



Have we observed **Lorentz invariance violation** in very high-energy cosmic messengers?

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**What? Quantum gravity
phenomenology?**

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Initial ideas in QG phenomenology

Initial ideas and suggestions to test quantum gravity by amplification mechanisms:

- Testing **CPT invariance** in neutral mesons

[Ellis, Lopez, Mavromatos, Nanopoulos, PRD 1996]

$$\frac{|m_{K^0} - m_{\bar{K}^0}|}{m_{K^0}} \sim \mathcal{O}(10^{-19})$$

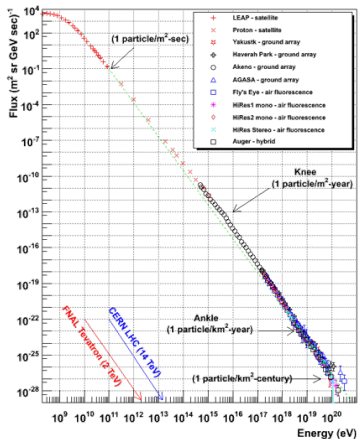
- **Time of flight studies** in GRBs (HEGRA, Whipple telescopes; EGRET satellite)

[Amelino-Camelia, Ellis, Mavromatos, Nanopoulos, Sarkar, Nature 1998]

$$\Delta t \approx \xi \frac{E}{E_{\text{Pl}}} \frac{L}{c}$$

The AGASA result and the GZK cutoff

Cosmic Ray Spectra of Various Experiments

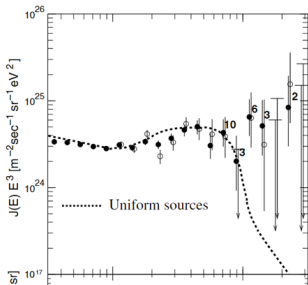


Cutoff GZK: $p + \gamma_{\text{CMB}} \rightarrow p + \pi$

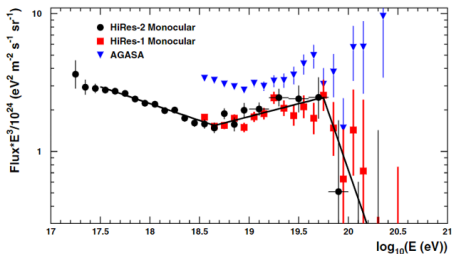
$$E_{\text{GZK}} \simeq \frac{m_p m_\pi}{2E_\gamma} \simeq 3 \times 10^{20} \text{ eV} \times \left(\frac{2.7 \text{ K}}{E_\gamma} \right)$$

[Greisen, 1966; Zatsepin and Kuzmin, 1966]

The AGASA result and the GZK cutoff



[Takeda et al., *Astrop. Phys.* 2003,
Akeno Giant Air Shower Array
(AGASA) experiment]



[Abbasi et al., *PRL* 2008, *High Resolution Fly's Eye*
(HiRES) experiment]

$$E^2 - p^2 - m^2 \simeq \xi_n E^2 \left(\frac{E}{E_{\text{Pl}}} \right)^n$$

$$\xi_n < 0$$

No GZK cutoff

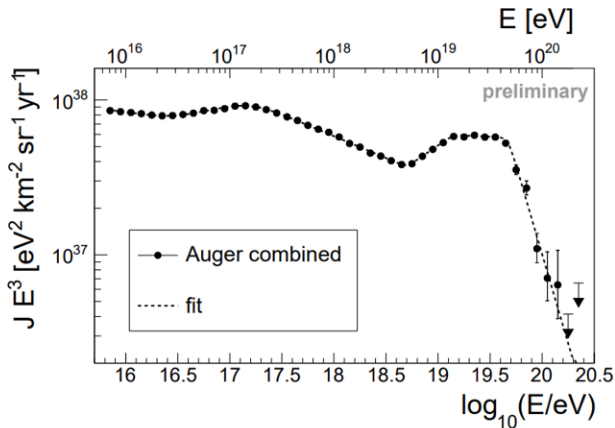
$$\xi_n > 0$$

$$\xi_1 \lesssim 10^{-14}, \quad \xi_2 \lesssim 10^{-6}$$

[Aloisio, Blasi, Ghia, Grillo, *PRD* 2000]

**Have we observed new physics
in VHE cosmic messengers?**

The UHECR spectrum and the muon puzzle

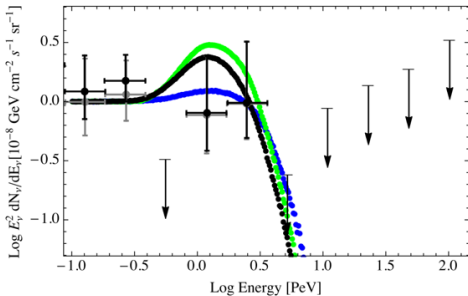


[Pierre Auger Collaboration, PoS (ICRC 2021)]

Muon puzzle: PA Collab, PRL 2016; Dembinski et al., EPJ Web Conf. (UHECR 2018):

"We combine data from eight leading air shower experiments to cover shower energies from PeV to tens of EeV. Above 10 PeV, we find a muon deficit in simulated air showers for each of the six considered hadronic interaction models. The deficit is increasing with shower energy. For the models EPOS-LHC and QGSJet-II.04, the slope is found significant at 8 sigma."

The spectrum of astrophysical neutrinos



Astrophysical neutrino flux from IceCube data (points)

[IceCube Collab., PRL 2014]

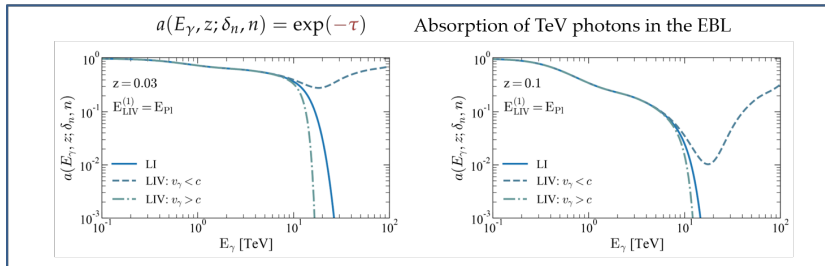
Neutrino spectrum with LIV propagation, showing a cutoff

[Stecker, Scully, Liberati, Mattingly, PRD 2015]

Transparency of the Universe

High-energy photons are absorbed in photon backgrounds,

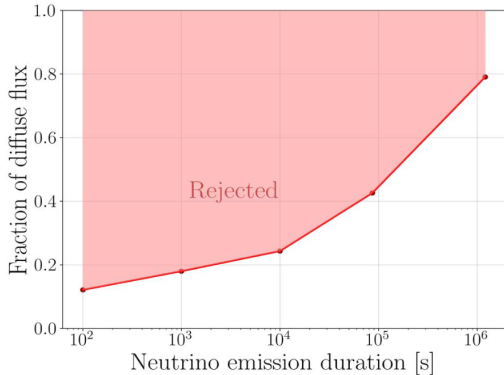
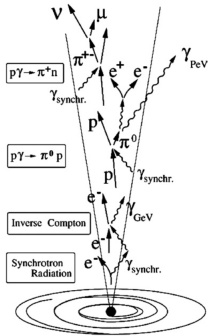
$$\Phi_{\text{obs}}(E, z) = \exp(-\tau(E, z))\Phi(E(1+z))$$



[Martínez-Huerta, Lang, de Souza, *Symmetry* 12,8 (2020)]

- Sensitivity of $E_{\text{LIV}}^{(1)}$ to the Planck scale
- LHAASO results severely constrains the superluminal scenario because of pair-emission ($\gamma \rightarrow e^+ e^-$) and photon splitting ($\gamma \rightarrow 3\gamma$) processes

Where are the GRB neutrinos?



IceCube Collab, ApJ 2022

ANTARES Collab, MNRAS 2021

**What are the implications of LIV
in the cosmic messengers?**

Neutrinos could be unstable particles!

LIV in the neutrino sector parametrized by a **high-energy scale Λ**

$$\mathcal{L}_{\text{free}} = \bar{\nu}_L (i\gamma^\mu \partial_\mu) \nu_L - \frac{1}{\Lambda^n} \bar{\nu}_L \gamma^0 (i\partial_0)^{n+1} \nu_L,$$

producing a **modified dispersion relation**,

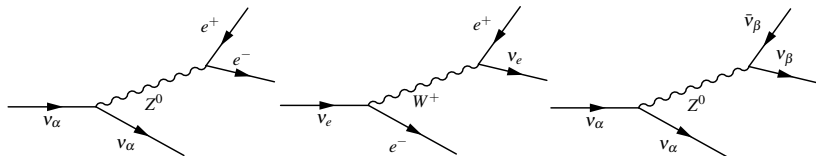
$$E_\nu = |\vec{p}_\nu| \left[1 + \left(\frac{|\vec{p}_\nu|}{\Lambda} \right)^n \right],$$
$$E_{\bar{\nu}} = |\vec{p}_{\bar{\nu}}| \left[1 + (-1)^n \left(\frac{|\vec{p}_{\bar{\nu}}|}{\Lambda} \right)^n \right].$$

$n = 1$ Superluminal neutrinos and subluminal antineutrinos

$n = 2$ Both neutrinos and antineutrinos are superluminal particles

Neutrinos could be unstable particles!

Superluminal neutrinos are **unstable** and can decay emitting an **electron-positron** (VPE) or **neutrino-antineutrino** (NSpl) pair,



VPE (Neutral channel / Charged channel)

NSpl (Neutral channel)

- VPE has a (kinematical) threshold $E_{\text{th}}^{(n)} := (2m_e^2 \Lambda^n)^{1/(2+n)}$
- The NSpl threshold is negligible

Neutrinos could be unstable particles!

We can use the **collinearity** of the high-energy interactions to compute the **total decay widths**

[Carmona, Cortés, Relancio, Reyes, PRD 2023]

$$\Gamma_{\nu_\alpha \rightarrow \nu_\alpha + l + \bar{l}}^{(n)}(E) = 10^{-4} G_F^2 \left[E^5 \left(\frac{E}{\Lambda} \right)^{3n} \right] K_{\nu_\alpha, l}^{(n)}$$

	$K_{\nu_\alpha, l}^{(n)}$	
Decay	$n = 1$	$n = 2$
$\nu_{\mu, \tau} \rightarrow \nu_{\mu, \tau} e^+ e^-$	1.01	1.24
$\nu_e \rightarrow \nu_e e^+ e^-$	13.0	16.1
$\nu_\alpha \rightarrow \nu_\alpha \nu_\beta \bar{\nu}_\beta$	1.29	1.29

Neutrinos could be unstable particles!

If we define an **energy scale** $E_\alpha^{(n)}$ at which the decay rate equals the expansion rate,

$$\Gamma_\alpha^{(n)}(E)|_{E=E_\alpha^{(n)}} = H_0.$$

then we can write

$$\Gamma_\alpha^{(n)}(E) = H_0 \left(E/E_\alpha^{(n)} \right)^{5+3n}$$

➤ As a consequence of the **strong energy dependence** of the decay width, $E_\alpha^{(n)}$ acts as an **'effective' threshold** for the decay of superluminal neutrinos, producing a **cutoff** in their energy spectrum

$$n = 1 \quad E_{\max}^{(1)} \approx 3.88 \text{ TeV} \left(\frac{\Lambda}{M_P} \right)^{3/8}$$

$$n = 2 \quad E_{\max}^{(2)} \approx 6.53 \times 10^4 \text{ TeV} \left(\frac{\Lambda}{M_P} \right)^{6/11}$$

Time delay studies are incomplete!

Another consequence of LIV modified dispersion relations is **energy-dependent** neutrino propagation **velocities**, even in the massless limit, leading to a modification of their **time of flight**

$$v = \frac{dE}{dp} \approx 1 \pm (n+1) \left(\frac{E}{\Lambda} \right)^n$$

$$n = 1 \quad \delta t_{\text{LIV}}^{(1)} \approx \pm 7.22 \times 10^3 \text{ s} \left(\frac{E}{100 \text{ TeV}} \right) \left(\frac{\Lambda}{M_P} \right)^{-1} I_1(z)$$

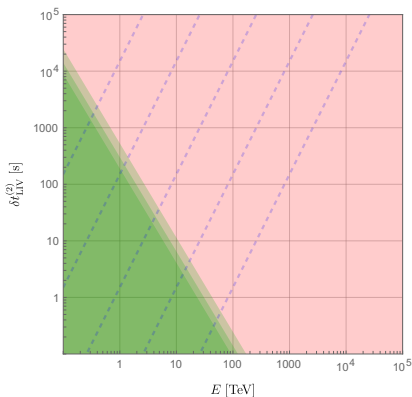
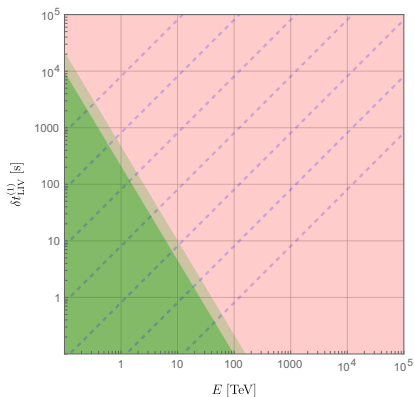
$$n = 2 \quad \delta t_{\text{LIV}}^{(2)} \approx \pm 8.89 \times 10^{-11} \text{ s} \left(\frac{E}{100 \text{ TeV}} \right)^2 \left(\frac{\Lambda}{M_P} \right)^{-2} I_2(z)$$

where

$$I_n(z) = \int_0^z dz' \frac{(1+z')^n}{\sqrt{\Omega_m(1+z')^3 + \Omega_\Lambda}}$$

Time delays studies are incomplete!

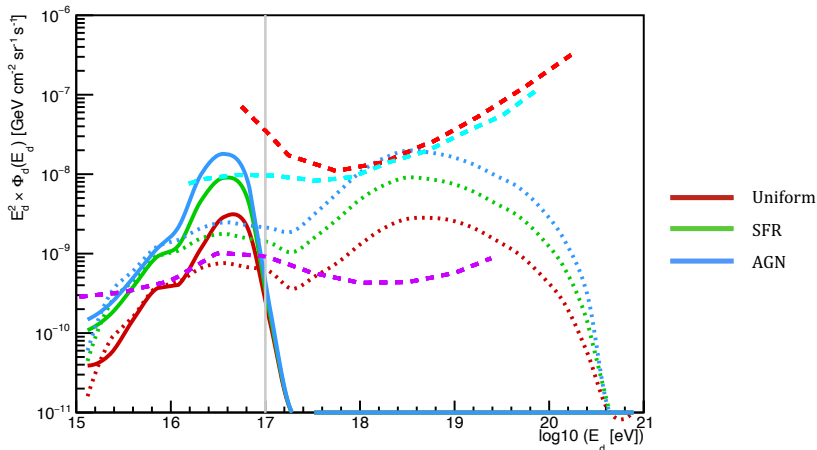
The observation of superluminal neutrinos is **correlated** with their possible time delays with respect to photons



Allowed (green) and excluded (red) regions for superluminal neutrino events, for $n = 1$ (left) and $n = 2$ (right), and from the lightest to the darker green, for $z = 0.1, 1$ and 3 .

Dashed blue lines show points with constant Λ (from top-left to bottom-right: $\log_{10}(\Lambda / M_p) = -2, -1, 0, 1, 2, 3$ and 4).

Cosmogenic neutrinos could be nearer than we thought!



Cosmogenic neutrino flux at Earth for $n = 2$, $\Lambda/M_p = 2.19$ and for different models for the production of the UHECR, and the 90% CL upper limits of IceCube (cyan), Auger (red), and IceCube-Gen2 (purple)

[Reyes, Boncioli, Carmona, Cortés, PoS(ICRC2023)]

Modified dispersion relation for photons:

$$E^2 - \vec{k}^2 = E^2 \sum_{n=1}^{\infty} S_n \left(\frac{E}{E_{\text{LIV},n}} \right)^n \quad S_n = \pm 1 \quad (+ \text{SuL}; - \text{SubL})$$

➤ $n = 1$

Birefringence: $E_{\text{LIV},1} \gg E_{\text{Pl}}$

SuL, photon decay: $E_{\text{LIV},1} \gtrsim 10^3 E_{\text{Pl}}$

Time delays: $E_{\text{LIV},1} \gtrsim E_{\text{Pl}}$

➤ $n = 2$

SuL, photon decay: $E_{\text{LIV},2} \gtrsim 10^{-4} E_{\text{Pl}}$

Time delays: $E_{\text{LIV},2} \gtrsim 10^{-8} E_{\text{Pl}}$

SubL, Univ transparency: $E_{\text{LIV},2} \gtrsim 10^{-7} E_{\text{Pl}}$

The $n = 2$ subluminal case offers two complementary phenomenological windows

Transparency studies of the Universe underestimate LIV!

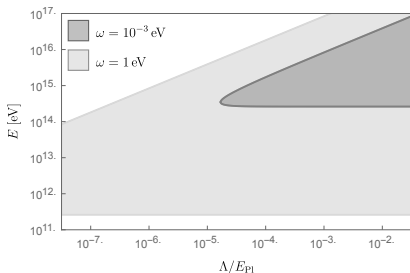
Pair creation: $\gamma_{\text{VHE}}(k) + \gamma_{\text{soft}}(q) \rightarrow e^-(p_-) + e^+(p_+)$

➤ Threshold in SR: $\bar{s} \equiv \frac{2E\omega(1 - \cos\theta)}{4m_e^2} \geq 1$

A subluminal LIV for the photon increases the transparency of the Universe to VHE gamma rays

➤ Modified photon dispersion relation: $E^2 - \vec{k}^2 = -\frac{E^4}{\Lambda^2}$

➤ New threshold condition: $\bar{\tau} \equiv \bar{s} - \bar{\mu} \geq 1$, where $\bar{\mu} = \frac{E^4}{4m_e^2\Lambda^2}$



Transparency studies of the Universe underestimate LIV!

SR: $\sigma_{\text{SR}}(E, \omega, \theta) = \frac{1}{\mathcal{K}(\bar{s})} \mathcal{F}_{\text{BW}}(\bar{s}) \quad \mathcal{K}(\bar{s}) = 8m_e^2 \bar{s}$

$$\mathcal{F}_{\text{BW}}(\bar{s}) = 4\pi\alpha^2 \left[\left(2 + \frac{2}{\bar{s}} - \frac{1}{\bar{s}^2} \right) \ln \left(\frac{1 + \sqrt{1 - 1/\bar{s}}}{1 - \sqrt{1 - 1/\bar{s}}} \right) - \left(2 + \frac{2}{\bar{s}} \right) \sqrt{1 - 1/\bar{s}} \right]$$

LIV:

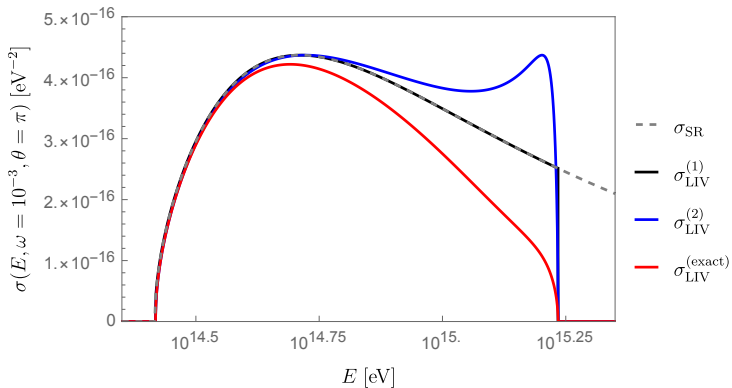
[Martínez-Huerta et al, *Symmetry* 2020] $\sigma_{\text{LIV}}^{(1)} \approx \sigma_{\text{SR}}(\bar{s})$

[Tavecchio, Bonoli, *A&A* 2016] $\sigma_{\text{LIV}}^{(2)} \approx \sigma_{\text{SR}}(\bar{\tau}), \quad \bar{\tau} \equiv \bar{s} - \bar{\mu}$

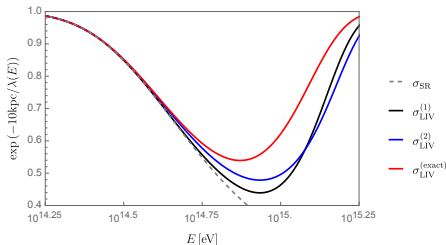
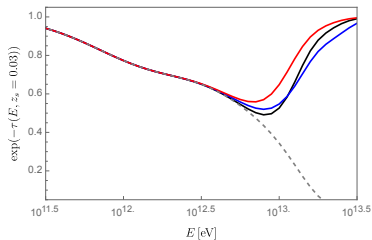
[New calculation] $\sigma_{\text{LIV}}^{(\text{exact})} = \frac{1}{\mathcal{K}(\bar{s})} \mathcal{F}_{\text{LIV}}(\bar{\tau}, \bar{\mu})$

$$\mathcal{F}_{\text{LIV}}(\bar{\tau}, \bar{\mu}) = 4\pi\alpha^2 \left[\left(2 + \frac{2\bar{\tau}(1 - 2\bar{\mu})}{(\bar{\tau} + \bar{\mu})^2} - \frac{(1 - \bar{\mu})}{(\bar{\tau} + \bar{\mu})^2} \right) \times \ln \left(\frac{1 + \sqrt{1 - 1/\bar{\tau}}}{1 - \sqrt{1 - 1/\bar{\tau}}} \right) - \left(2 + \frac{2\bar{\tau}(1 - 4\bar{\mu})}{(\bar{\tau} + \bar{\mu})^2} \right) \sqrt{1 - 1/\bar{\tau}} \right]$$

Transparency studies of the Universe underestimate LIV!



Transparency studies of the Universe underestimate LIV!



$z = 0.03$

ϵ	30%	50%
$\Lambda^{(2)}/E_{Pl}$	$1.6 \cdot 10^{-8}$	$1.1 \cdot 10^{-8}$
$\Lambda^{(expl.)}/E_{Pl}$	$2.0 \cdot 10^{-8}$	$1.5 \cdot 10^{-8}$

$d = 10 \text{ kpc}$

ϵ	30%	50%
$\Lambda^{(2)}/E_{Pl}$	$1.3 \cdot 10^{-4}$	$1.0 \cdot 10^{-4}$
$\Lambda^{(expl.)}/E_{Pl}$	$1.8 \cdot 10^{-4}$	$1.4 \cdot 10^{-4}$

➤ The use of the standard approximation produces a $\sim 25\%$ underestimate in the bounds on the LIV scale with respect to the explicit calculation

Conclusions: Have we observed LIV in cosmic messengers?

- **High-energy astrophysics** has the potential to reveal experimental signatures of a **QG theory**: tiny effects in the interaction and propagation of the cosmic messengers may show up in observations thanks to the **amplification** offered by time delays or by threshold anomalies
- A number of '*anomalies*' could be '*explained*' by invoking LIV effects. However, LIV analyses need to be performed in a **consistent** way
- Better sensitivity to these effects requires specific improvements in the **instrumental capabilities** with respect to
 - *Energy and angular resolution* (correlation between messengers and source identification)
 - *Rejection properties* (sensitivity to low fluxes)
 - *Flavour and particle-antiparticle* determination for astrophysical neutrinos
 - Discrimination power on the *mass composition* for UHECRs

What's next?

- A **new generation** of instruments in the near future (CTA, LHAASO, KM3NeT, IceCubeGen-2, Askaryan detectors, LIGO and other GW detector upgrades) will deepen in the *new astrophysical windows* recently opened and improve the *sensitivity to the fluxes* of the cosmic messengers in their highest energy ranges
- These experimental advancements will have to be accompanied by **theoretical developments** in the *astrophysical modelling*, in the *methods of analysis* (such as a proper combination of samples corresponding to sources of different redshifts), in the *simulation codes* that model the propagation of messengers and the development of showers in the atmosphere to include QG effects, as well as in a *complete and consistent* formulation of the phenomenological consequences of *LIV* models
- **QGMM network site:** <https://sites.google.com/view/qgmm>

Thank you for your attention