

Testing Model Predictions of Depth of Air-Shower Maximum and Signals in Surface Detectors using Hybrid Data of the Pierre Auger Observatory

Jakub Vícha^a for the Pierre Auger Collaboration^b

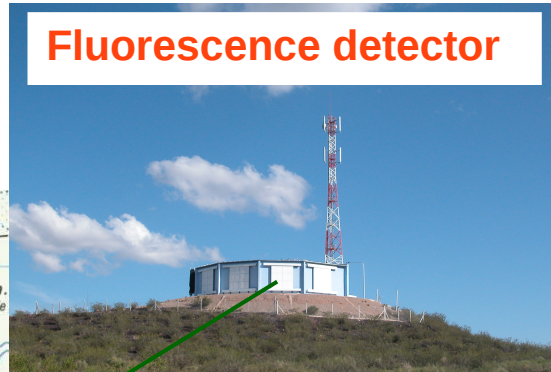
^a Institute of Physics of the Czech Academy of Sciences, Prague

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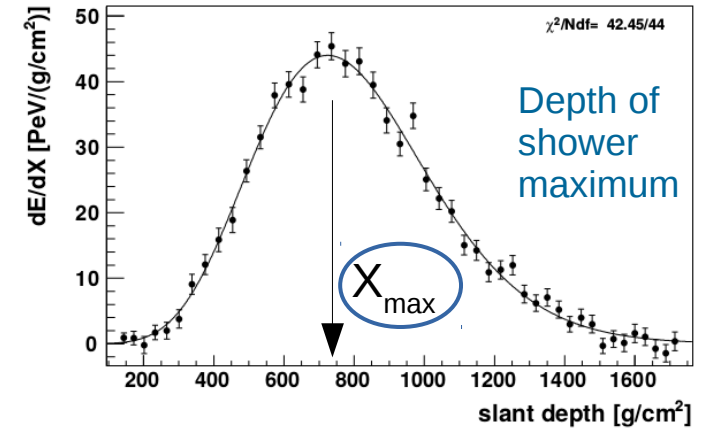
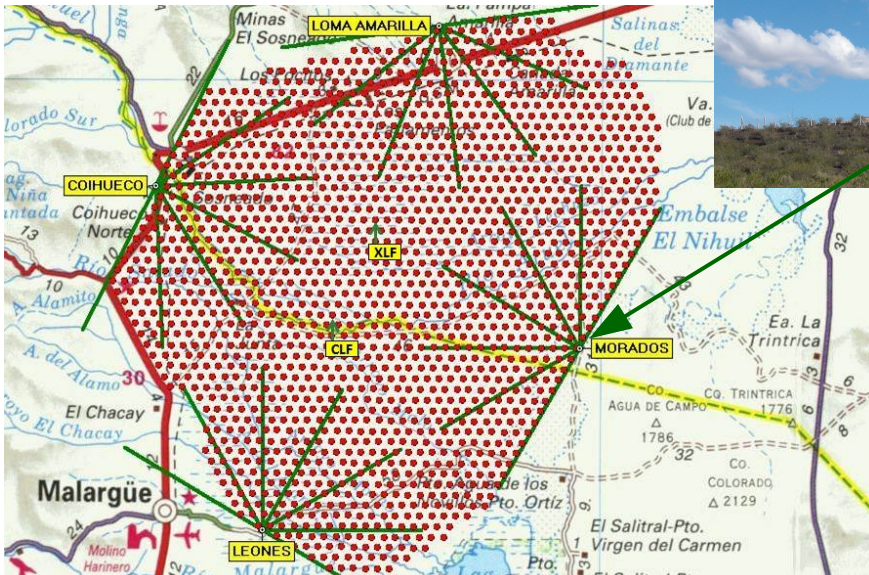
vicha@fzu.cz

Hybrid detection at the Pierre Auger Observatory

Fluorescence detector

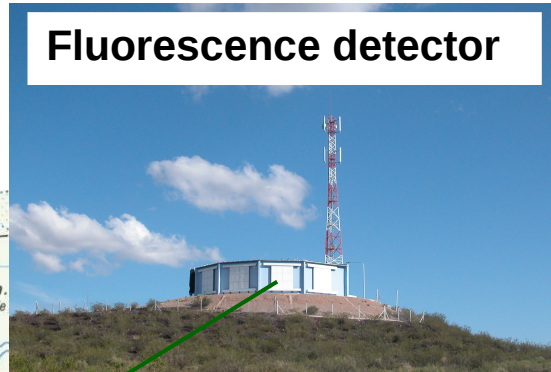


[Nucl. Instrum. Meth. A 798 (2015) 172]

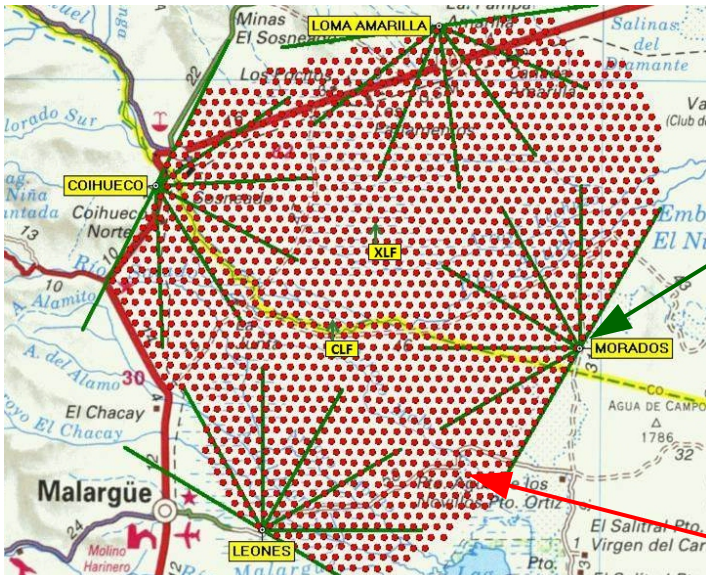


Hybrid detection at the Pierre Auger Observatory

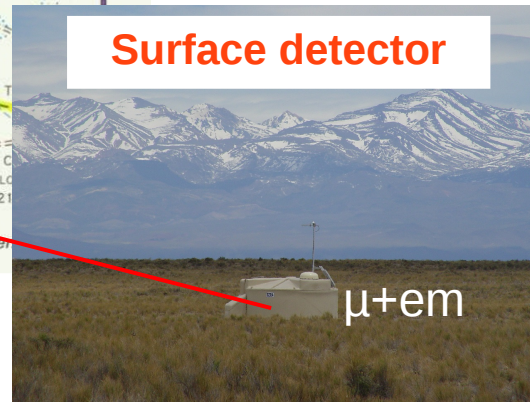
Fluorescence detector



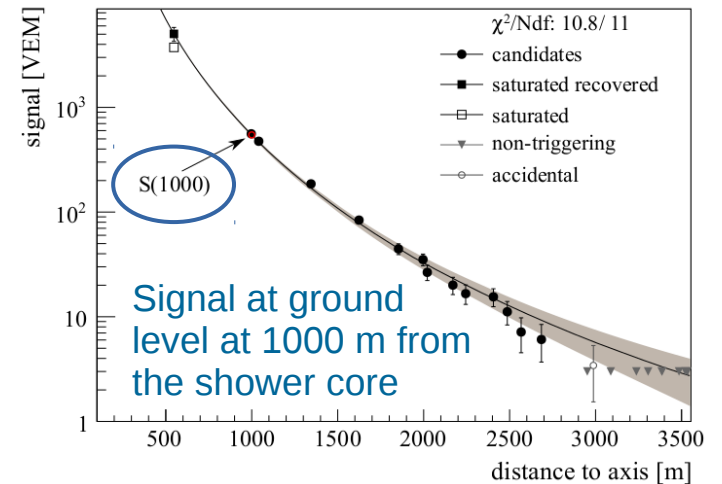
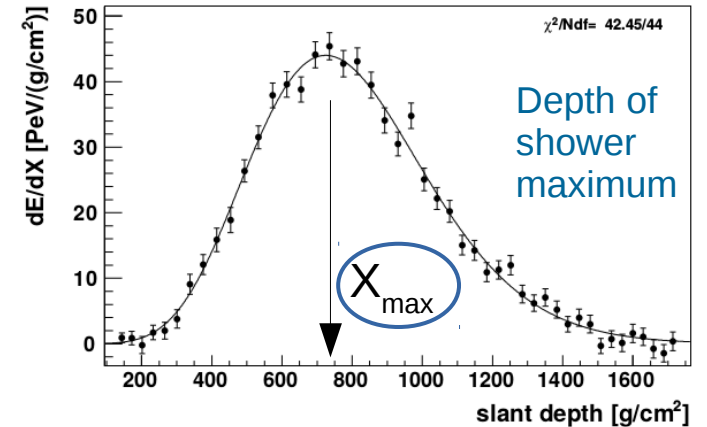
[Nucl. Instrum. Meth. A 798 (2015) 172]



Surface detector



$\mu+em$



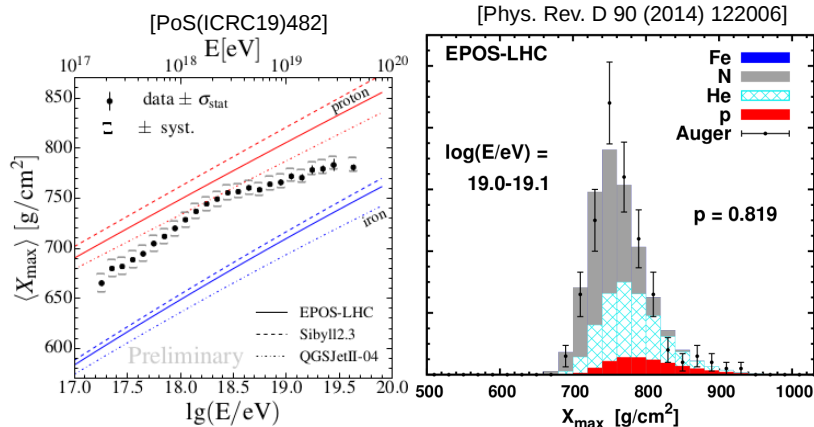
Mass composition & tests of hadronic interactions

Deficit of simulated muon signal: previous analyses in Auger

1) Mass composition is inferred from X_{\max}

measurements using the nominal X_{\max}

predictions of hadronic interaction (HI) models



Mass composition & tests of hadronic interactions

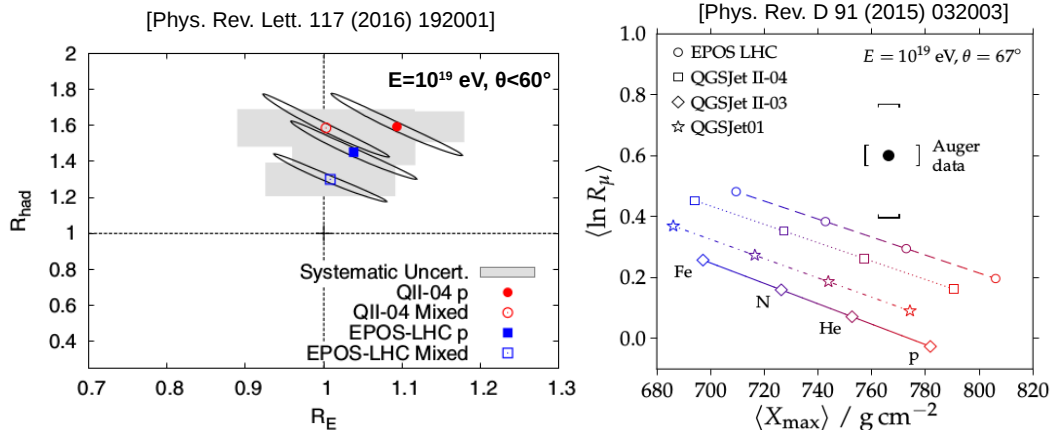
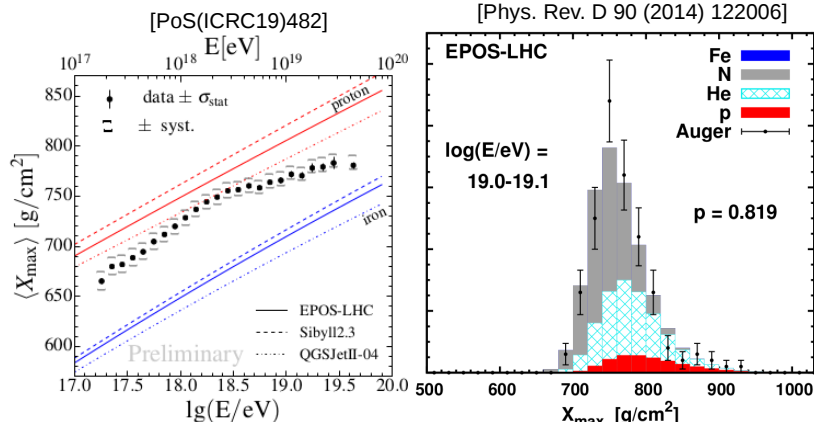
Deficit of simulated muon signal: previous analyses in Auger

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2) Discrepancy in predicted and measured ground signal is usually evaluated using the inferences on the mass composition from the X_{\max} analysis



Mass composition & tests of hadronic interactions

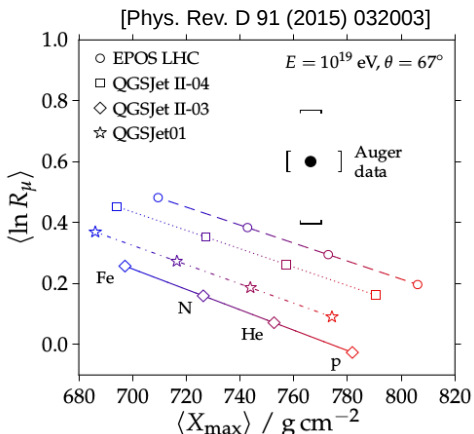
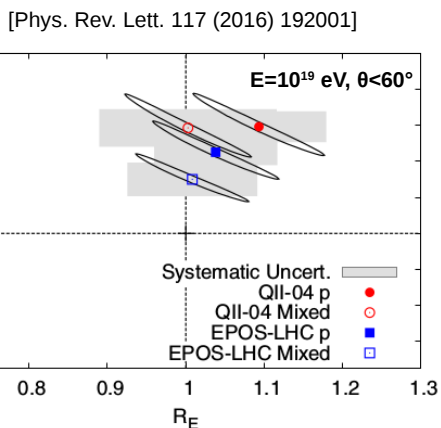
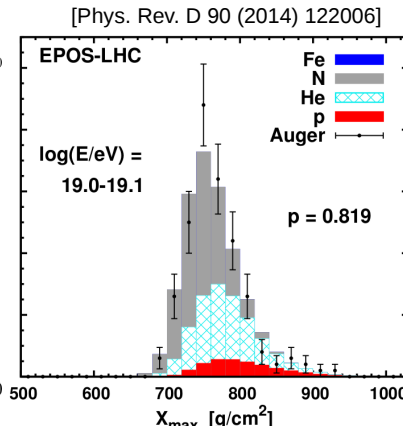
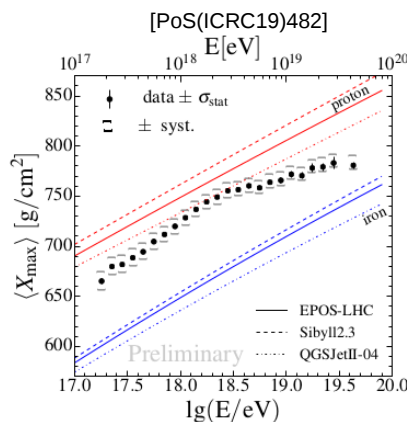
Deficit of simulated muon signal: previous analyses in Auger

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This work

Mass composition fit of observed $[X_{\max}, S(1000)](\theta)$ distributions with free adjustments of MC predictions **not only to hadronic signal but also to X_{\max}**

Motivations for adjustments of MC predictions

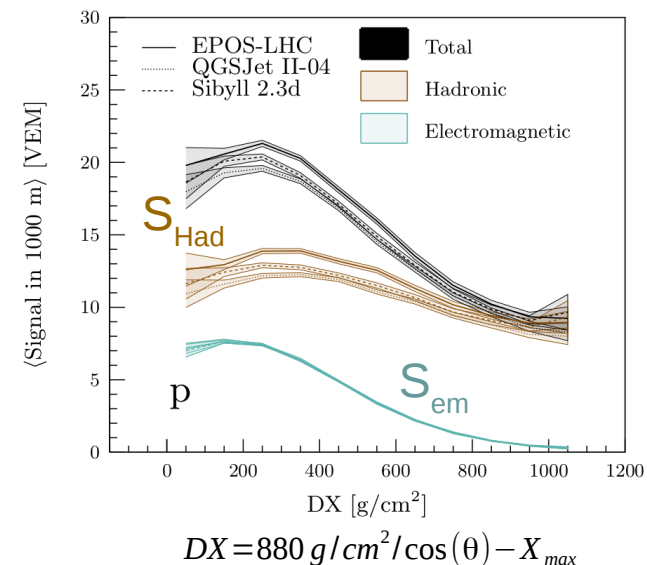
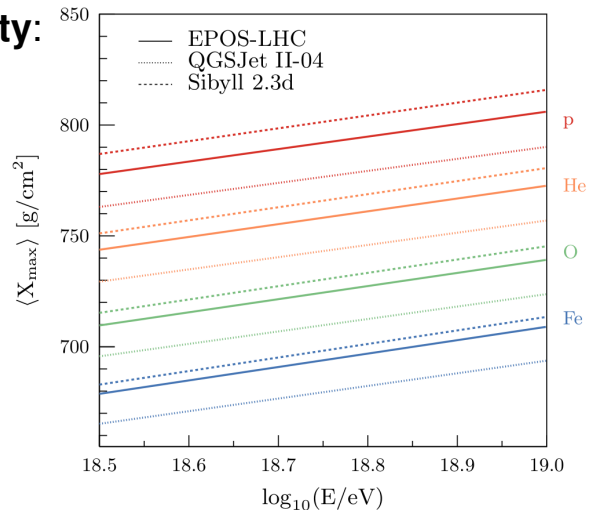
- Properties of **4-component shower universality**:

[Astropart. Phys. 87 (2017) 23, Astropart. Phys. 88 (2017) 46]

- $S(1000) = S_{\text{Had}} + S_{\text{em}}$
- S_{em} very universal

- **Main differences** between model predictions:

- Scale of $\langle X_{\text{max}} \rangle$ and $\langle S_{\text{Had}} \rangle$ are approx. primary and energy independent



ad-hoc adjustments

$$X_{\text{max}} \rightarrow X_{\text{max}} + \Delta X_{\text{max}}$$

$$S_{\text{Had}}(\theta) \rightarrow S_{\text{Had}}(\theta) \cdot R_{\text{Had}}$$

New !

Motivations for adjustments of MC predictions

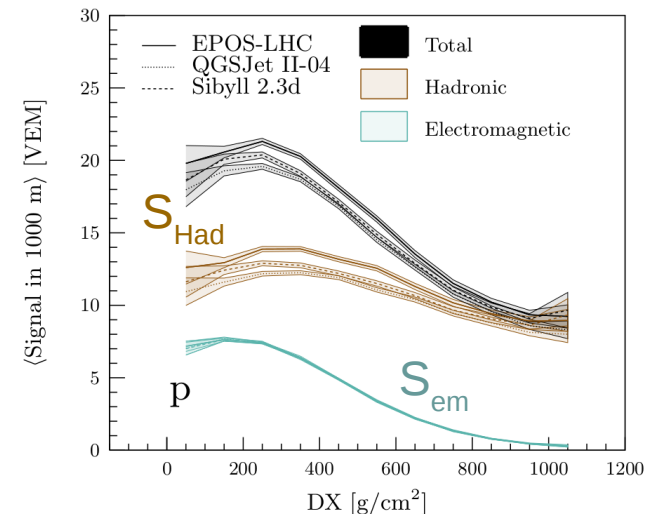
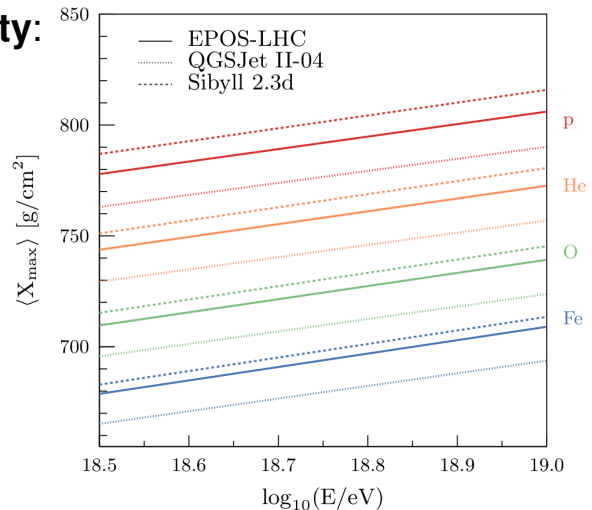
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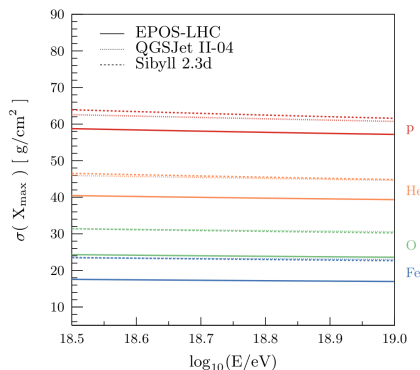
- Scale of $\langle X_{max} \rangle$ and $\langle S_{Had} \rangle$ are approx. primary and energy independent



$$DX = 880 \text{ g/cm}^2 / \cos(\theta) - X_{max}$$

- Ignored **model differences**:

- $R_{Had}(\theta)$ - see backup, PoS(ICRC2021)310
- fluctuations of X_{max} and $S(1000)$
- mass dependence of R_{Had} , ΔX_{max}
- etc.



ad-hoc adjustments

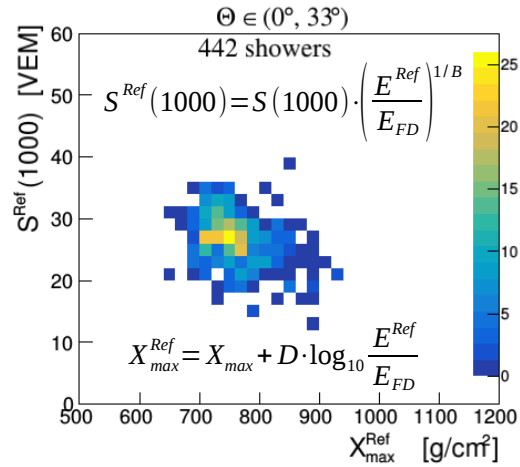
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New !

Global fit method

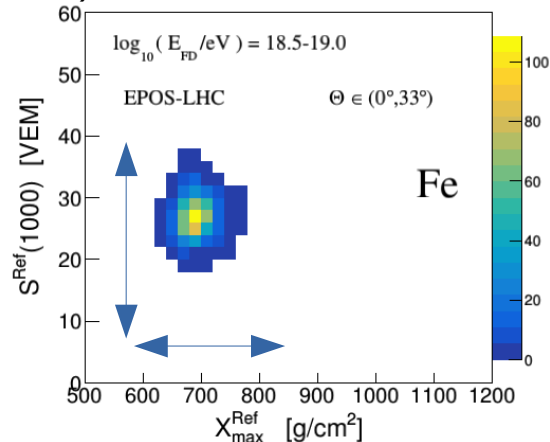
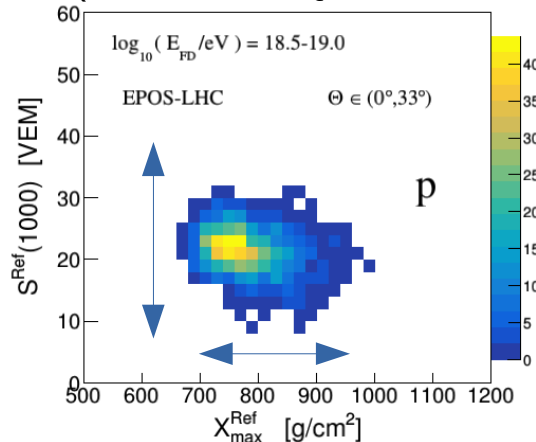
Auger data



Simultaneous likelihood ratio fit of **two-dimensional distributions** of X_{max} and $S(1000)$ in 5 zenith-angle bins with **MC templates** for combinations of four primary nuclei (p, He, O, Fe)

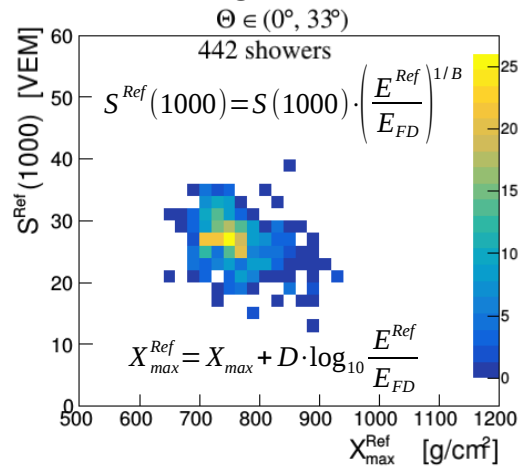
New !

MC templates: from ~15k showers per primary and model (EPOS-LHC, QGSJet II-04, Sibyll 2.3d)



Global fit method

Auger data

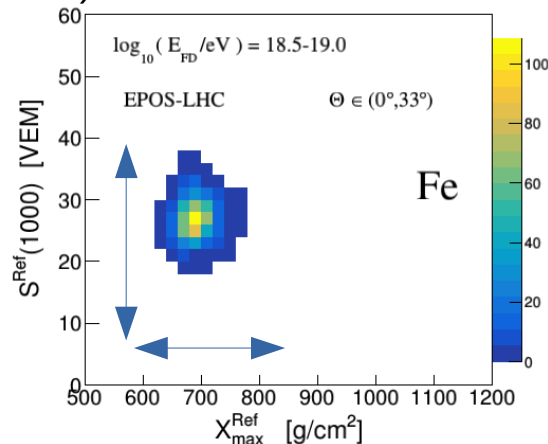
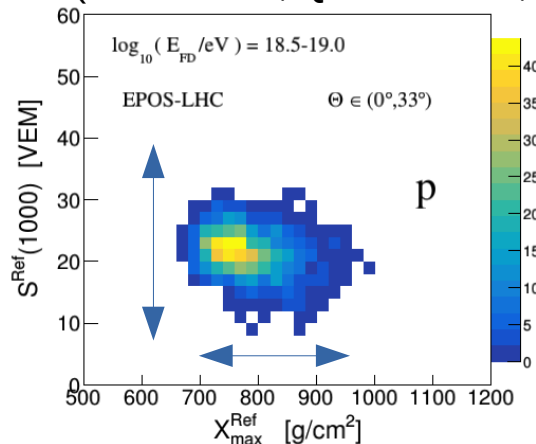


Simultaneous likelihood ratio fit of **two-dimensional distributions** of X_{max} and $S(1000)$ in 5 zenith-angle bins with **MC templates** for combinations of four primary nuclei (p, He, O, Fe)

New !

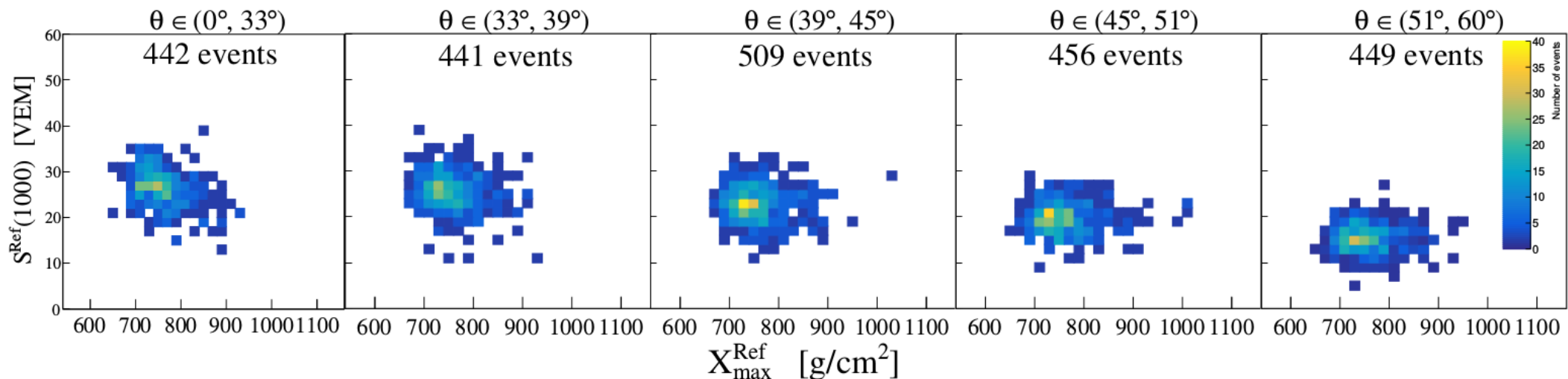
- **Freedom** in X_{max} (ΔX_{max}) and $S(1000)$ (R_{Had}) and **primary fractions**
- Change of S_{Had} and S_{em} due to ΔX_{max} incorporated
- **Degeneracy** between mass composition and ΔX_{max} reduced due to the nearly model-independent correlation between $S(1000)$ and X_{max} [Phys. Lett. B 762 (2016) 288]

MC templates: from ~15k showers per primary and model (EPOS-LHC, QGSJet II-04, Sibyll 2.3d)



Measured data

2297 high-quality showers for $\log_{10}(E_{\text{FD}} [\text{eV}]) = 18.5\text{-}19.0$, $\theta < 60^\circ$



Event selection according to [Phys. Rev. D 90 (2014) 122005, PoS(ICRC19)482] and [Phys. Rev. D 102 (2020) 062005]

Progressive adjustments to MC templates

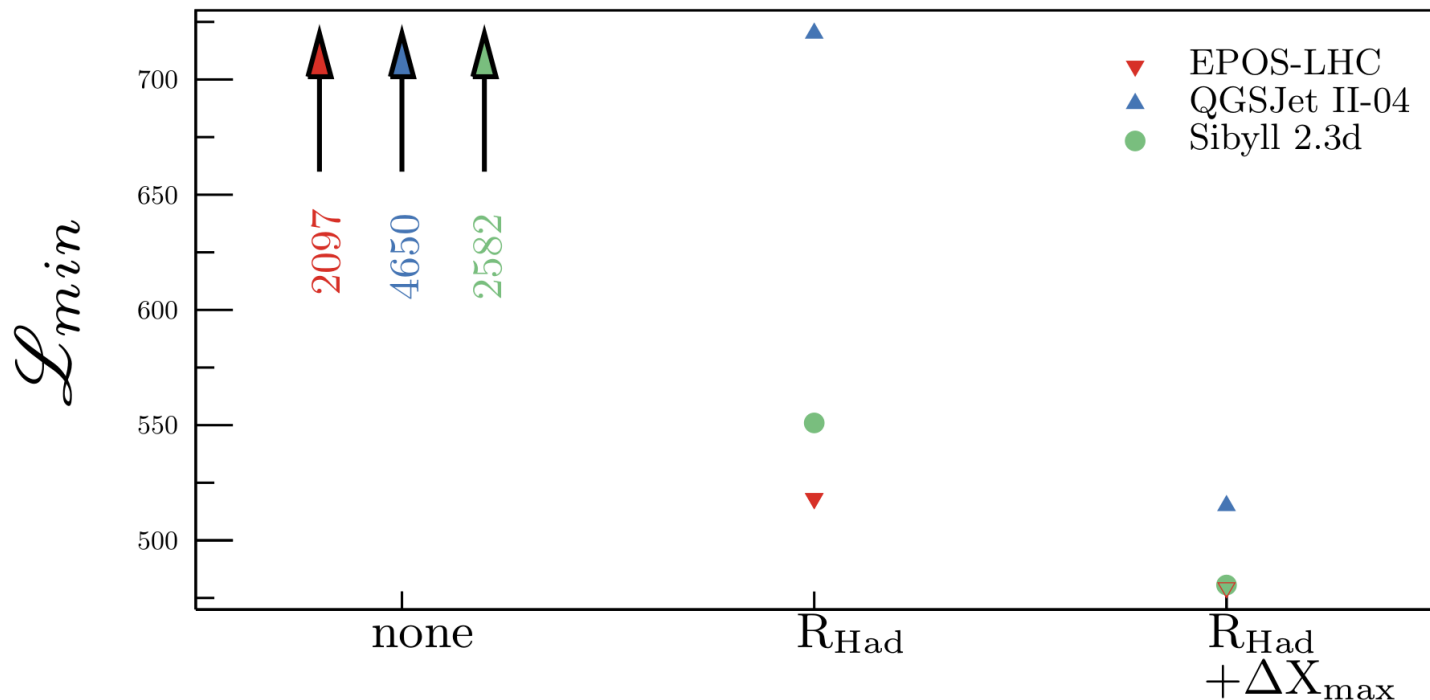
1) NO adjustment at all



2) R_{Had}



3) $R_{\text{Had}} + \Delta X_{\text{max}}$

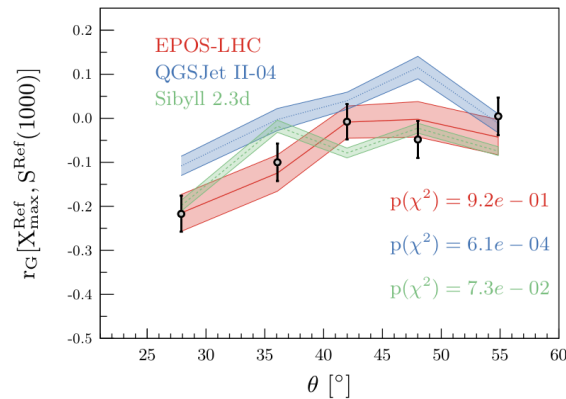
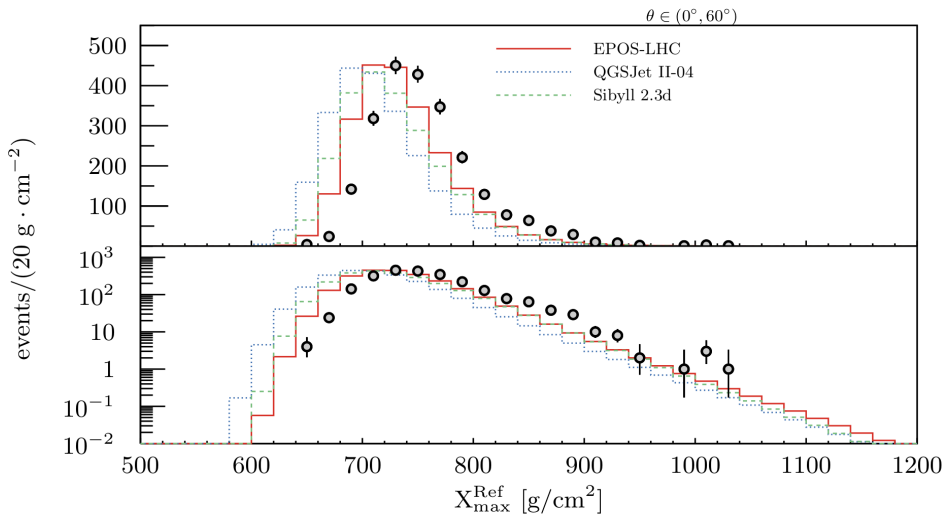


$$\forall n_{jz} > 0: \mathcal{L} = \sum_z^{\theta \text{ bins}} \sum_j^{2D \text{ bins}} \left(C_{jz} - n_{jz} + n_{jz} \cdot \ln \frac{n_{jz}}{C_{jz}} \right)$$

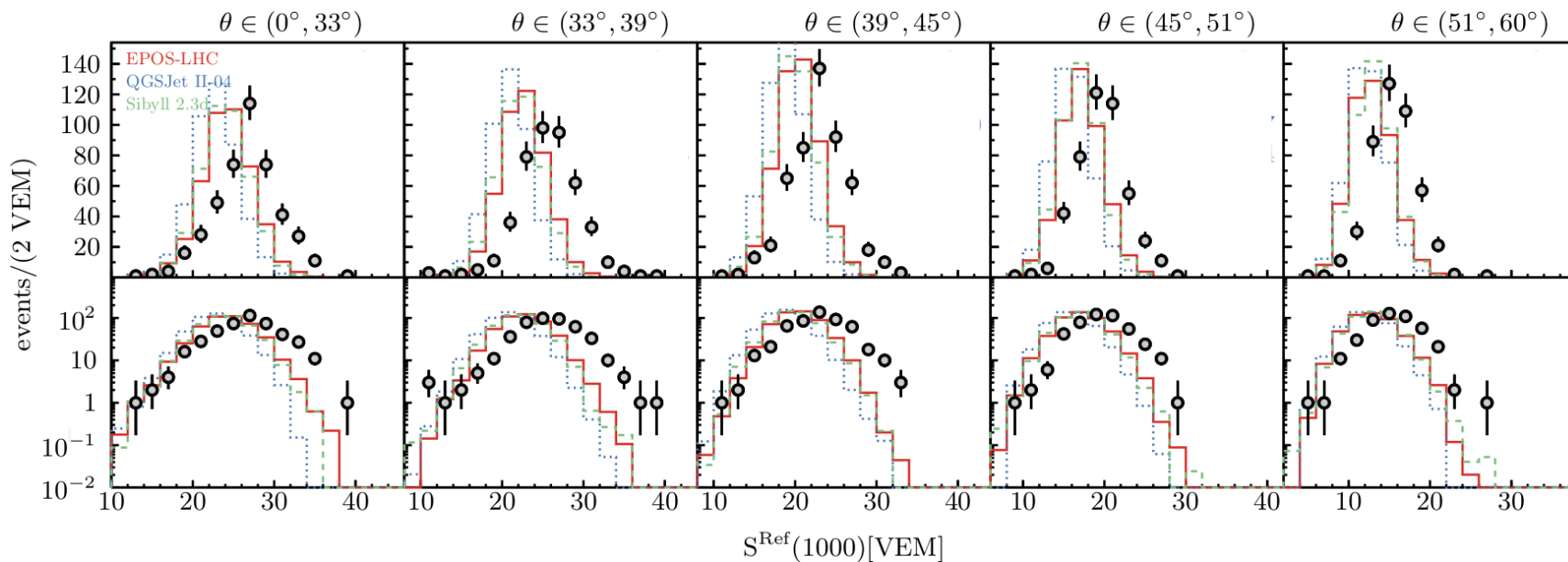
$$\forall n_{jz} = 0: \mathcal{L} = \sum_z \sum_j C_{jz},$$

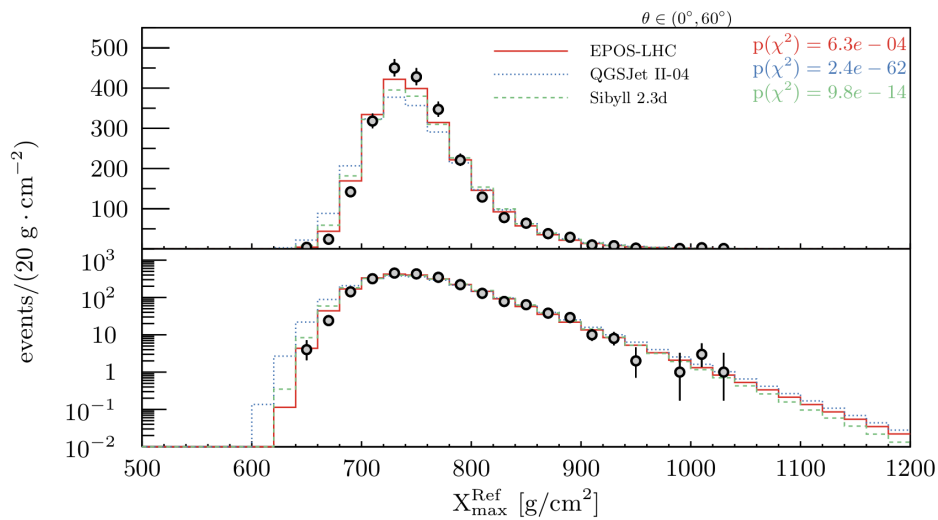
n_{jz} - measured number of events
 C_{jz} - predicted number of events

1) NO adjustments

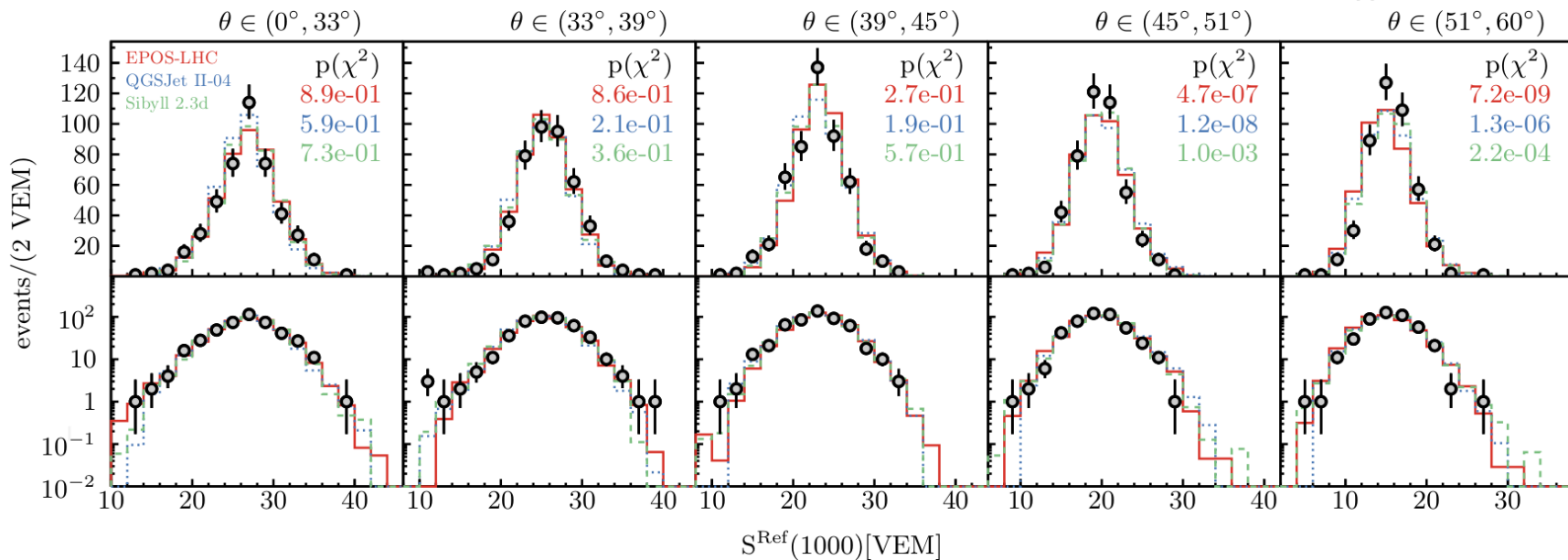
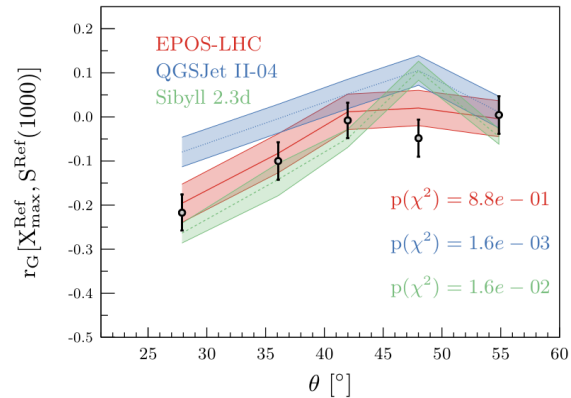


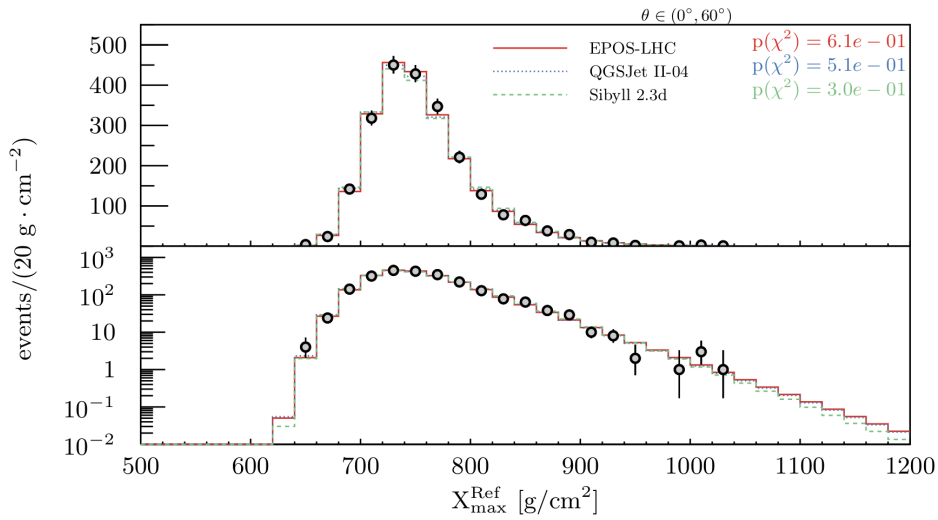
Gideon-Hollister correlation coefficient
[J. Am. Stat. Assoc. 82 (1987) 656]



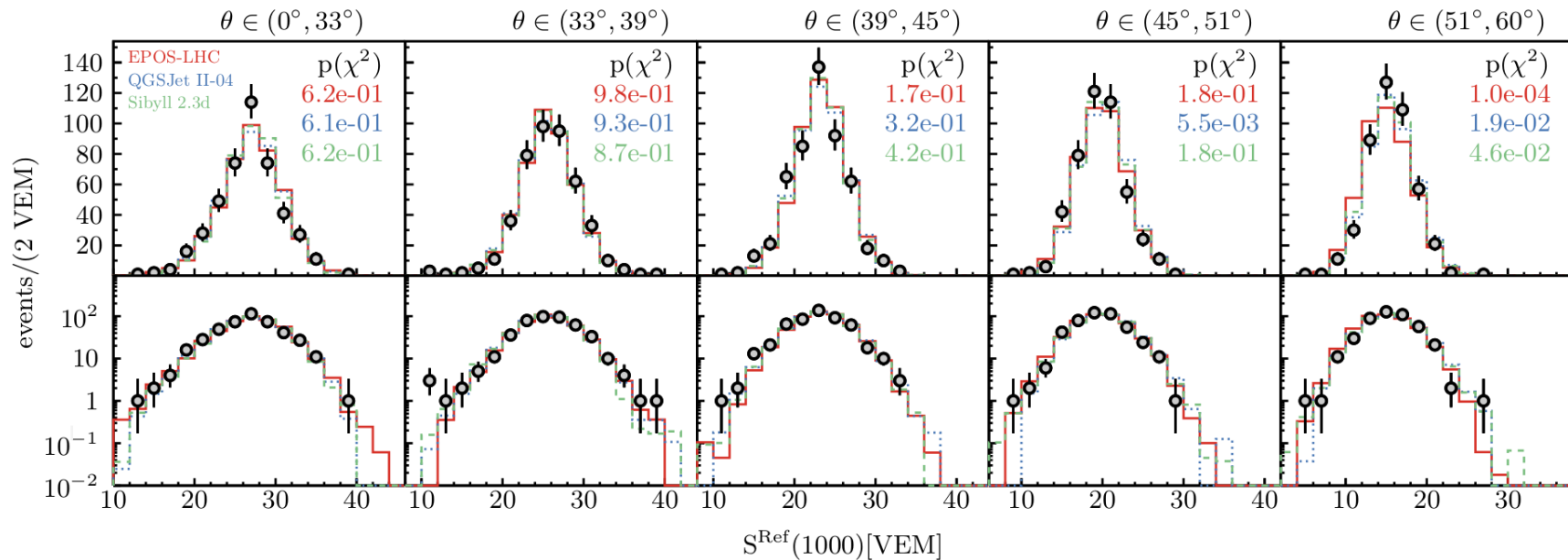
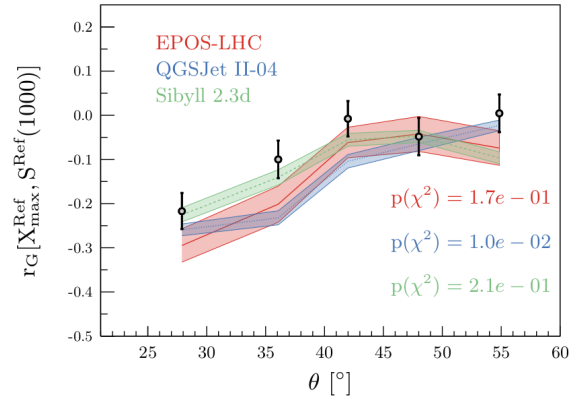


2) R_{Had}





3) $R_{\text{Had}} + \Delta X_{\text{max}}$



Systematic Uncertainties

- Experimental
 - 1) Energy scale $\pm 14\%$
 - 2) X_{\max} measurement $+8, -9 \text{ g/cm}^2$
 - 3) S(1000) measurement $\pm 5\%$
- Method
 - 4) Biases from MC-MC tests for each model

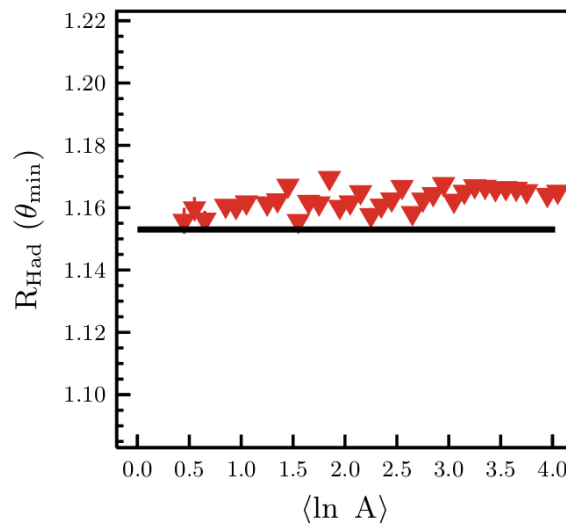
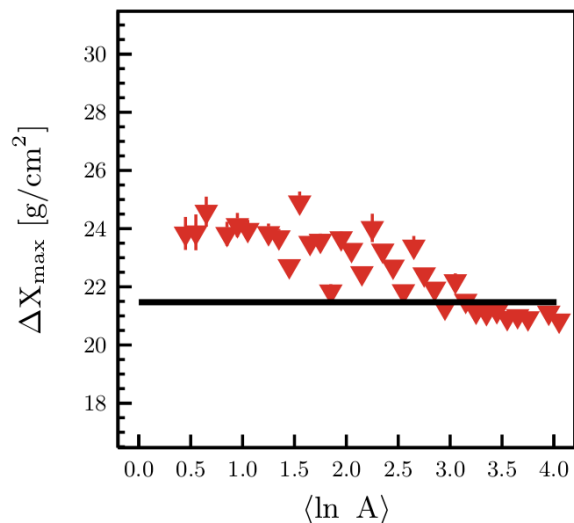
All four contributions
summed in quadrature

Systematic Uncertainties

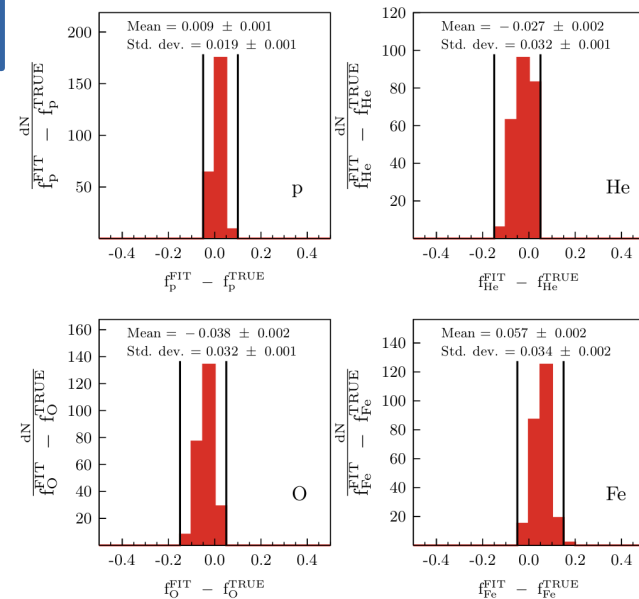
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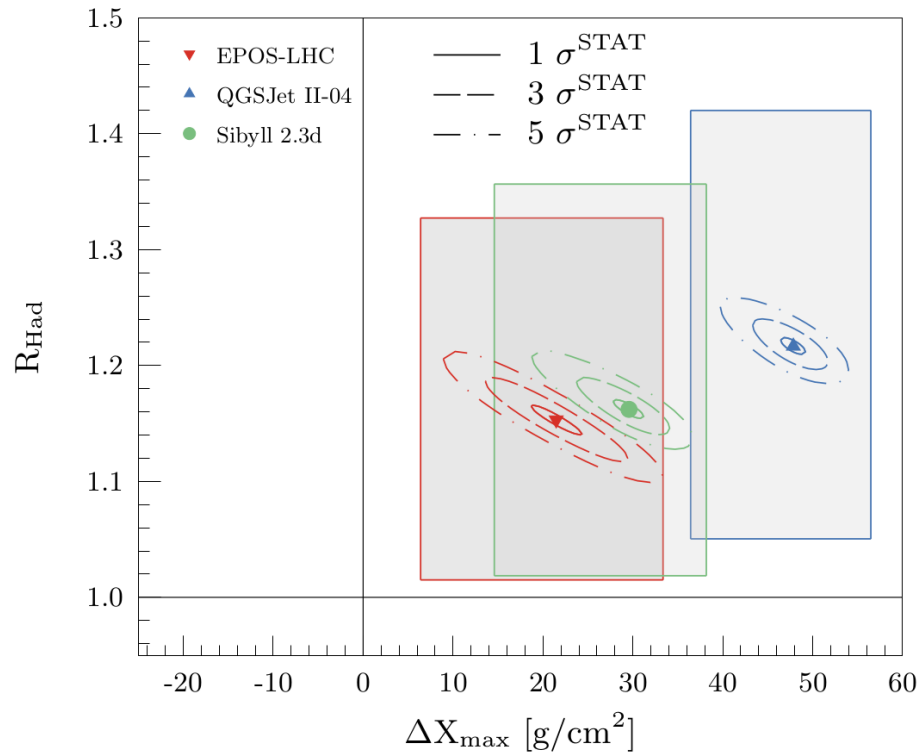
Method works within $\sim 5 \text{ g/cm}^2$ for ΔX_{\max} and few percent for R_{Had}



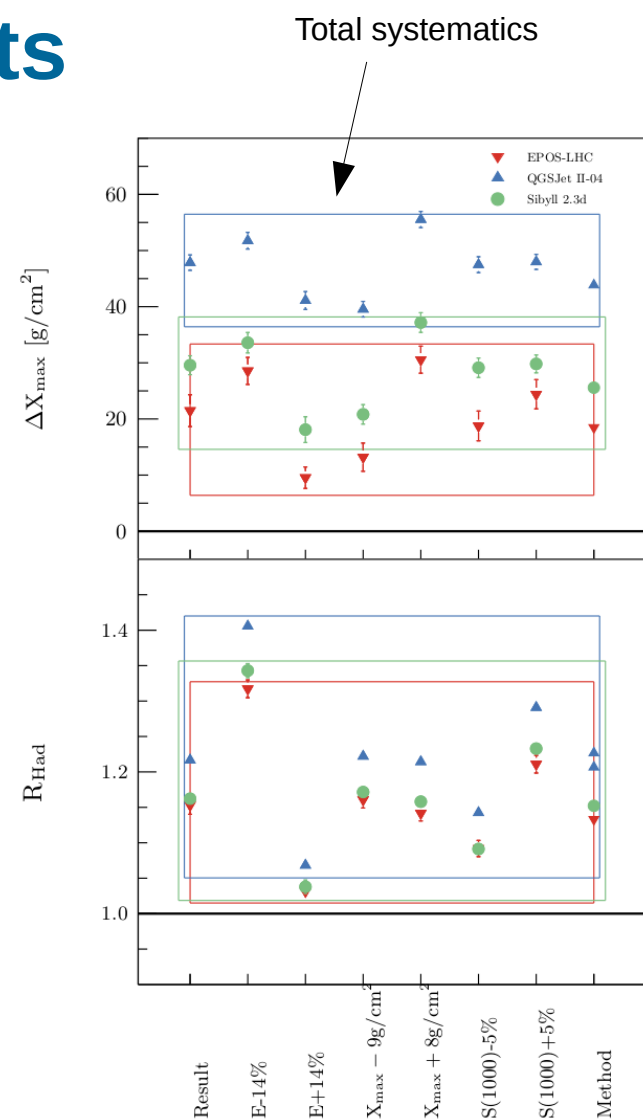
MC-MC tests using EPOS-LHC with artificial changes in $\Delta X_{\max} \approx 22 \text{ g/cm}^2$, $R_{\text{Had}} \approx 1.15$



Fitted MC adjustments



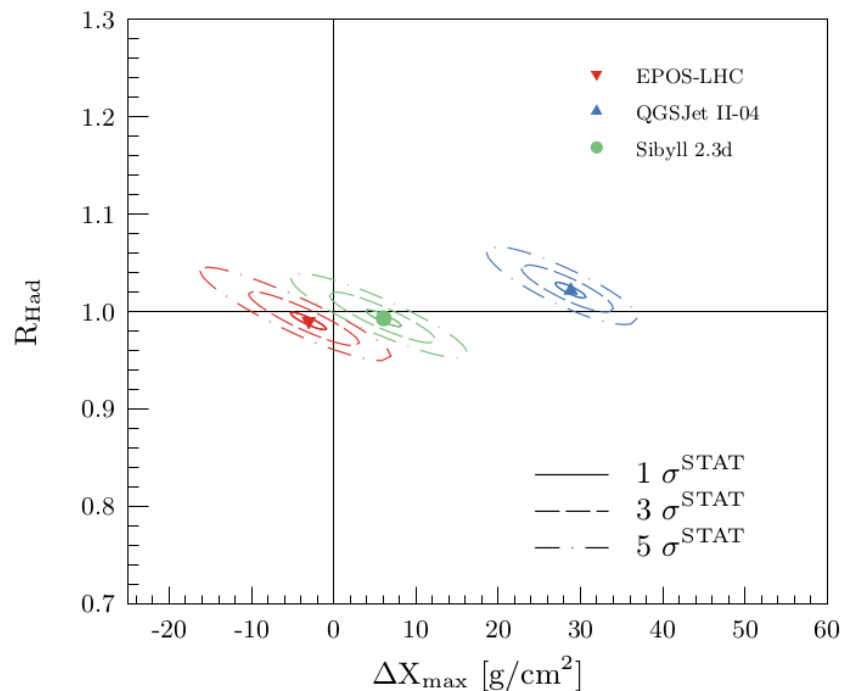
Deeper predicted $\langle X_{\text{max}} \rangle$
→ alleviated “muon puzzle”



Significance of MC adjustments

Most favorable direction for models in combinations of $1\sigma^{\text{SYS}}$ experimental systematics:

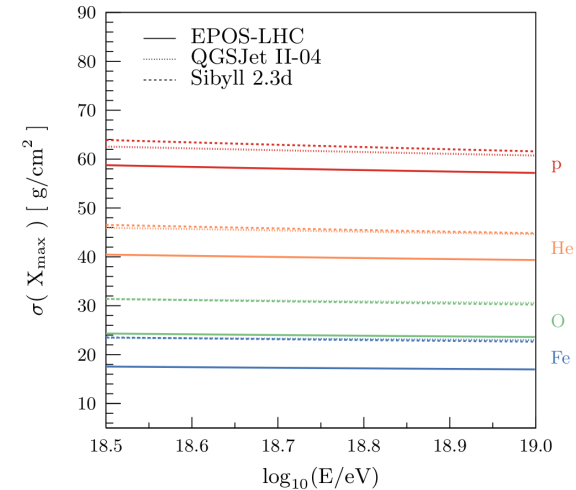
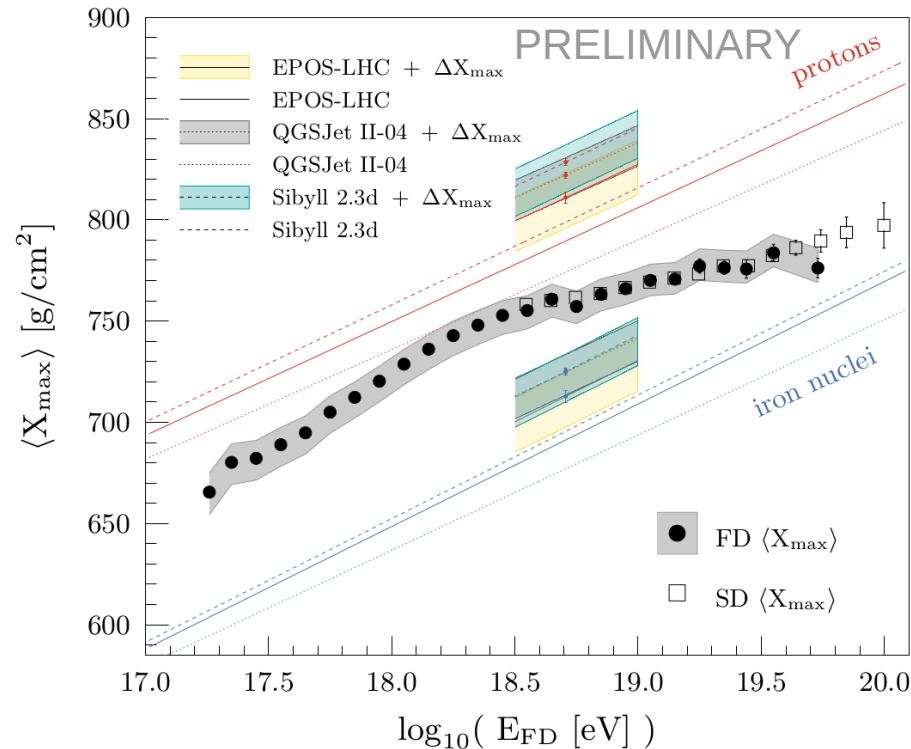
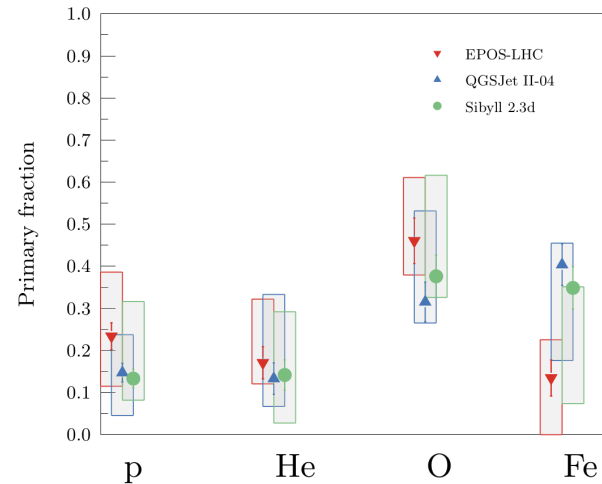
Energy + 14% & X_{max} - 9 g/cm² & S(1000) - 5%



The discrepancy with the data $\approx 5\sigma^{\text{STAT}}$

Less model-dependent mass composition

$\langle X_{\max} \rangle$ MC scale found lower at **energy $10^{18.5-19}$ eV** by ~ 10 g/cm² for EPOS-LHC mainly due to lower $\sigma(X_{\max})$; checked by artificially smeared X_{\max}



Summary

- Two-dimensional distributions of $[X_{\max}, S(1000)]$ for energies $10^{18.5} - 10^{19.0}$ eV and zenith angles $< 60^\circ$, measured by the Pierre Auger Observatory, were fitted allowing for ad-hoc adjustments of the simulated X_{\max} and hadronic signal for EPOS-LHC, Sibyll 2.3d and QGSJet II-04
- For all three hadronic interaction models, the **improved description of the data** is achieved, **if in the simulations:**
 - X_{\max} is shifted towards deeper values → Heavier mass composition !
 - Hadronic signal is increased by $\sim 15\text{-}25\%$ → Alleviation of the muon puzzle !

Caveat: other differences in model predictions under study (shower-to-shower fluctuations etc.)
- The statistical significance of the adjustments is **greater than $\sim 5\sigma^{\text{STAT}}$** even for the combination of experimental systematic shifts within $1\sigma^{\text{SYS}}$ that are the most favorable for the models

Stay tuned: paper in preparation [PoS(ICRC2021)310]

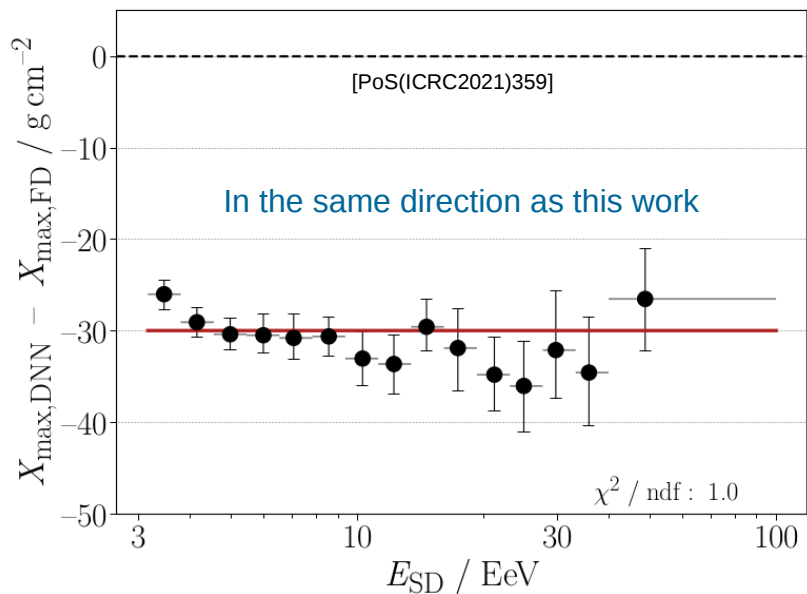
Backup slides

$$N \propto N_0 \cdot E_0^\alpha \quad \kappa \propto \kappa_0 \cdot E_0^{-\omega}$$

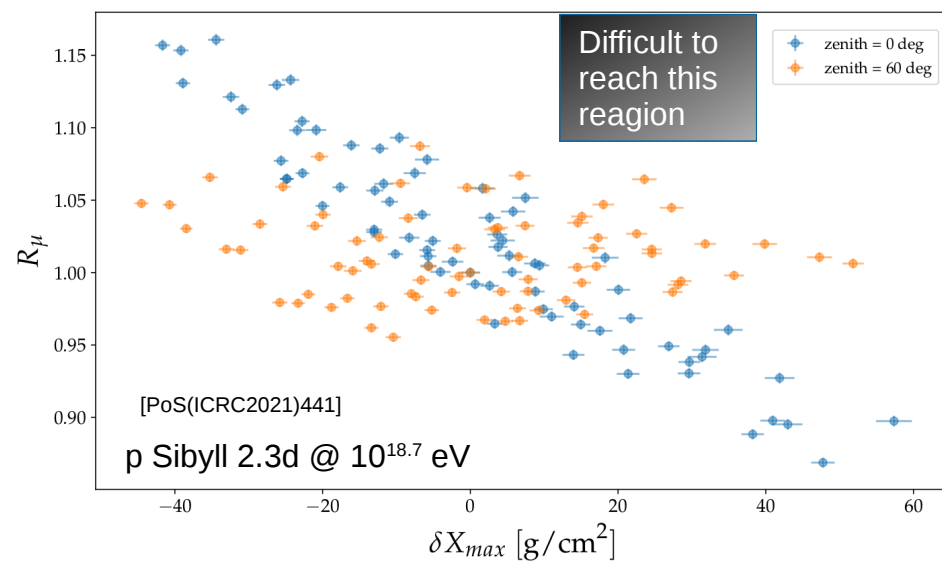
Matthews [Astropart. Phys. 22 (2005) 387] model: Ad-hoc change of multiplicity (N_δ) or elasticity (κ_δ) would **change X_{\max} independently on primary and energy**

$$X_{\max}^A = X_1^A + X_0 \ln \frac{\kappa E_0}{A \cdot 2N \xi_c^\pi} = X_1^A + (1 - \alpha - \omega) \cdot \left(X_0 \ln \frac{E_0}{A \cdot \xi_c^\pi} \right) + X_0 \cdot (\ln \kappa_0 - \ln N_0)$$

DNN method applied to Auger data from EPOS-LHC simulations

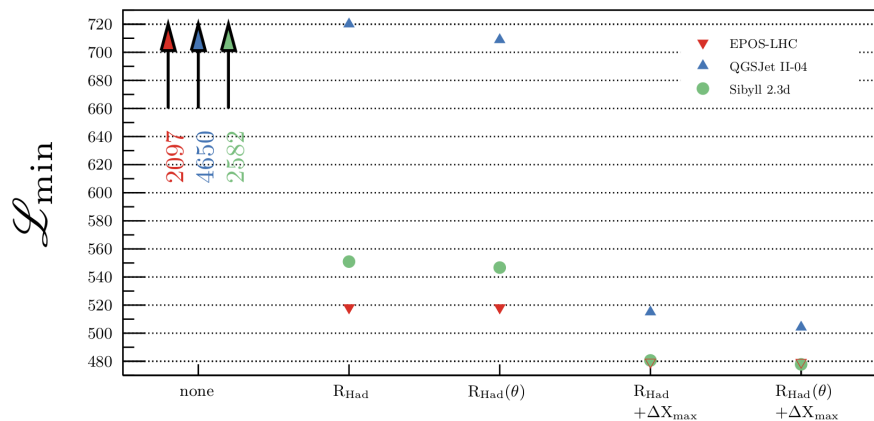
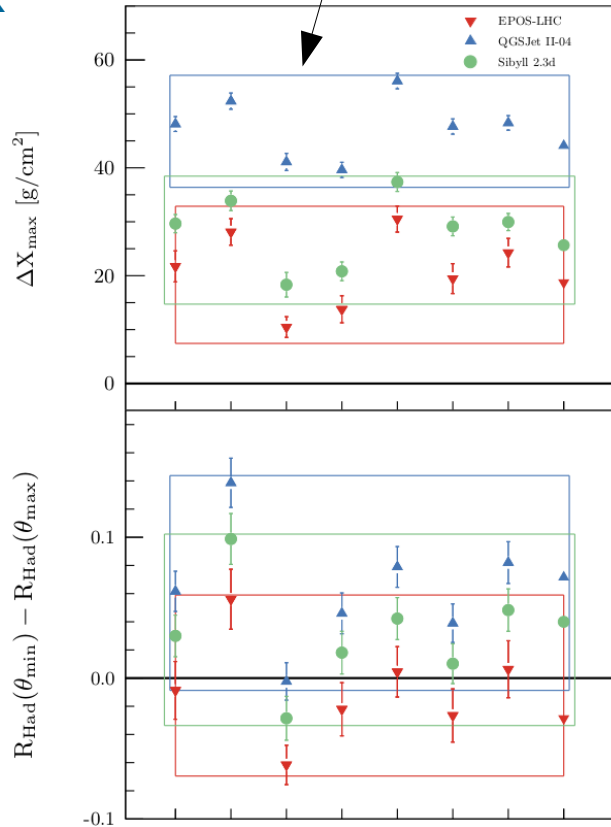
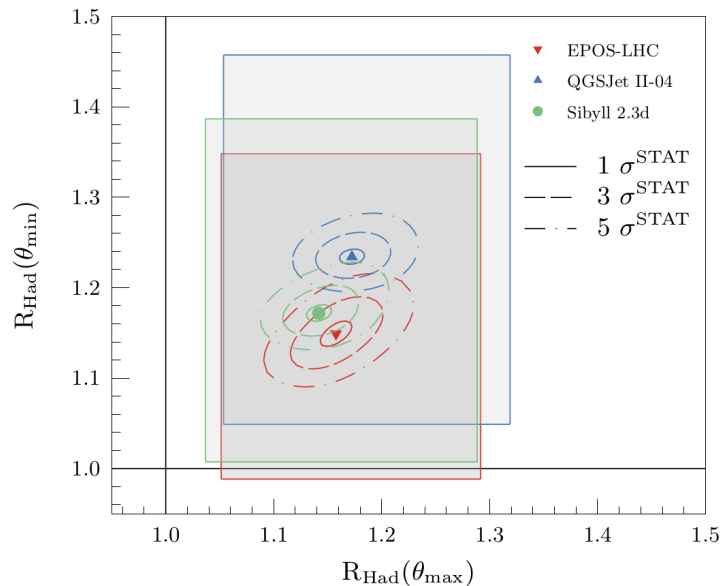
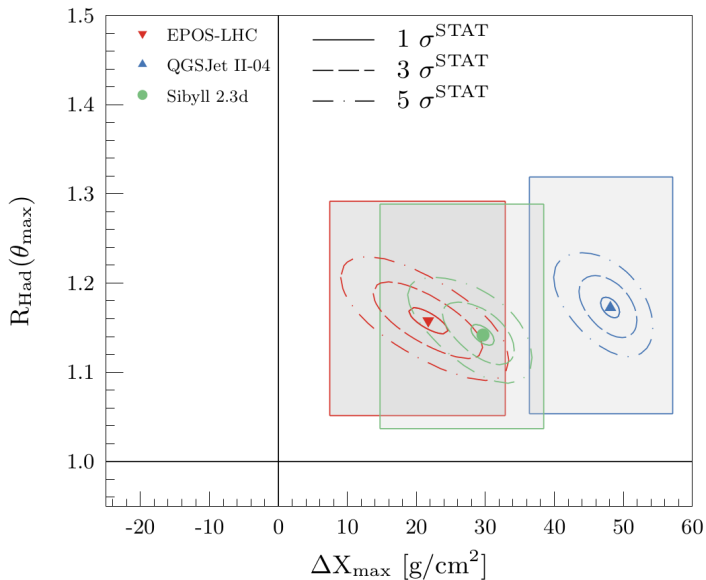


Conservative estimation of possibilities using combination of changes in cross-section, elasticity, multiplicity



Fitting $R_{\text{Had}}(\theta) + \Delta X_{\text{max}}$

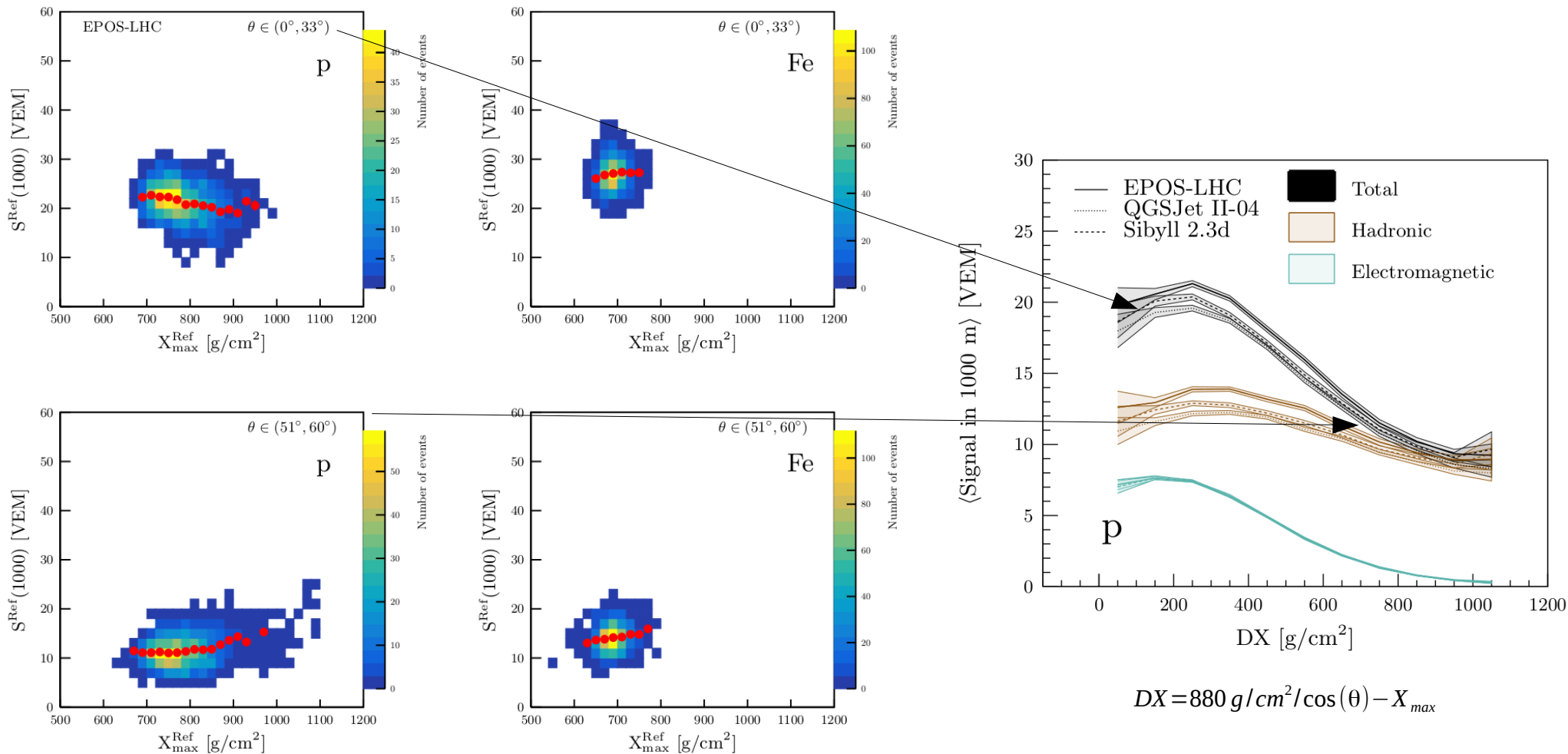
Total systematics



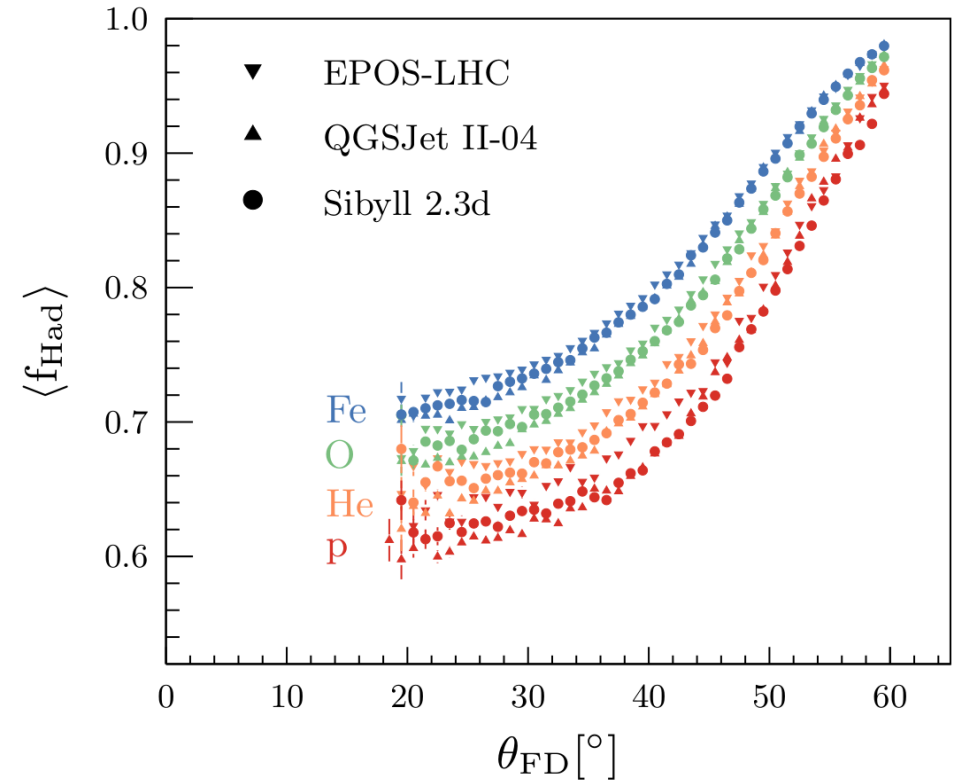
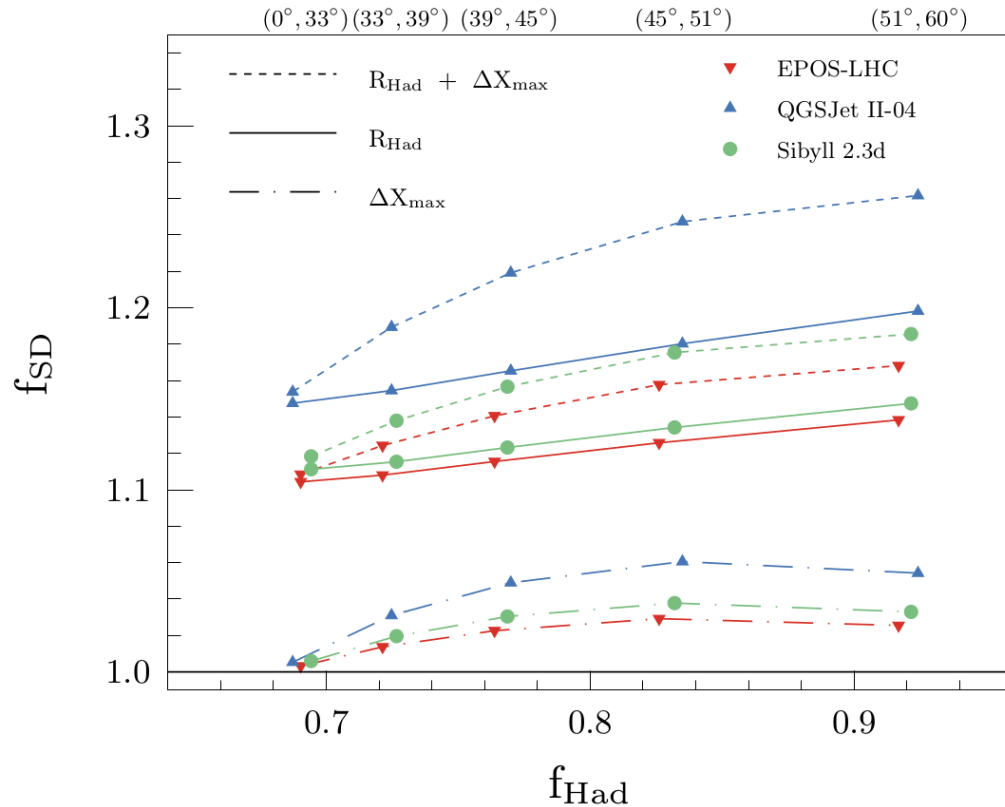
R_{Had} attenuation
is correlated
with the energy
scale

Result
E-14%
E+14%
 $X_{\text{max}} - 9\text{g/cm}^2$
 $X_{\text{max}} + 8\text{g/cm}^2$
S(1000)-5%
S(1000)+5%
Method

θ -dependent correlation between X_{\max} and ground signal



Contributions to rescaling of ground signal



$$E^{Ref} = 10^{18.7} \text{ eV}$$

$$B = 1.031$$

$$D = 58 \text{ g/cm}^2$$

Fitting procedure

$$\forall n_{jz} > 0: \mathcal{L} = \sum_z \sum_j \left(C_{jz} - n_{jz} + n_{jz} \cdot \ln \frac{n_{jz}}{C_{jz}} \right), \quad \forall n_{jz} = 0: \mathcal{L} = \sum_z \sum_j C_{jz}$$

zenith bins
MC
data
2D bins
↓
↓

$$S(1000)(\theta) \cdot \left(\frac{E^{Ref}}{E_{FD}} \right)^{1/B} \cdot f_{SD}(\theta) = R_{Had}(\theta) \cdot g_{Had}(\theta, \Delta X_{max}, R_{Had}(\theta)) \cdot S_{Had}(\theta) \cdot \left(\frac{R_E \cdot E^{Ref}}{E_{FD}} \right)^\beta + R_{em} \cdot g_{em}(\theta, \Delta X_{max}) S_{em}(\theta) \cdot \left(\frac{R_E \cdot E^{Ref}}{E_{FD}} \right)$$

$$f_{SD}(\theta) = R_{Had}(\theta) \cdot R_E^\beta \cdot \left(\frac{E^{Ref}}{E_{FD}} \right)^{\beta-1/B} \cdot g_{Had}(\theta, \Delta X_{max}, R_{Had}(\theta)) \cdot f_{Had}(\theta) + R_{em} \cdot R_E \cdot \left(\frac{E^{Ref}}{E_{FD}} \right)^{1-1/B} \cdot g_{em}(\theta, \Delta X_{max}) \cdot (1 - f_{Had}(\theta)), \quad f_{Had}(\theta) = \frac{S_{Had}(\theta)}{S(1000)(\theta)}$$

$$\Rightarrow \langle f_{SD} \rangle_z = R_{Had}^z \cdot R_E^\beta \cdot \left(\frac{E^{Ref}}{\langle E_{FD}^{\beta-1/B} \rangle_z} \right) \cdot g_{Had}^z(\Delta X_{max}, R_{Had}^z) \cdot \langle f_{Had} \rangle_z + R_{em} \cdot R_E \cdot \left(\frac{E^{Ref}}{\langle E_{FD}^{1-1/B} \rangle_z} \right) \cdot g_{em}^z(\Delta X_{max}) \cdot (1 - \langle f_{Had} \rangle_z)$$

$$R_{em} = R_E = 1$$

$$\Rightarrow \langle f_{SD} \rangle_z = R_{Had}^z \cdot \left(\frac{E^{Ref}}{\langle E_{FD}^{\beta-1/B} \rangle_z} \right) \cdot g_{Had}^z(\Delta X_{max}, R_{Had}^z) \cdot \langle f_{Had} \rangle_z + \left(\frac{E^{Ref}}{\langle E_{FD}^{1-1/B} \rangle_z} \right) \cdot g_{em}^z(\Delta X_{max}) \cdot (1 - \langle f_{Had} \rangle_z)$$

$$X_{max}^{Ref} + \Delta X_{max}$$

$$R_{Had}(\theta) = R_{Had}(\theta_{min}) + (R_{Had}(\theta_{max}) - R_{Had}(\theta_{min})) \cdot \frac{DX(\theta) - DX(\theta_{min})}{DX(\theta_{max}) - DX(\theta_{min})}$$