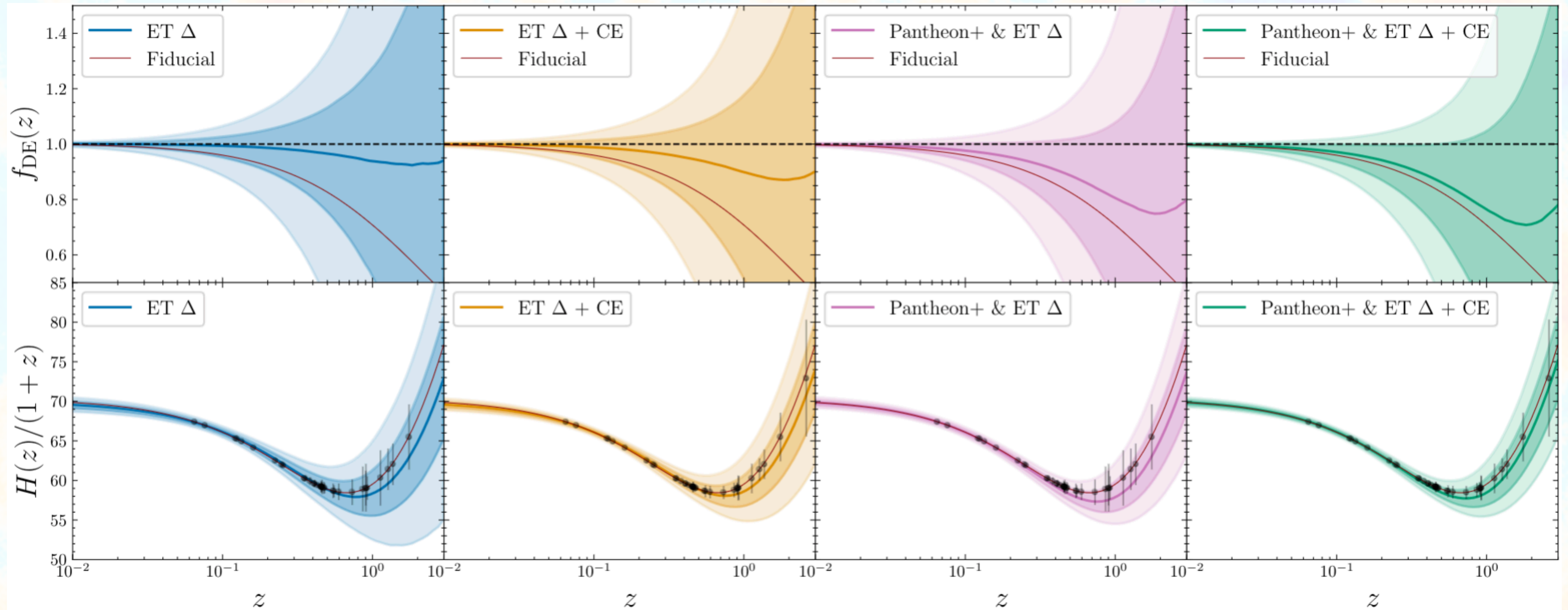
$$\mu(z; \sigma_f, \ell_f, z_c) \sim \mathcal{N}(\bar{f} = 1, k(\sigma_f, \ell_f))$$

- Successful reconstruction of 2 **phenomenological** profiles for $\mu(z) \equiv \frac{G_{\text{eff}}(z)}{G}$
- Unbiased estimation of $\sigma_{8,0}$!
- Posteriors of the hyperparameters contains **valuable information**

$\mu \neq 1 \Rightarrow$ **New physics!**

Calderón, L'Huillier, Polarski, Shafieloo & Starobinsky - Phys. Rev. D 108, 023504

Applications to bright sirens



Cozzumbo, Dupletsa, Calderón, Murgia+, in prep.

Some possible research directions

- **Late-time reconstruction of the expansion history**
Bright & Dark Sirens x LSS (HI-IM)
Robust model-independent determination of H_0
- **Early-Universe changes to the expansion (& growth) history**
Implications for the Hubble and S_8 tensions
Physics prior to recombination
Testing non-standard inflationary scenarios with EFTofLSS
- **Gravitational Waves**
Population studies/Modeling Mass-distributions
Testing the (an)isotropy of the Universe
Model-independent tests of gravity

$$h_p'' + (2 + \alpha_M)\mathcal{H}h_p' + (1 + \alpha_T)k^2h_p = \Pi_p \quad \longrightarrow \quad d_L^{\text{GW}}(z) = d_L^{\text{EM}}(z) \exp\left(\frac{1}{2} \int_0^z \alpha_M(\tilde{z}) d \ln(1 + \tilde{z})\right)$$

Summary & prospects

- More **constraining power** demands more **careful** analyses:
Scrutiny for systematics and confirmation biases
- **BAO** is one of the **most mature probes** of modern cosmology
Distance measurements that can be used to test alternative cosmological models
Direct-fit/Full-shape power spectrum analysis on the way (RSD)!
- Tantalizing hints of an **evolving dark energy** component:
 $\sim 2.5 - 4\sigma$ deviation from ($w_0 = -1, w_a = 0$)
- Year 3 data acquisition complete. Analysis on the way!

Distance measurements that can be used to test alternative cosmological models

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