



CYGNO collaboration meeting 2021
Gran Sasso Science Institute, L'Aquila, Italy

Detector simulation and saturation



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for the “digitization group” (Davide, Giulia, Pietro, ...)

20-21 December 2021

- Detector response
 - Ionization and drift
 - Gain fluctuations
 - Diffusion and smearing
 - Electrons to photons conversion
 - Photons collection
- Saturation effect
- Code improvement
- Data/MC comparison
- Next steps

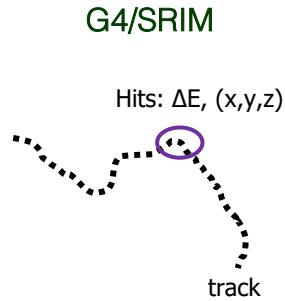
Detector simulation

The simulation of an event in the detector, is done in two parts:

SIMULATION of a primary particle interacting in the gas volume: Geant4 for electron recoils (ER), SRIM for nuclear recoils (NR).

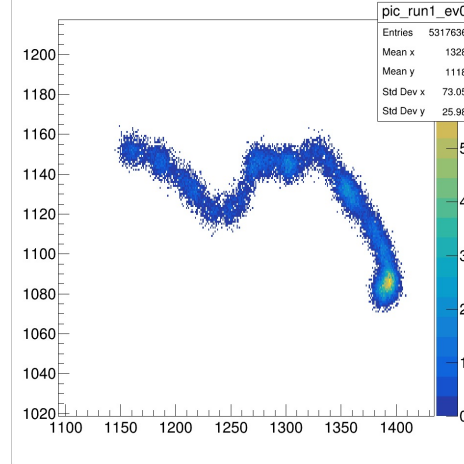
- Along the track:
 - hits energy deposition ΔE
 - hits position coordinates x, y, z

DIGITIZATION: Simulation (modelling) of the detector response returning a 2D image as for real data

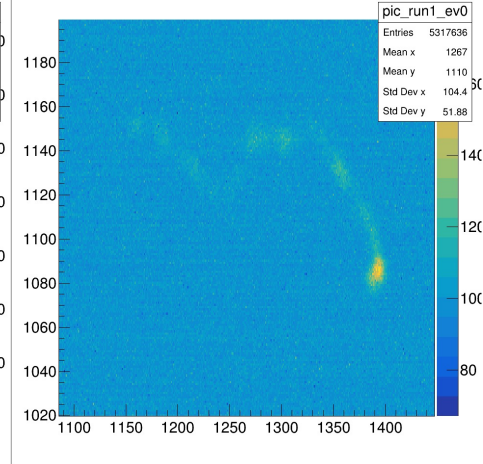


DIGITIZATION

Detector response



Detector response + noise



Takes the output of Geant4/SRIM as an input, and returns a “2D image”:
a 2D histogram where each cell contains the number of photons in a CMOS pixel

- The following processes are considered:
 - Ionization
 - Drift of the ionization electrons towards the 3-GEM stack
 - Multiplication in the 3-GEM stack
 - Production of photons in the multiplication process
 - Saturation effect
 - Photon collection on the sensor
 - Smearing of the impact position
- The digitization is a Python code still under development/optimization.
 - Code: <https://github.com/CYGNUS-RD/digitization/>
 - Wiki documentation: <https://github.com/CYGNUS-RD/WIKI-documentation/wiki/Digitization>

1. For each G4/SRIM hit, a mean number of ionization electrons are produced:

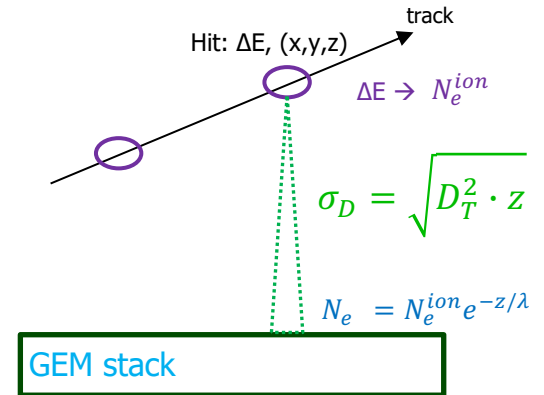
$$\bar{N}_e^{ion} = \Delta E / W_i \quad (W_i = 46.2 \text{ eV/pair in He/CF}_4 \text{ 60/40})$$

2. The actual number N_e^{ion} of ionization electrons is obtained from a Poisson distribution with mean $= \bar{N}_e^{ion}$

3. Ionization electrons diffuse in the drift region on the x-y plane of the GEM stack: $\sigma_D^2 = D_T^2 \cdot z$

4. Ionization electrons are partially absorbed in the gas:

$$N_e = N_e^{ion} e^{-z/\lambda} \quad \text{where } z \text{ is the distance from the GEM stack}$$



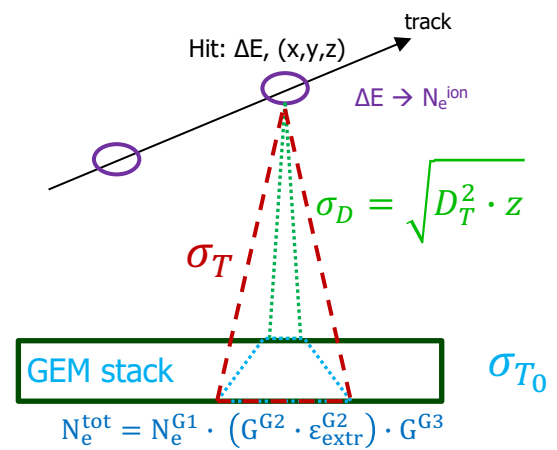
Gain and fluctuations

Ionization electrons arrive at the GEM stack; gain and efficiencies of the 3 GEM foils should be considered.

- gain fluctuations in the first foil only are relevant:
- For each ionization electron $\rightarrow N_e^{G1,k}$ multiplication electrons in the first GEM ($k=1, N_e^{ion}$) are extracted using an exponential distribution with **mean** = G^{G1} (G^{G1} is the gain of the first GEM foil)
- Total number of multiplication electron for the first foil:

$$N_e^{G1} = \sum N_e^{G1,k} \cdot \epsilon_{extr}^{G1} \quad (\epsilon_{extr}^{G1}: \text{extraction efficiency for the first GEM})$$

- The total number of multiplication electrons computed considering the gain of other two GEM foils and the extraction efficiency of the second foil: $N_e^{tot} = N_e^{G1} \cdot (G^{G2} \cdot \epsilon_{extr}^{G2}) \cdot G^{G3}$



- Electrons diffuse also in the GEM stack (σ_{T0}): $\sigma_T = \sqrt{\sigma_{T0}^2 + \sigma_D^2}$

Photons collection

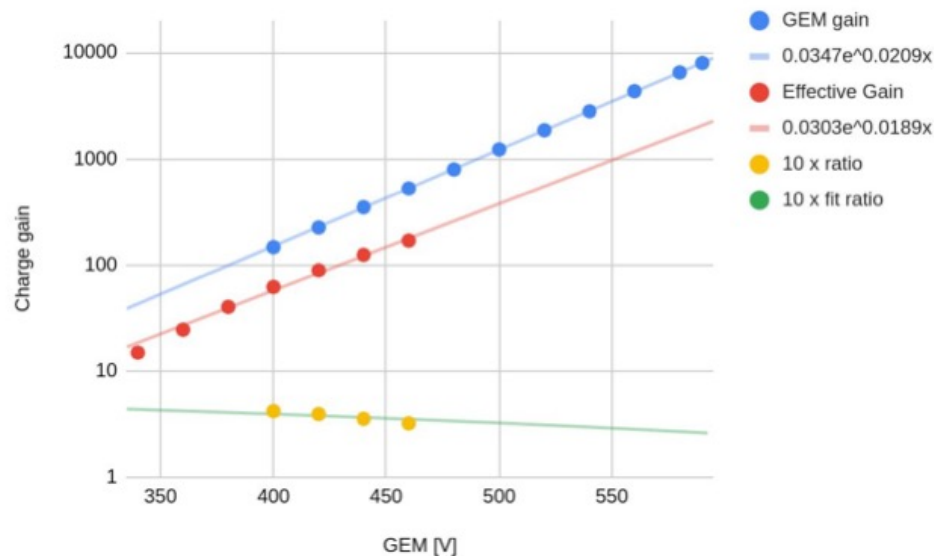
1. The mean total number of photons is obtained using $0.07 \gamma/e$: $N_{\gamma}^{\text{mean,tot}} = N_e^{\text{tot}} \cdot 0.07 \gamma/e$
2. The number of total photons N_{γ}^{tot} extracted from a Poisson distribution with mean value $N_{\gamma}^{\text{mean,tot}}$
3. The number of photons hitting the sensor depends on the solid angle ratio Ω : $N_{\gamma} = N_{\gamma}^{\text{tot}} \cdot \Omega$
 where: $\Omega = \frac{1}{(4(\delta+1)a)^2}$; $\delta = \left(\frac{\text{image size}}{\text{sensor size}}\right)$ ($= \frac{350 \text{ mm}}{14.976 \text{ mm}}$ for ORCA Fusion on LIME); $a = 0.95$ aperture
4. γ 's positions are obtained with random extractions of N_{γ} positions from a gaussian around the initial hit position, with $\sigma_T = \sqrt{\sigma_{T_0}^2 + \sigma_D^2}$
5. The sensor noise is added to the simulation as an image:
 - from a pedestal file (option used so far);
 - from a set of images simulated with the code from the Brazilian colleagues.

GEM gain and efficiency

The GEM gain G and efficiency changes according to operating conditions and detector configuration

Dependence of the gain as a function of HV: $G = 0.347 \cdot e^{0.029 \cdot HV}$

Dependence of the efficiency as a function of HV: $\varepsilon = 0.873 \cdot e^{0.002 \cdot HV}$



- GEM gain from Fernando's measurements
- Efficiency from effective gain measurements from Francesco and Karolina

Gain saturation (in a nutshell)



from Davide, see:
<https://cernbox.cern.ch/index.php/s/UJlyEZZPLdkSrH6/download>

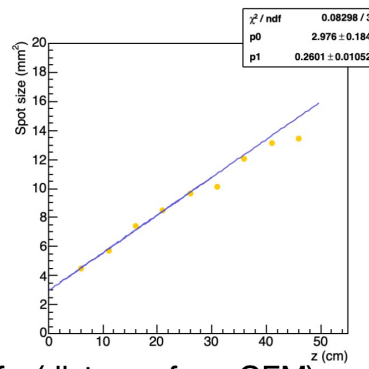
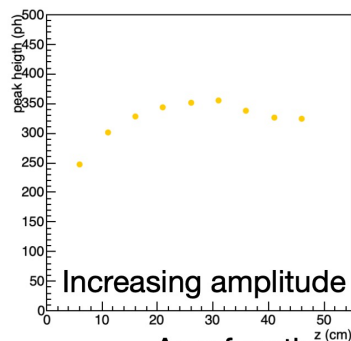
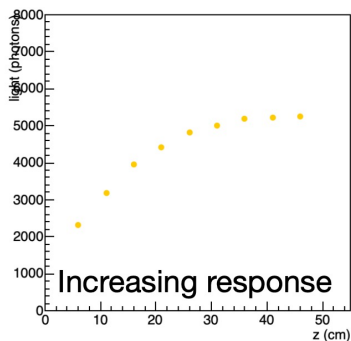
In a real optical TPC: Gain and light yield (ph/e) are not constant → no linearity between light production and ionization

- In an ideal optical TPC:
 - charges are efficiently drifted toward GEM;
 - gain and light yield (ph/e) are constant



- As a function of the distance from the GEM:
- Decreasing of the spot amplitude and increasing of the spot size (because of diffusion)

• Observed behaviour:

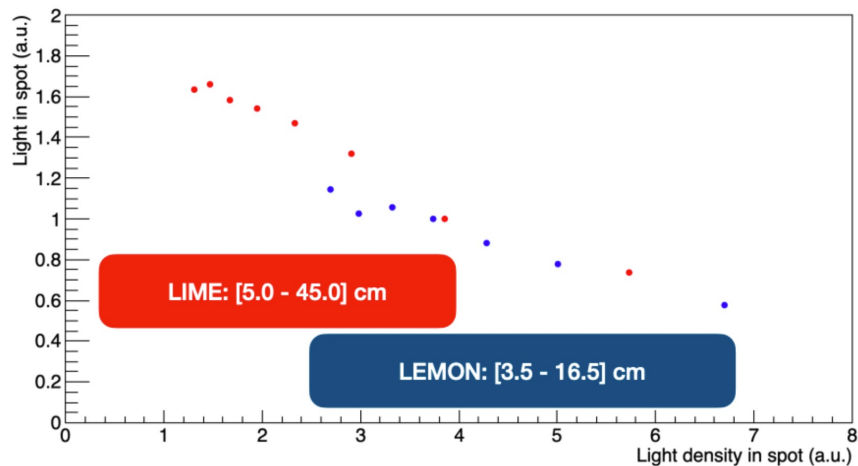


As a function of z (distance from GEM)

Spot size increasing because of the diffusion

Gain saturation (in a nutshell)

⁵⁵Fe data; expected density evaluated from diffusion parameters (simulations)



From a
“simple” model:

$$G = \frac{Ae^{\alpha V_{GEM}}}{1 + \beta n_0 (e^{\alpha V_{GEM}} - 1)}$$

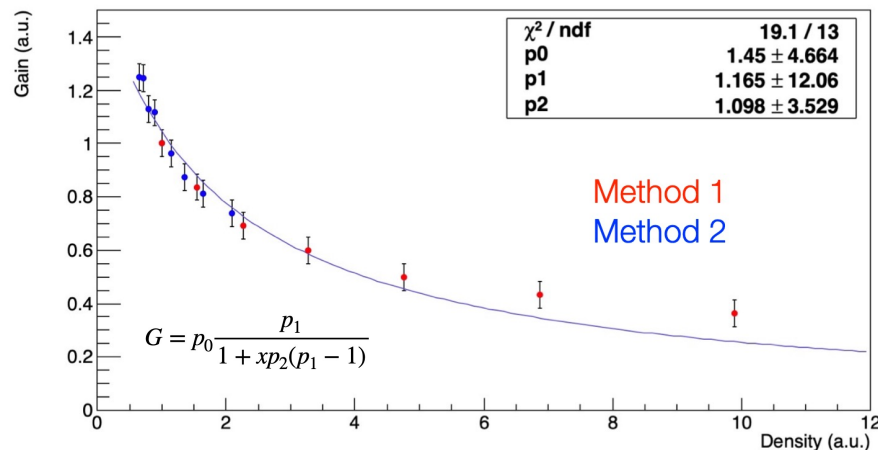
from Davide, see:

<https://cernbox.cern.ch/index.php/s/tJlyEZZPLdkSrH6/download>



Charge density on GEM3 can be varied:

- Varying the gain of GEM1; changing the charge (method 1)
- Varying the z; changing the size of the spot (method 2)



Simulation of the saturation

- The number of electrons entering GEM3 are calculated as before.
- The charge cloud have a 3D gaussian shape:

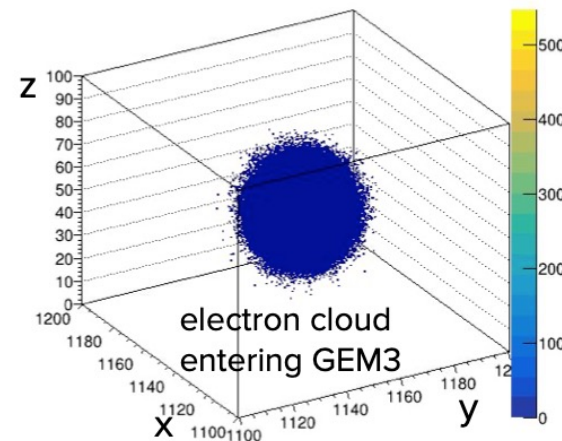
$$\sigma_T = \sqrt{\sigma_{T_0}^2 + \sigma_{D,T}^2} \quad \text{in the plane of the GEM as before;}$$

$$\sigma_L = \sqrt{\sigma_{L_0}^2 + \sigma_{D,L}^2} \quad \text{along the z axis}$$

- Clouds are divided in voxels (with the size of the pixels in the x-y plane and 2 x GEM thickness in z);
- Non saturated gain in GEM#1 and GEM#2 is assumed;
- the number n of electrons in each voxel is multiplied by a gain

$$G = A \frac{g}{1 + \frac{n}{n_h}(g-1)} \quad \text{where g is the no-saturated gain; A is an overall free parameter}$$

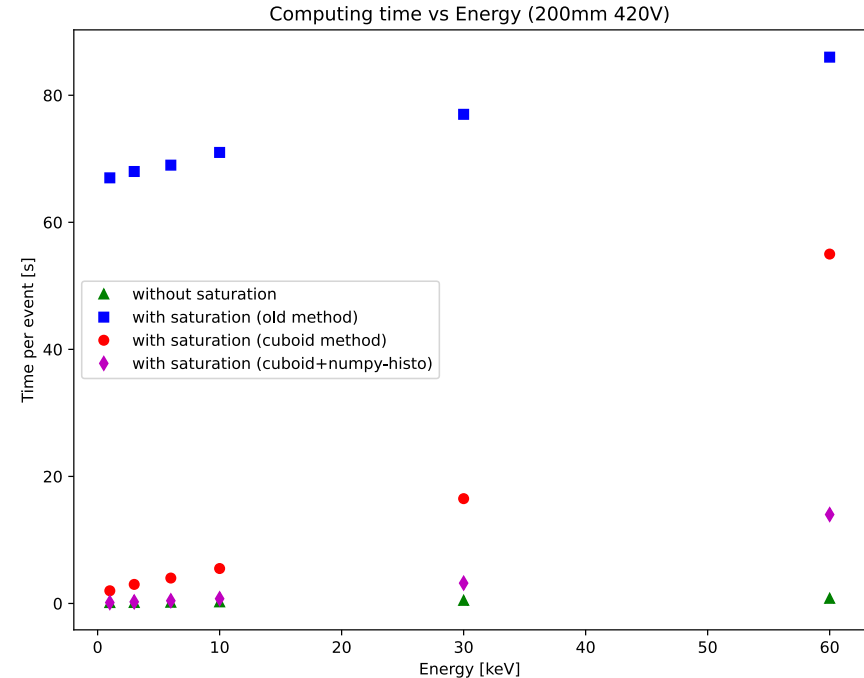
- Total number of electrons is the sum of all voxels along z.
- The number of photons (in each x-y bin) is obtained as before (light yield, geometrical efficiency, ...).



The simulation of the saturations resulted to be extremely slow (tens s per events).

Technical, but relevant, improvements to the method are being developed:

- “cuboid” method:
 - The saturation is applied only in a much smaller cuboid around the track, not the full 3D histo
- “cuboid+Numpy-histo”:
 - A smaller numpy histo (with the size of the cuboid) is used. The rest of the blank image is added in the end.
- Another improvement under study, promising for further improvement at high energies.



Data/MC comparison

Data: ^{55}Fe data taking with LIME (April 2021, runs from 4119 to 4190)

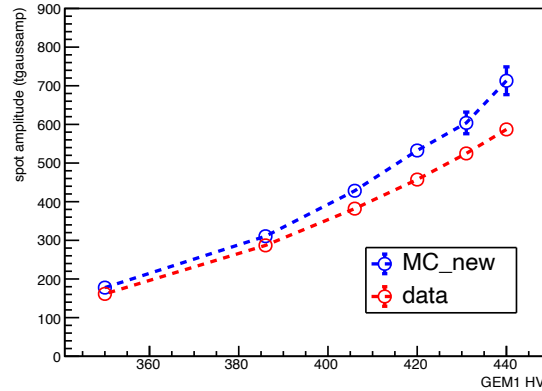
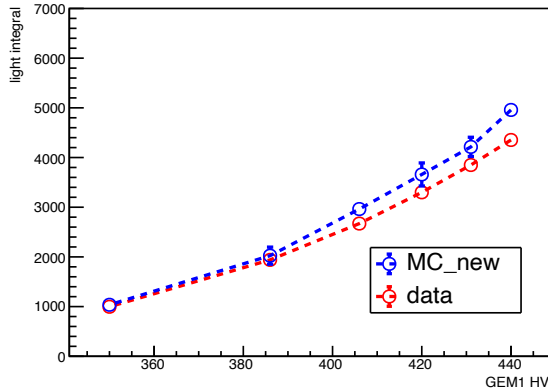
- GEM1_HV scan: 350, 386, 406, 420, 431, 440 V
- GEM2_HV = GEM3_HV = 440 V
- Distance from GEM scan: 6, 11, 16, 21, 26, 31, 36, 41, 46 cm

Data and MC reconstructed and analysed with the same code ("autumn21" branch)

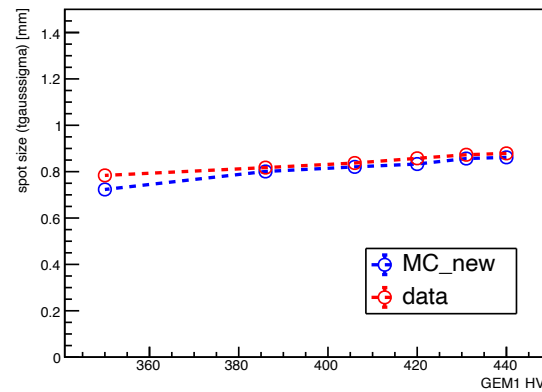
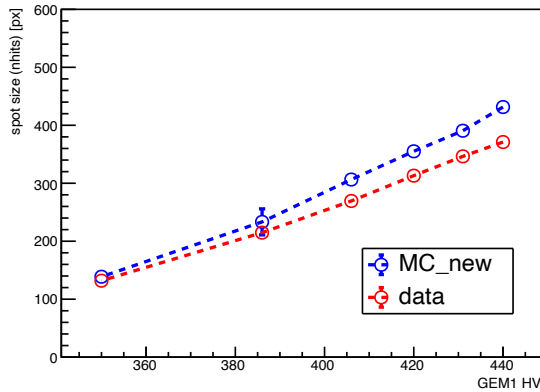
Simulation parameters:

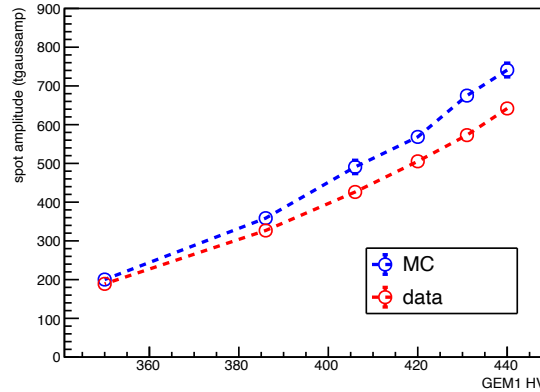
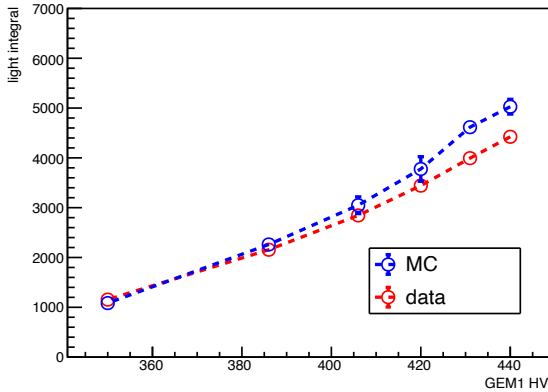
- 6 keV electrons
- Saturation: $\beta = \frac{1}{n_h} = 1e^{-5}$, $A = 1$
- Absorption: $\lambda = 1000$ mm
- Light yield: 0.07 photons/electrons
- Diffusion parameters:
(from <https://arxiv.org/pdf/2007.00608.pdf>)
 - $\sigma_{T_0} = 350$ μm , $\sigma_T = 0.11$ mm/sqrt(cm)
 - $\sigma_{L_0} = 260$ μm , $\sigma_L = 0.099$ mm/sqrt(cm)

- ORCA Fusion:
 - 2304 x 2304 pixels (1 pixel 6.5 μm x 6.5 μm)
 - Camera aperture $a = 0.95$
 - Sensor size: 14.976 mm
 - Sensor calibration \rightarrow 1 photon = 2 sensor counts
 - Active area: 35 cm x 35 cm
 - $\delta = \frac{350 \text{ mm}}{14.976 \text{ mm}}$
- GEM1_HV=350, 386, 406, 420, 431, 440 V
- GEM2_HV = 440 V, GEM3_HV = 440 V
- Distance from GEM scan: 10, 15, 20, 25, 30, 35, 40, 45 cm

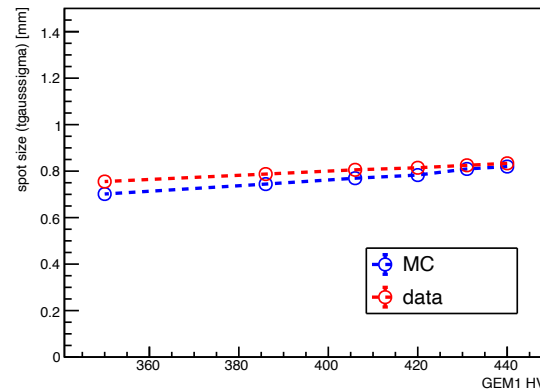
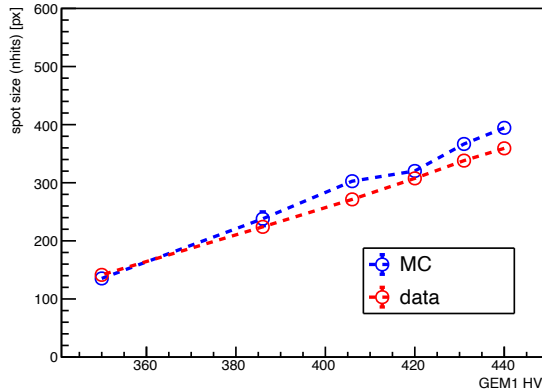


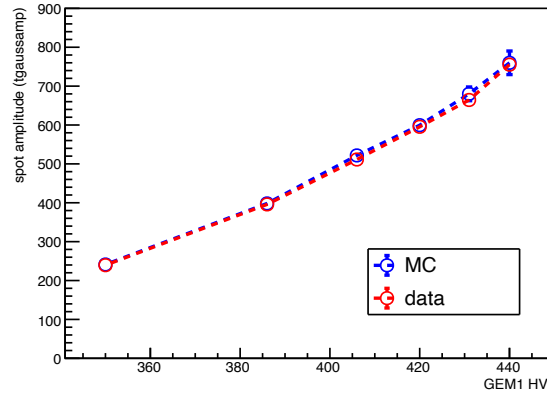
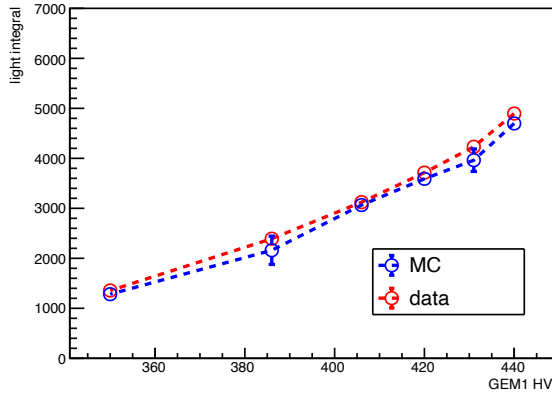
$z = 45$ cm



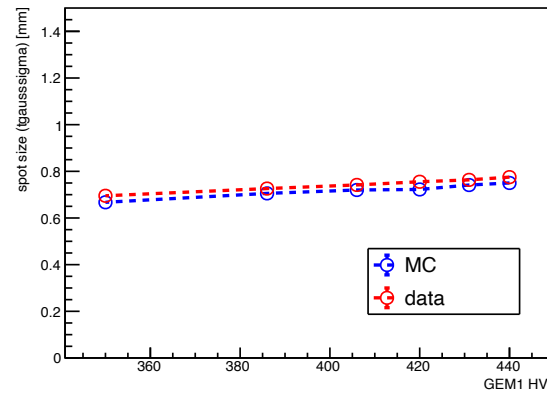
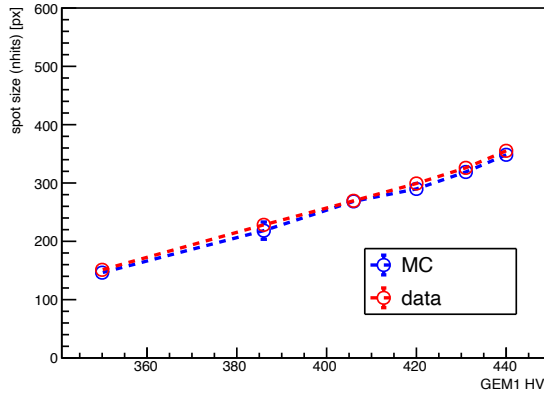


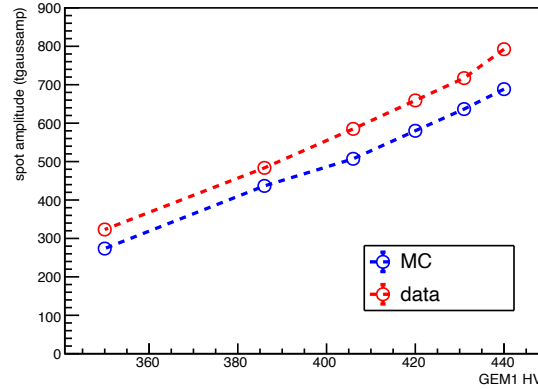
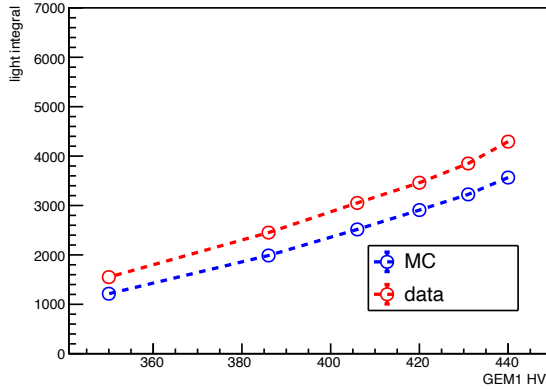
$z = 35$ cm



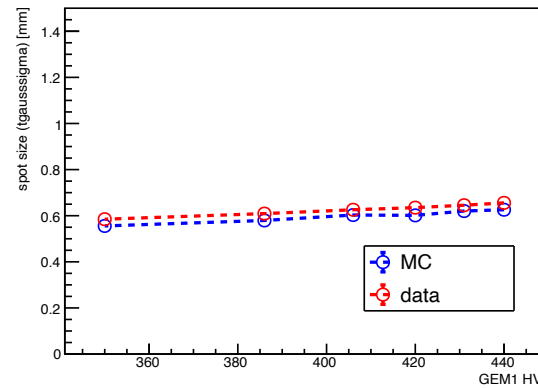
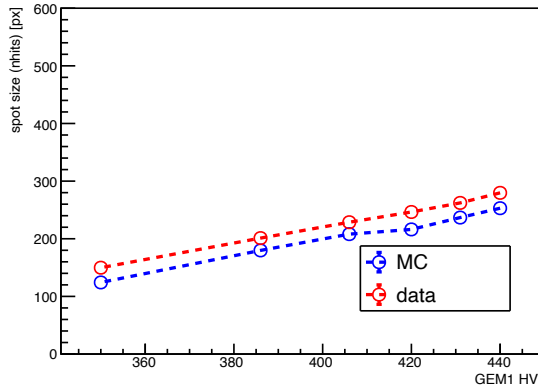


$z = 25$ cm



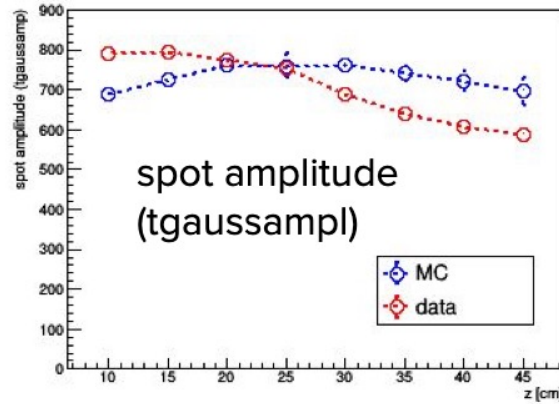
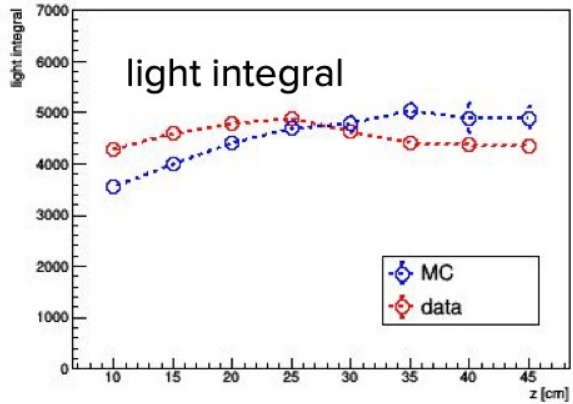


$z = 10$ cm

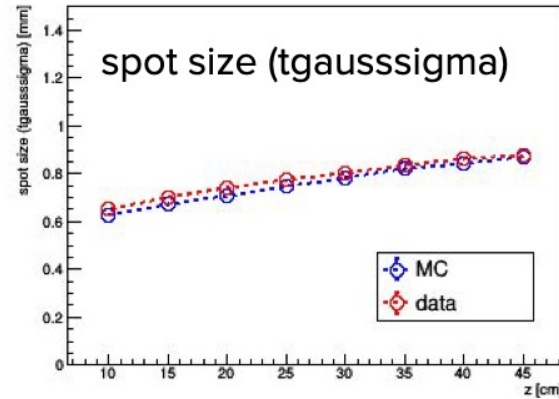
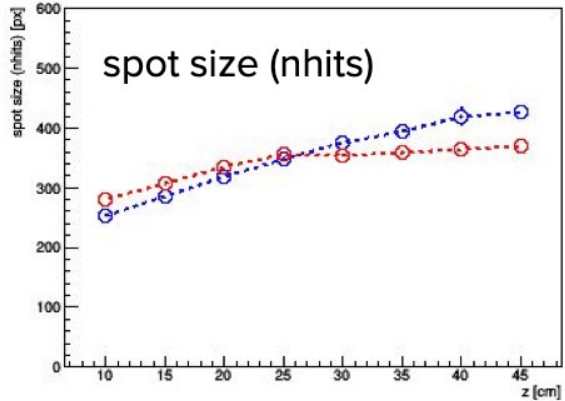


Data/MC comparison

Results from Giulia



HV = 440 V



- The digitization is reasonably fast and provides acceptable results.
- Simulation parameters must be tuned in order to improve data/MC agreement.
- Data/MC comparison must be extended:
 - using higher statistics;
 - looking at other reconstructed variables;
 - exploiting data at different energies and with different sources.

