

Nucleosynthesis of light and heavy elements across the Galaxy

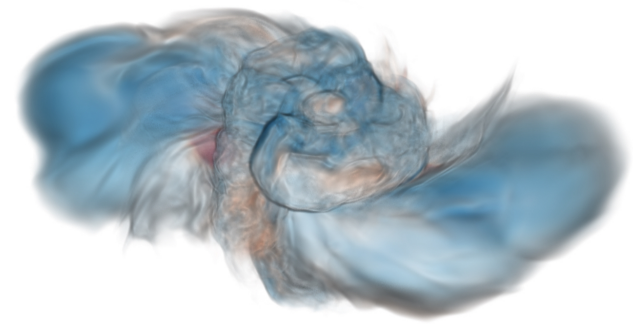
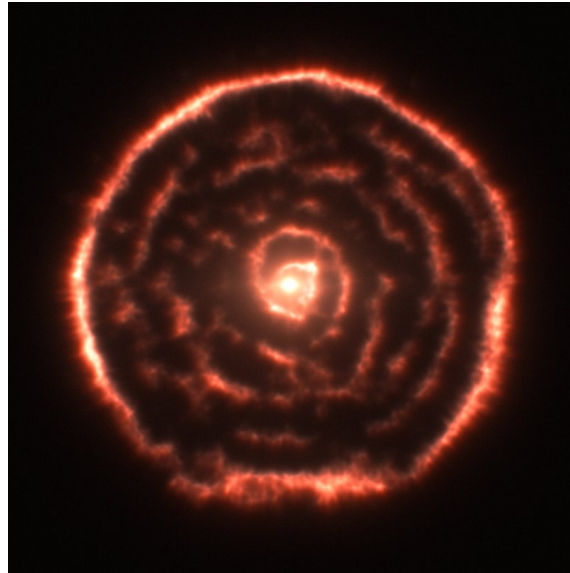
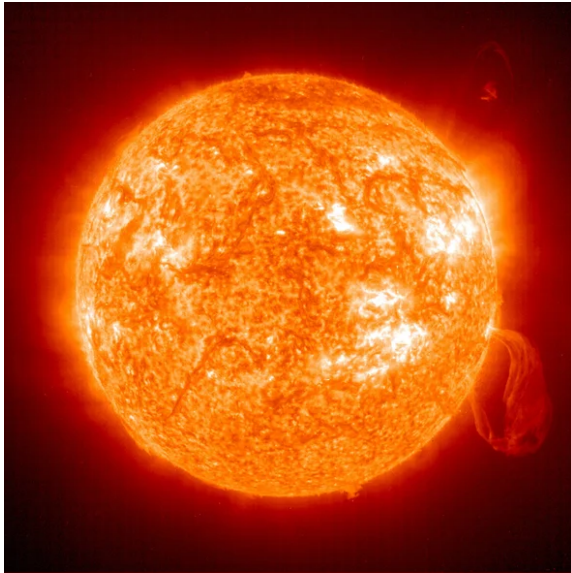
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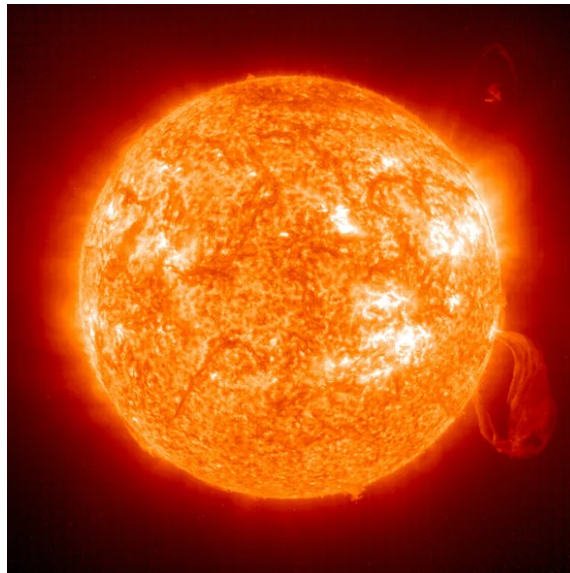


Outline

- Solar neutrinos and luminosity constraint in the era of precision solar physics
- Presolar grains and magnetic-buoyancy-induced mixing in Asymptotic Giant Branch (AGB) stars
- Kilonovae and production of very light elements in Neutron Star Mergers (NSMs)

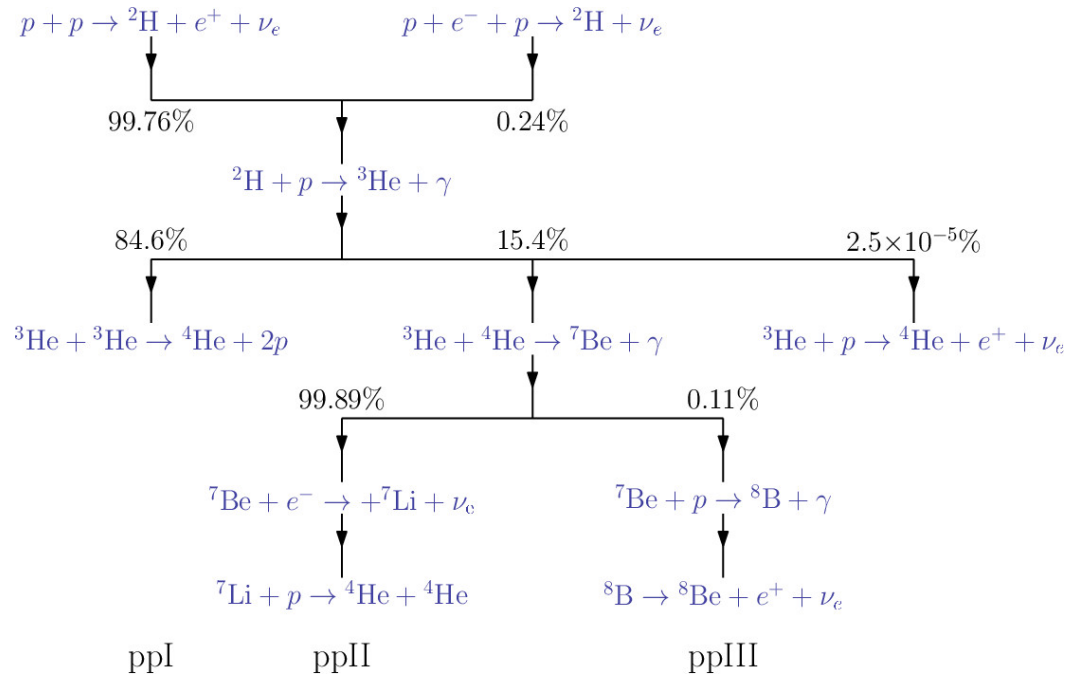


Solar neutrinos and luminosity constraint in the era of precision solar physics



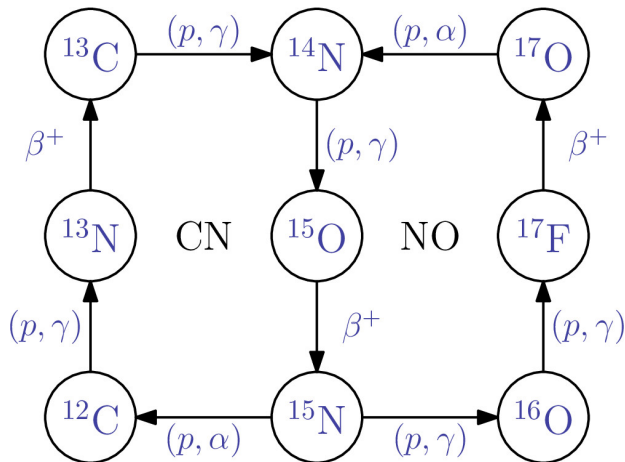
The Sun: nuclear processes and neutrinos

- The Sun is powered by nuclear reactions that transform H into ${}^4\text{He}$
- Two main sequences of reactions:



1) pp chain

2) CNO cycle



Products: neutrinos

→ pp, pep, hep, ${}^7\text{Be}$, ${}^8\text{B}$, ${}^{13}\text{N}$, ${}^{15}\text{C}$, ${}^{17}\text{F}$

Standard Solar Model (SSM)

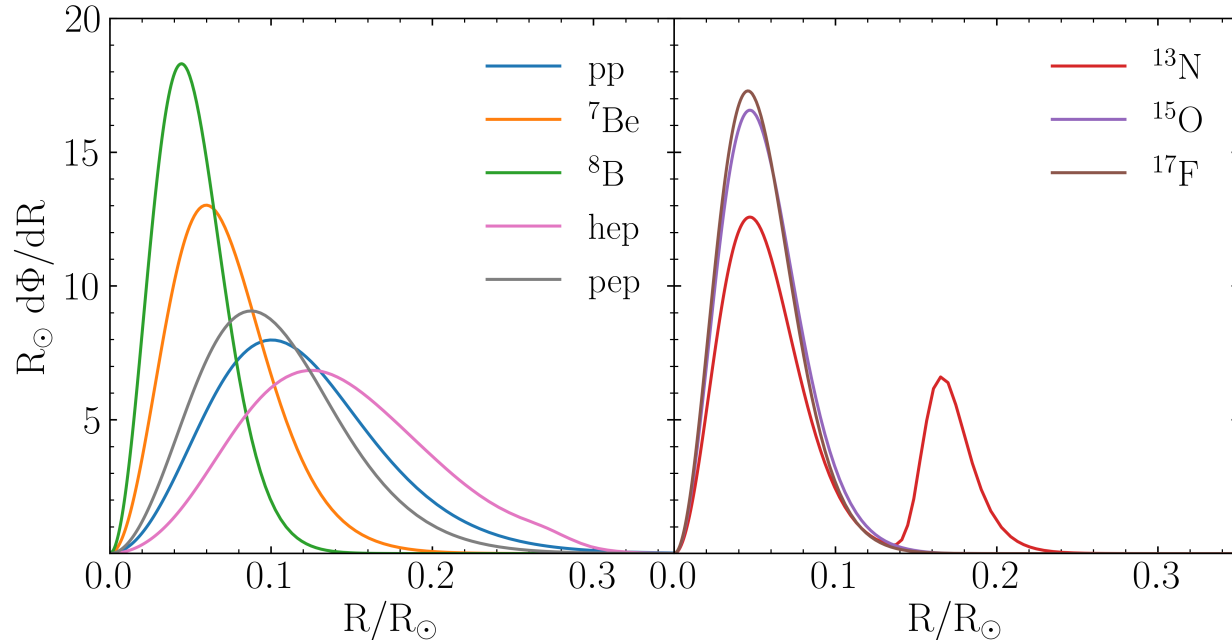
“A SSM is one which reproduces, within uncertainties, the observed properties of the Sun, by adopting a set of physical and chemical inputs chosen within the range of their uncertainties” (Bahcall, 1995)

- Evolve a model with $1 M_{\odot}$ starting from a chemically homogeneous model to present solar age with the best available micro- and macro-physics

→ Match R_{\odot} , L_{\odot} , and $(Z/X)_{\odot}$ to better than one part in 10^{-5}

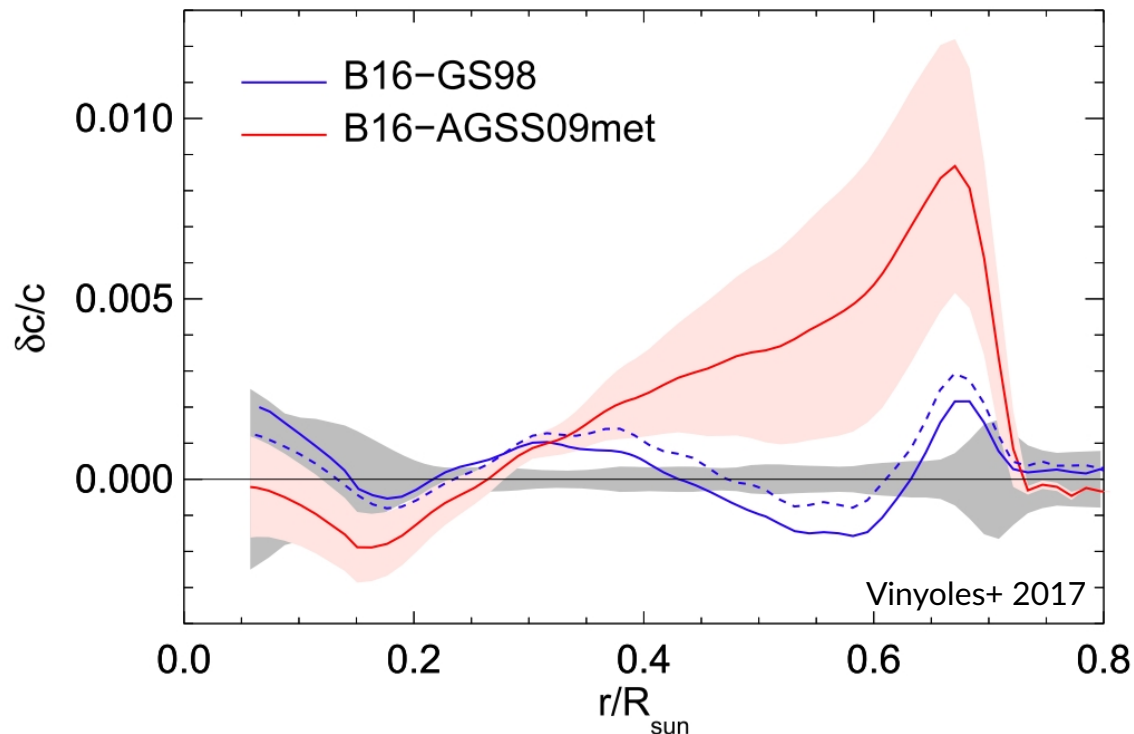
- Predictions:

- 1) Physical quantities
- 2) Chemical profiles
- 3) Helioseismic quantities
- 4) Neutrino fluxes



SSM: the solar abundance problem

- SSM can be then validated by observational constraints → **solar neutrino fluxes** and **helioseismic** measurements
- New generation of spectroscopic studies yield a solar metallicity lower than older results
- Theoretical predictions of SSMs adopting low metallicity surface compositions fail in reproducing all helioseismic determinations of solar properties

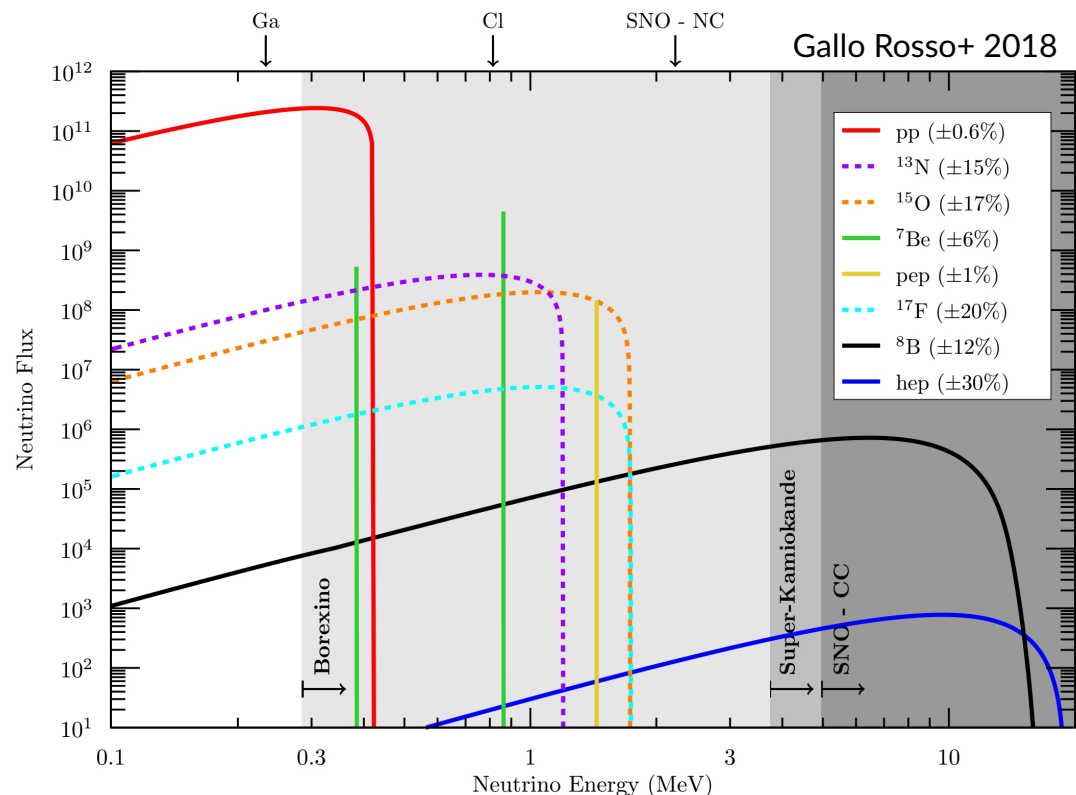


SSMs: solutions?

- Solutions:
 - 1) Increase of the heavy-element admixture
 - 2) Increase of the radiative opacity at the base of the convective envelope
- The degeneracy between radiative opacity and solar composition can be removed by **measuring the neutrino fluxes produced in the CNO cycle**, i.e. the CNO burning rate

- CNO neutrinos have low energies (\sim MeV) and are produced in the same energy region of neutrinos from the pp chain

→ Experimental challenge



Constraints from neutrinos

- Experimental measured fluxes ($\Phi_i = \varphi_i \times 10^{\gamma_i} \text{ cm}^2/\text{s}$) agree with SSM results

Vescovi+, JPhG 2021

Flux	γ_i	φ_i		Experimental results	Source
		GS98	PLJ14		
Φ_{pp}	10	5.99(1 ± 0.01)	6.01(1 ± 0.01)	6.1(1 ± 0.1)	BX
Φ_{pep}	8	1.42(1 ± 0.02)	1.43(1 ± 0.02)	1.27(1 ± 0.17)	BX
Φ_{Be}	9	4.73(1 ± 0.12)	4.52(1 ± 0.12)	4.99(1 ± 0.03)	BX
Φ_B	6	5.52(1 ± 0.24)	5.01(1 ± 0.24)	5.41(1 ± 0.016)	SK
Φ_{hep}	3	8.15(1 ± 0.30)	8.28(1 ± 0.30)	8(1 ± 2)	SNO
Φ_N	8	2.87(1 ± 0.30)	2.58(1 ± 0.29)	—	—
Φ_O	8	2.13(1 ± 0.36)	1.86(1 ± 0.35)	—	—
Φ_F	6	5.51(1 ± 0.37)	4.04(1 ± 0.36)	—	—
Φ_{CNO}	8	5.06(1 ± 0.32)	4.48(1 ± 0.31)	$7.0^{+3.0}_{-2.0}$	BX

- ${}^7\text{Be}$ and ${}^8\text{B}$ neutrino fluxes are probed with high precision → solar core temperature
- What about pp and CNO fluxes?
- Helpful instrument: **luminosity constraint**

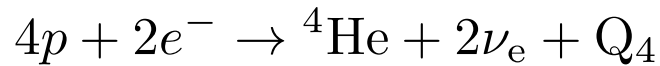
The “standard” luminosity constraint

- Nuclear fusion is responsible for the observed solar luminosity

→ Gravothermal energy negligible

$$\longrightarrow L_{\odot} = L_{\text{nuc}} - L_{\nu}$$

→ Local nuclear equilibrium



$$\longrightarrow L_{\text{nuc}} = Q_4 \dot{N}({}^4\text{He})$$

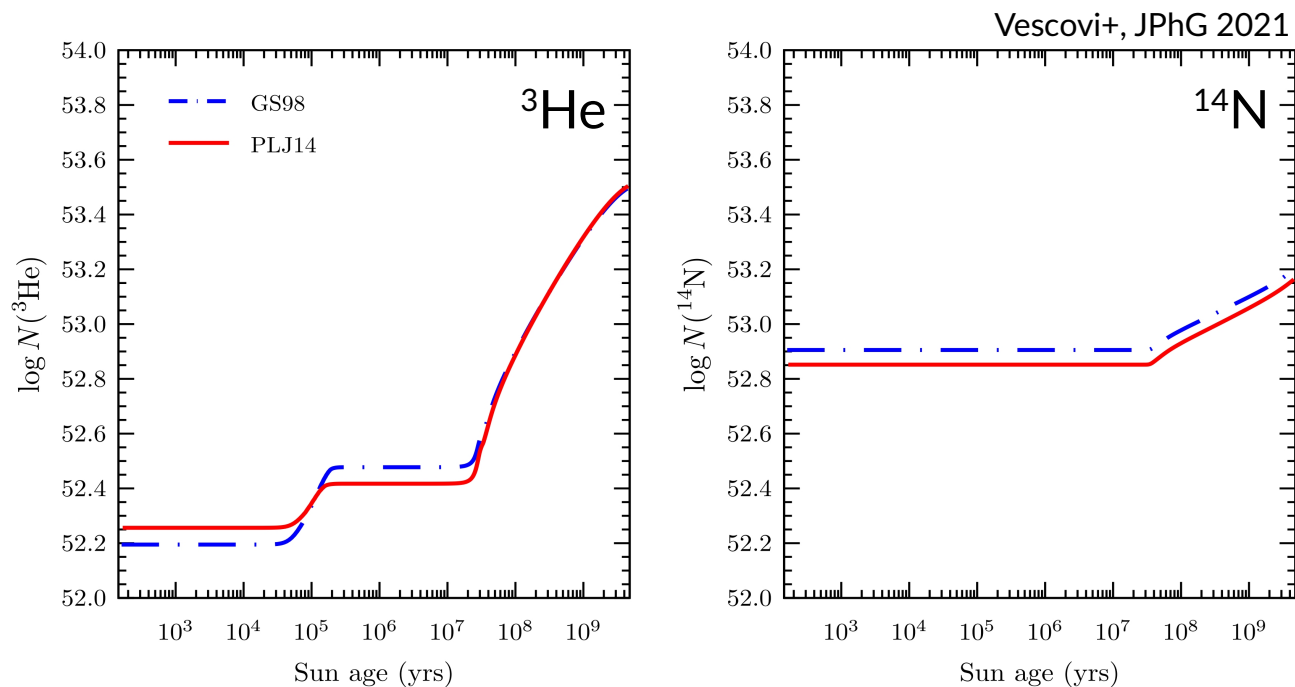
→ Lepton number conservation

$$\longrightarrow 4\pi\text{au}^2 \sum_i \Phi_i = 2\dot{N}({}^4\text{He})$$

$$L_{\odot} = Q_4 \underbrace{\frac{4\pi\text{au}^2 \sum_i \Phi_i}{2}}_{\dot{N}({}^4\text{He})} - \underbrace{4\pi\text{au}^2 \sum_i \langle E_i \rangle \Phi_i}_{L_{\nu}} \longrightarrow \boxed{\frac{L_{\odot}}{4\pi\text{au}^2} = \sum_i \left(\frac{Q_4}{2} - \langle E_i \rangle \right) \Phi_i}$$

Limits of the standard luminosity constraint

- The total number of both ^3He and ^{14}N nuclei in the whole Sun increases with the time
- In the Sun, the gravothermal energy is absorbed to produce an expansion against gravity on a timescale of few Myr



- The standard luminosity constraint is **accurate to better than 1%**
- Extremely precise determination of $L_{\odot} = 3.8275 (1 \pm 0.4\text{‰}) \times 10^{33} \text{erg/s}$ **requires corrections** to the “standard” form

A new version of the luminosity constraint

- **Not only** nuclear fusion is responsible for the observed solar luminosity

→ Gravothermal energy

$$\longrightarrow L_{\odot} = L_{\text{nuc}} - L_{\nu} - L_{\text{g}}$$

→ Production of more nuclei

$$\longrightarrow L_{\text{nuc}} = \sum_j Q_j \dot{N}(j)$$

→ Lepton number conservation

$$\longrightarrow 4\pi\text{au}^2 \sum_i \Phi_i = \sum_j c_j \dot{N}(j)$$

$$\longrightarrow \frac{1}{4\pi\text{au}^2} \left(L_{\odot} + L_{\text{g}} + \sum_{j \neq {}^4\text{He}} L_j \right) = \sum_i \left(\frac{Q_4}{2} - E_i \right) \Phi_i$$

Where $L_j := \left(\frac{c_j Q_4}{2} - Q_j \right) \dot{N}(j)$ accounts for the corrections due to the isotope j

SSM computations

- By making use of SSMs, corrective terms can be evaluated!
- Two solar mixtures → high-metallicity (GS98) and low-metallicity (PLJ14)
- State-of-the-art opacities (OPAL05)
- Latest reaction rates (Solar fusion II + updates)

→ Relevant corrections: must be of the order of **0.4‰** $L_{\odot} \approx 1.5 \times 10^{30} \text{ erg s}^{-1}$

Models	$\dot{N}(^3\text{He})$	$\dot{N}(^{14}\text{N})$	$L_{^3\text{He}}$	$L_{^{14}\text{N}}$	L_{g}
GS98	3.29(1 ± 0.07)	2.15(1 ± 0.13)	3.39(1 ± 0.07)	0.57(1 ± 0.13)	1.54(1 ± 0.04)
PLJ14	3.42(1 ± 0.07)	2.07(1 ± 0.13)	3.53(1 ± 0.07)	0.55(1 ± 0.13)	1.52(1 ± 0.04)

$\dot{N}(j)$ (units of 10^{35} s^{-1}) and L_j (units of $10^{30} \text{ erg s}^{-1}$)

→ $L_{^3\text{He}}$, $L_{^{14}\text{N}}$, and L_{g} **do matter** and have small uncertainties

A new version of the luminosity constraint II

$$1 \pm 0.4 \text{‰} = \frac{1}{\mathcal{F}} \sum_i \left(\frac{Q_4}{2} - \langle E_i \rangle \right) \Phi_i$$

Standard

$$\mathcal{F} = \frac{L_{\odot}}{4\pi \text{au}^2}$$



$$\mathcal{F} = 8.4946 \times 10^{11}$$

$$\mathcal{F} = \frac{L_{\odot} + L_{^3\text{He}} + L_{^{14}\text{N}} + L_{\text{g}}}{4\pi \text{au}^2}$$

New



$$\mathcal{F}(\text{GS98}) = 8.5068 \times 10^{11}$$

$$\mathcal{F}(\text{PLJ14}) = 8.5070 \times 10^{11}$$

- Fixed solar luminosity (by observations) and the three new terms are all positive \rightarrow number of expected neutrinos increased
- \mathcal{F} increases of $\sim 1.5 \text{‰}$
- Negligible dependence on solar composition

Luminosity constraint and the search for CNO neutrinos

It is possible to obtain a constraint on the flux of pp and CNO neutrinos by:

- neglecting Φ_{hep} (very small)
- adopting $\Phi_{\text{pep}}/\Phi_{\text{pp}}$ and $\Phi_{\text{O}}/\Phi_{\text{N}}$ from SSMs
- fixing Φ_{Be} and Φ_{B} to the experimental results - known better than theory



$$\Phi_{\text{pp}} + 1.654 \Phi_{\text{N}} = k(1 \pm 2 \text{‰}) \times 10^{10} \text{cm}^{-2} \text{s}^{-1}$$

Corrective terms	GS98	PLJ14	Average
None	5.9936	5.9936	5.9936
$L_{3\text{He}}$	5.9994	5.9996	5.9995
$L_{3\text{He}} + L_{14\text{N}}$	6.0004	6.0006	6.0005
$L_{3\text{He}} + L_{14\text{N}} + L_{\text{g}}$	6.0030	6.0031	6.0031



+1.5 ‰

pp flux and CNO flux

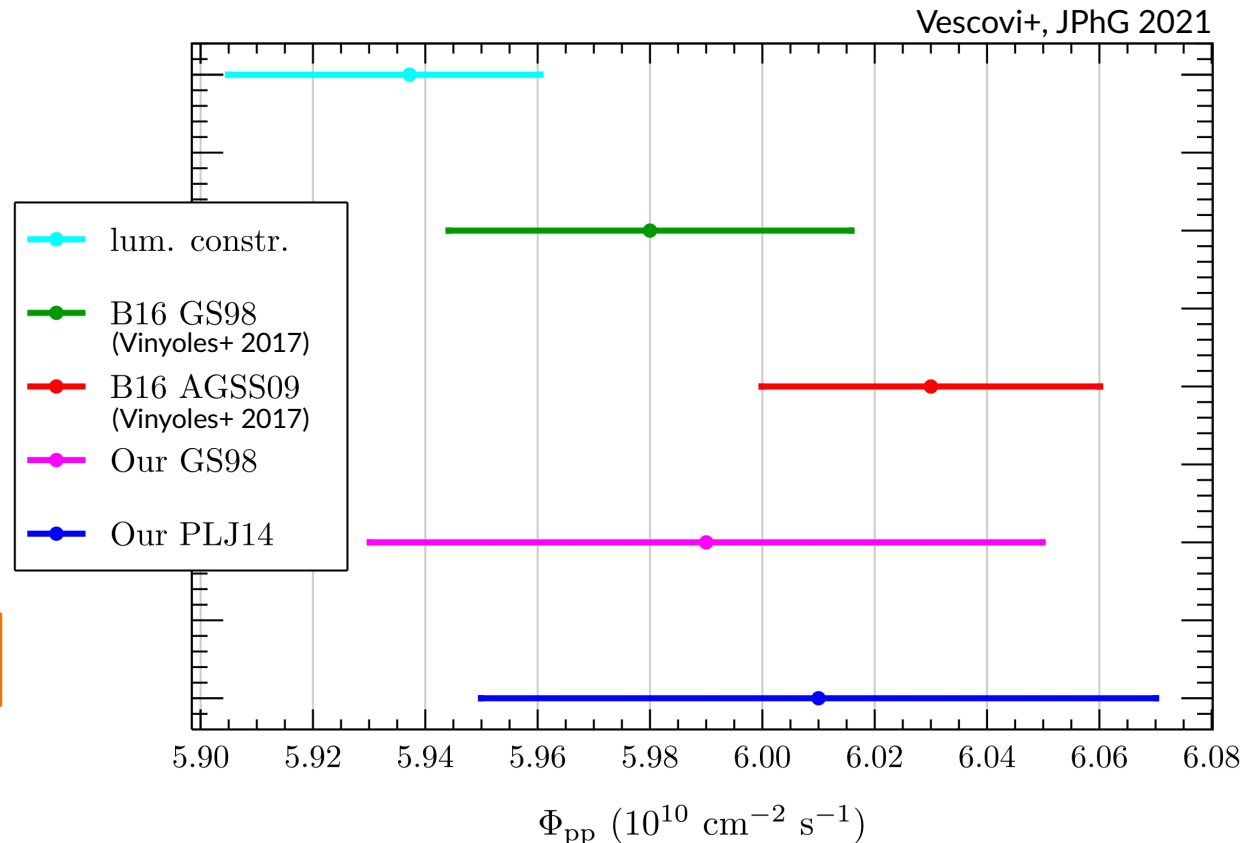
In terms of $\Phi_{\text{CNO}} = \Phi_{\text{N}} + \Phi_{\text{O}} + \Phi_{\text{F}}$:

$$\longrightarrow \Phi_{\text{pp}} + 0.946 \Phi_{\text{CNO}} = 6.003 (1 \pm 2 \%) \times 10^{10} \text{cm}^{-2} \text{s}^{-1}$$

- Using Φ_{CNO} measured by Borexino collaboration



$$\Phi_{\text{pp}} = 5.937^{+0.023}_{-0.032} \text{cm}^{-2} \text{s}^{-1}$$

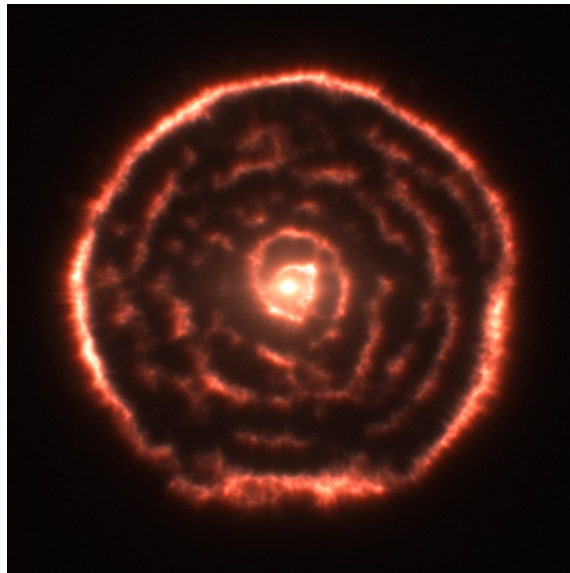


Summary I - Probing metals and CNO in the Sun

Location	Method	Precision
Surface	Observation/ modeling	permil
Convective/radiative interface	Helioseismology	permil
Core	CNO neutrinos	percent

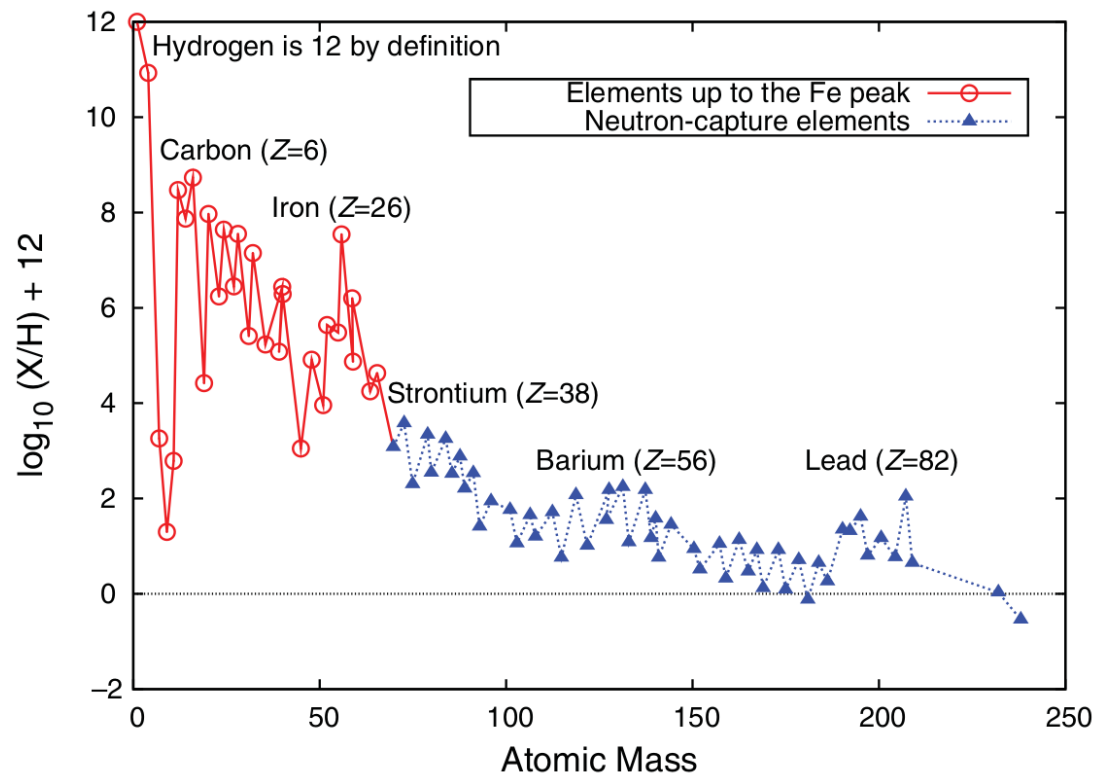
- CNO flux measurement may **solve** the longstanding solar abundance problem
- It relies on the **luminosity constraint** which establishes the best available limits on the rate of creation of pp neutrinos
- Development of a **new version** including corrective terms → non-equilibrium burning of ^3He and ^{14}N abundances and gravothermal energy
- Simple relation linking in Φ_{pp} and Φ_{CNO} , independent from solar core metallicity
- Φ_{pp} in better agreement with high-metallicity SSMs

Presolar grains and magnetic-buoyancy-induced mixing in Asymptotic Giant Branch stars



The origin of heavy elements in the Solar System

- Fusion reactions between **charged particles**
- Neutron capture processes :
 - r(apid)-process
 - s(low)-process



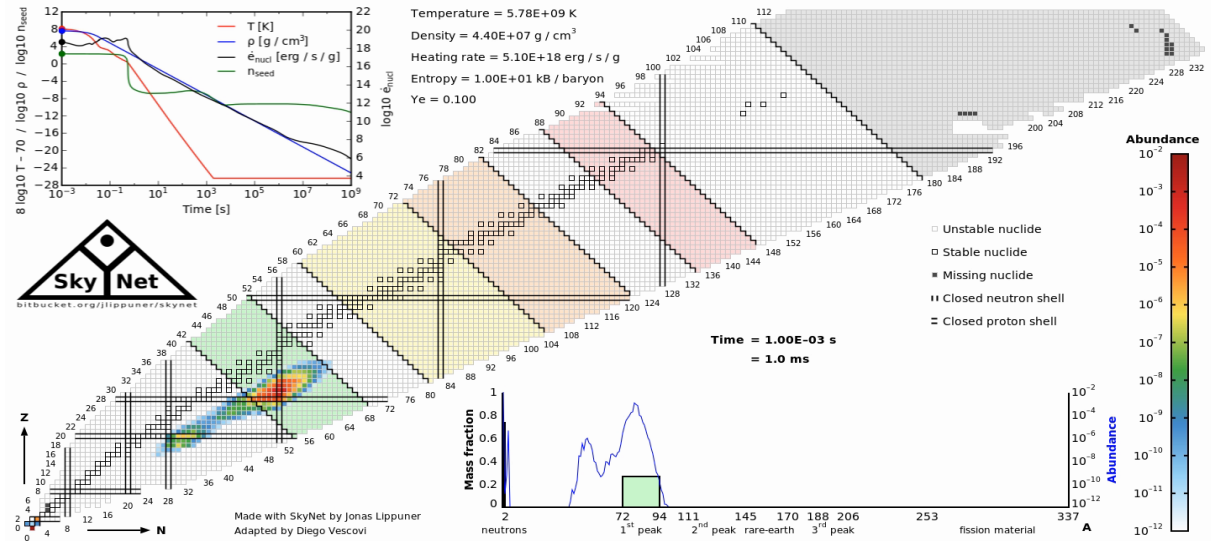
s- and r- process

r-process

High neutron density n_n

$$\rightarrow \tau_{(n,\gamma)} \ll \tau_{\beta\text{-decay}}$$

\rightarrow Supernovae and compact binary mergers

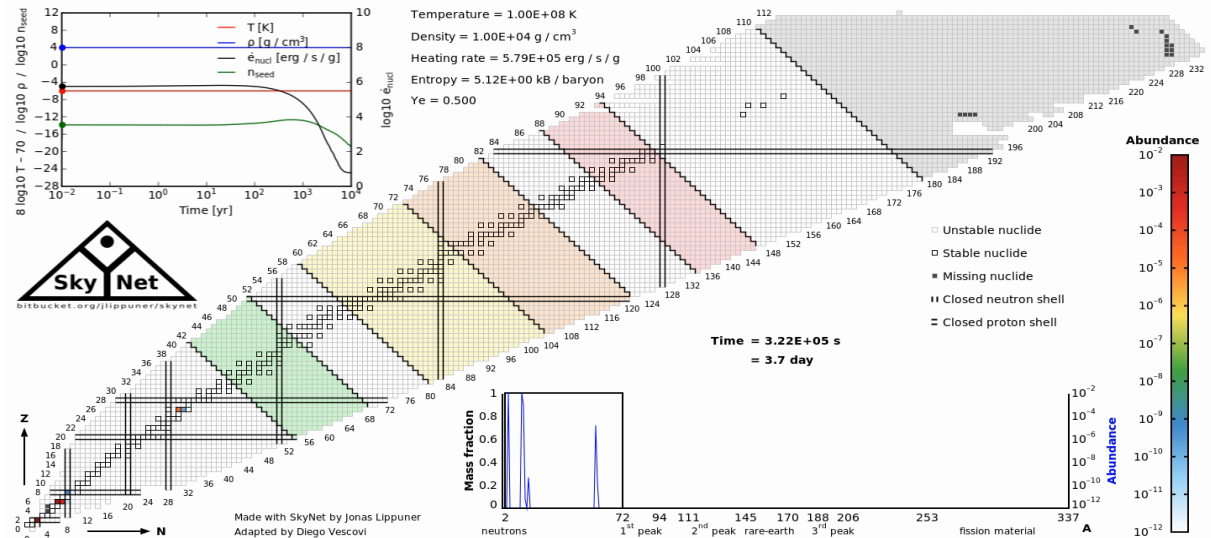


s-process

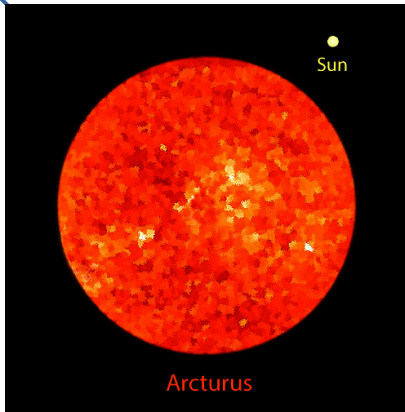
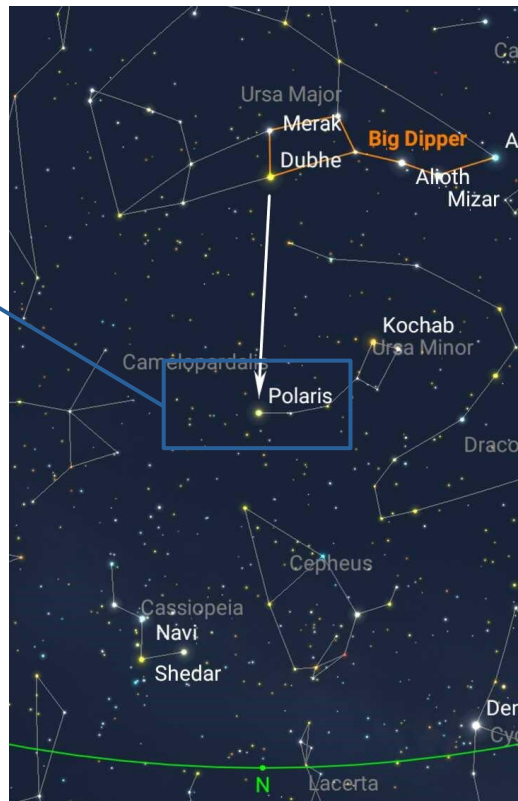
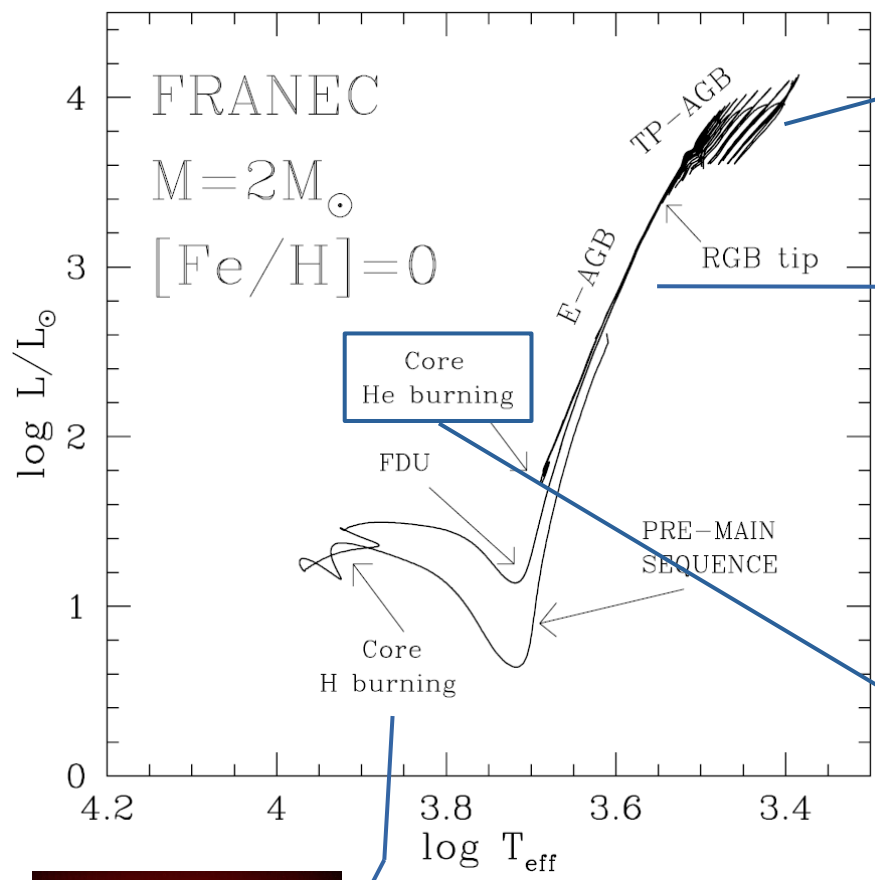
Mild neutron density n_n

$$\rightarrow \tau_{(n,\gamma)} \gtrsim \tau_{\beta\text{-decay}}$$

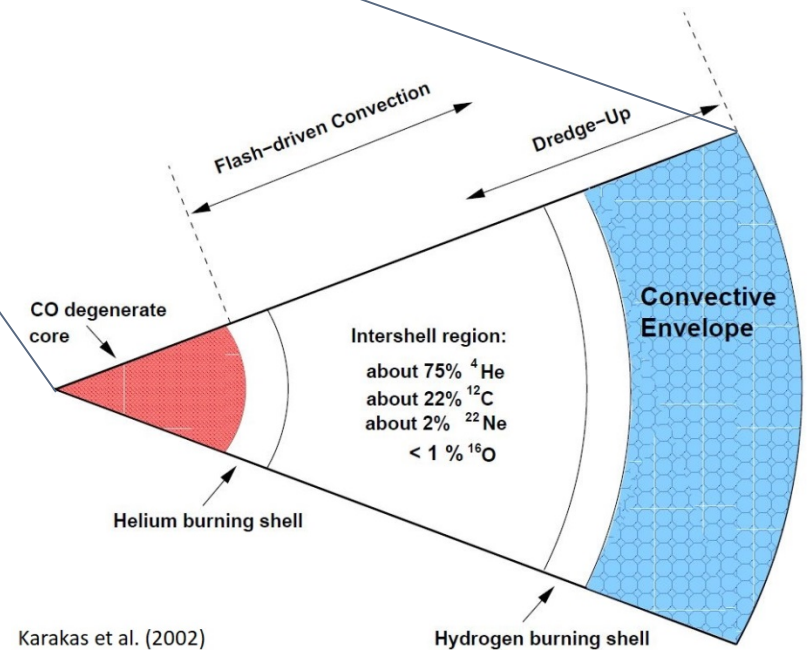
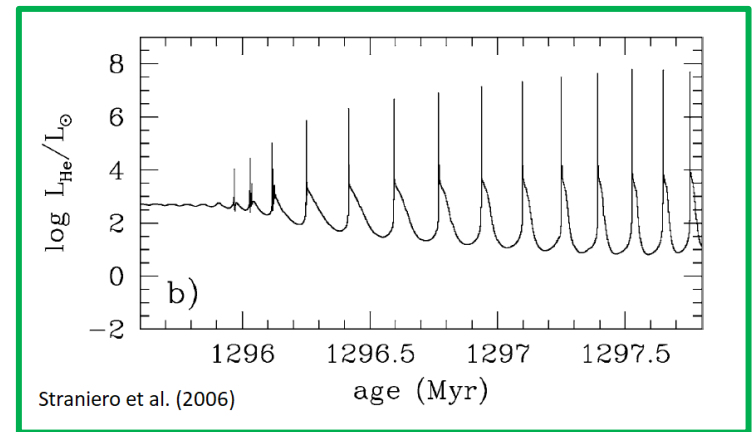
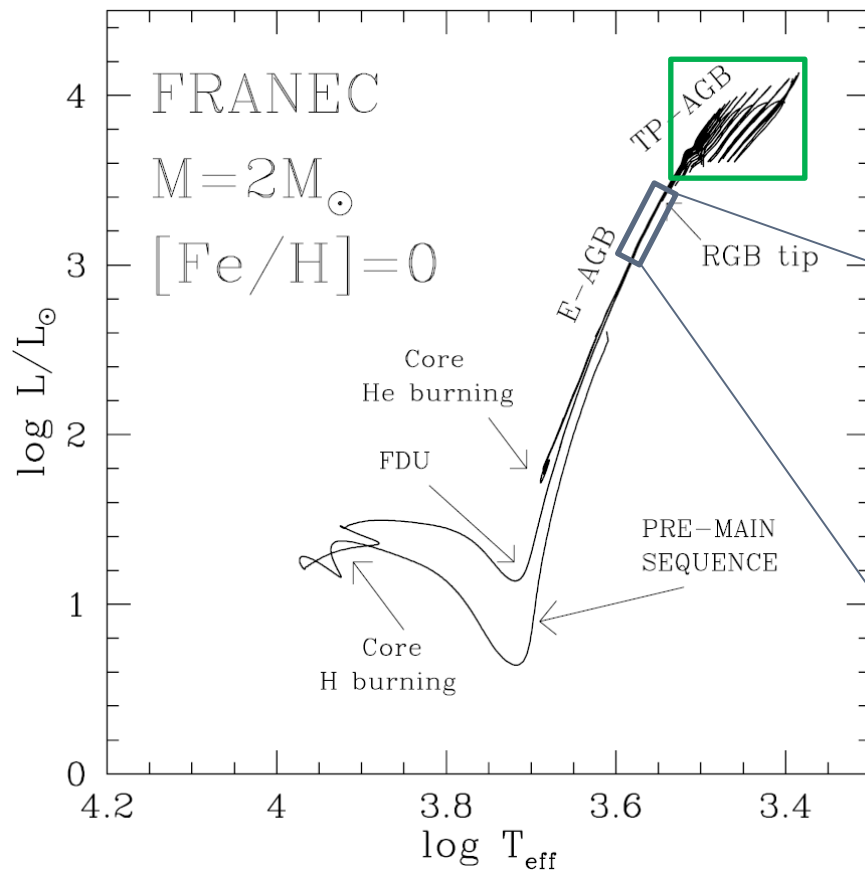
\rightarrow Asymptotic Giant Branch (AGB) and massive stars



Moving towards the AGB phase

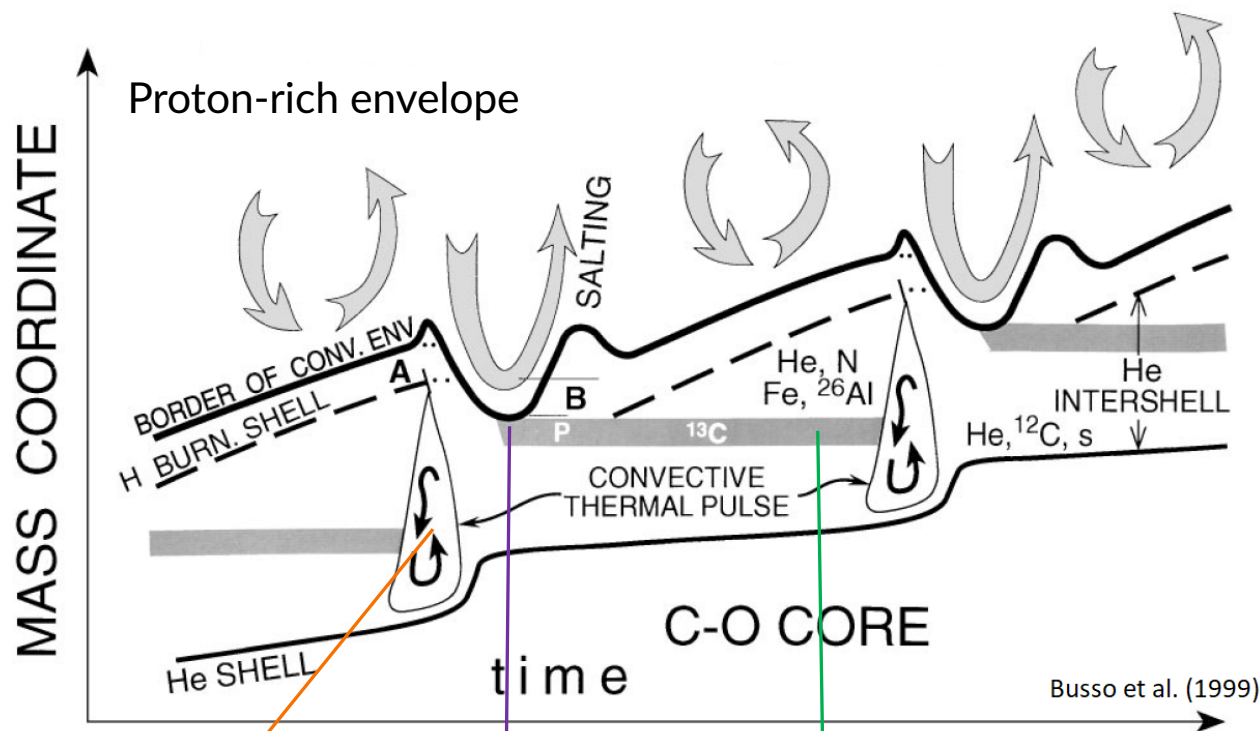


AGB stars

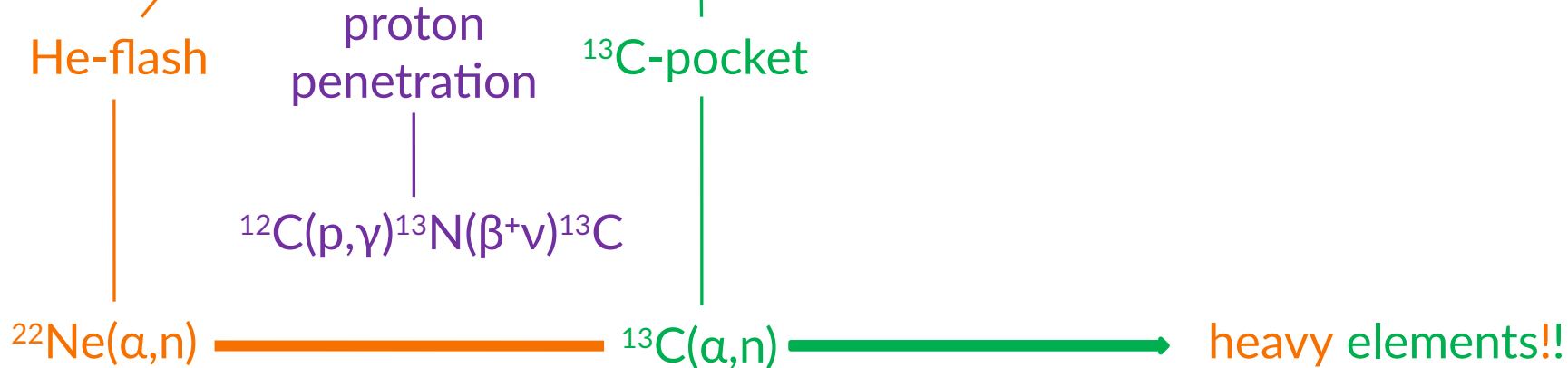


- Low-Mass Stars
- Asymptotic Giant Branch (AGB)
- Thermal Pulses

H- and He-burning in TP-AGB stars



- **What?**
Low-Mass Stars
- **When?**
Asymptotic Giant Branch (AGB)
- **How?**
Thermally Pulsing (TP)



The ^{13}C -pocket: formation

- Protons can penetrate into the He-rich region at each TDU (Third Dredge-Up) phenomenon

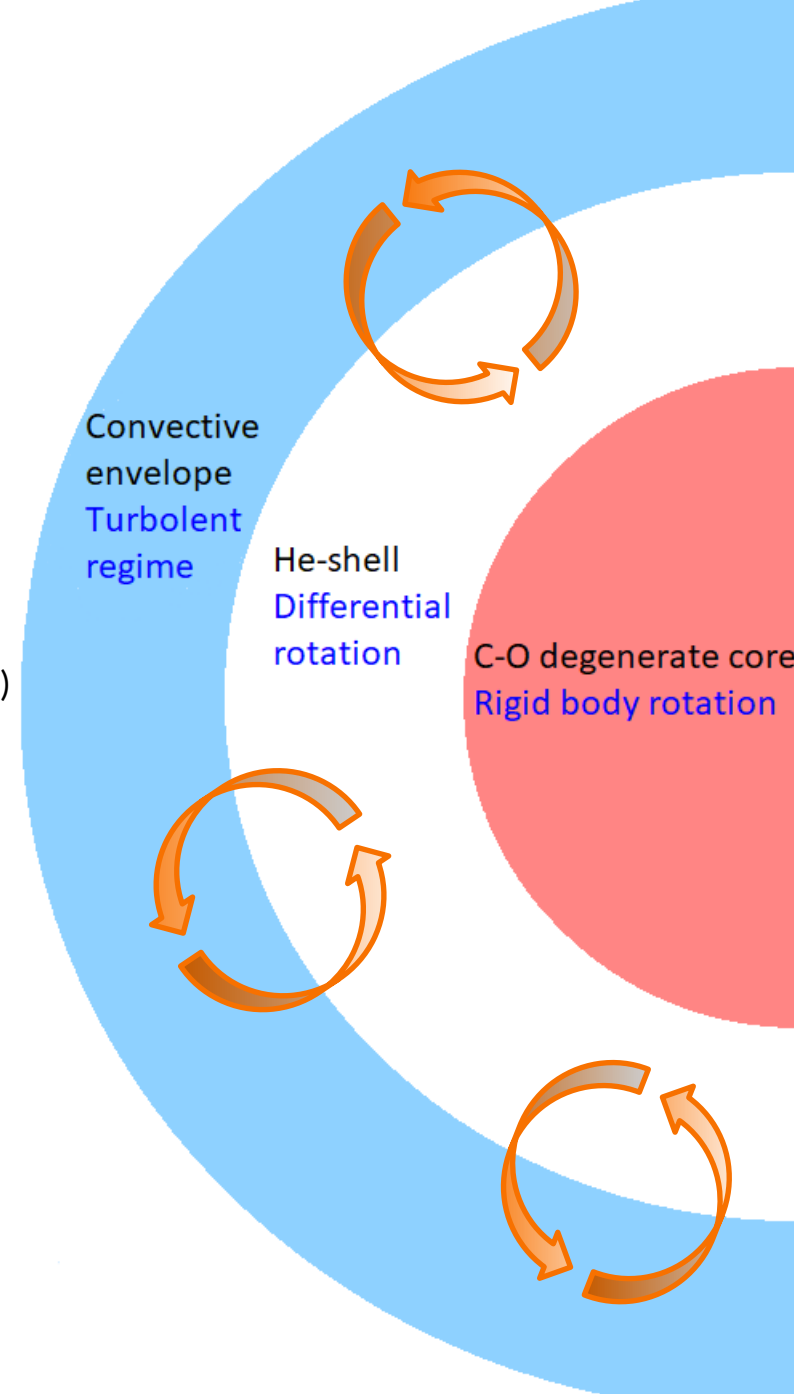
Which is the physical mechanism?

Classic models **assume** the ^{13}C -pocket formation

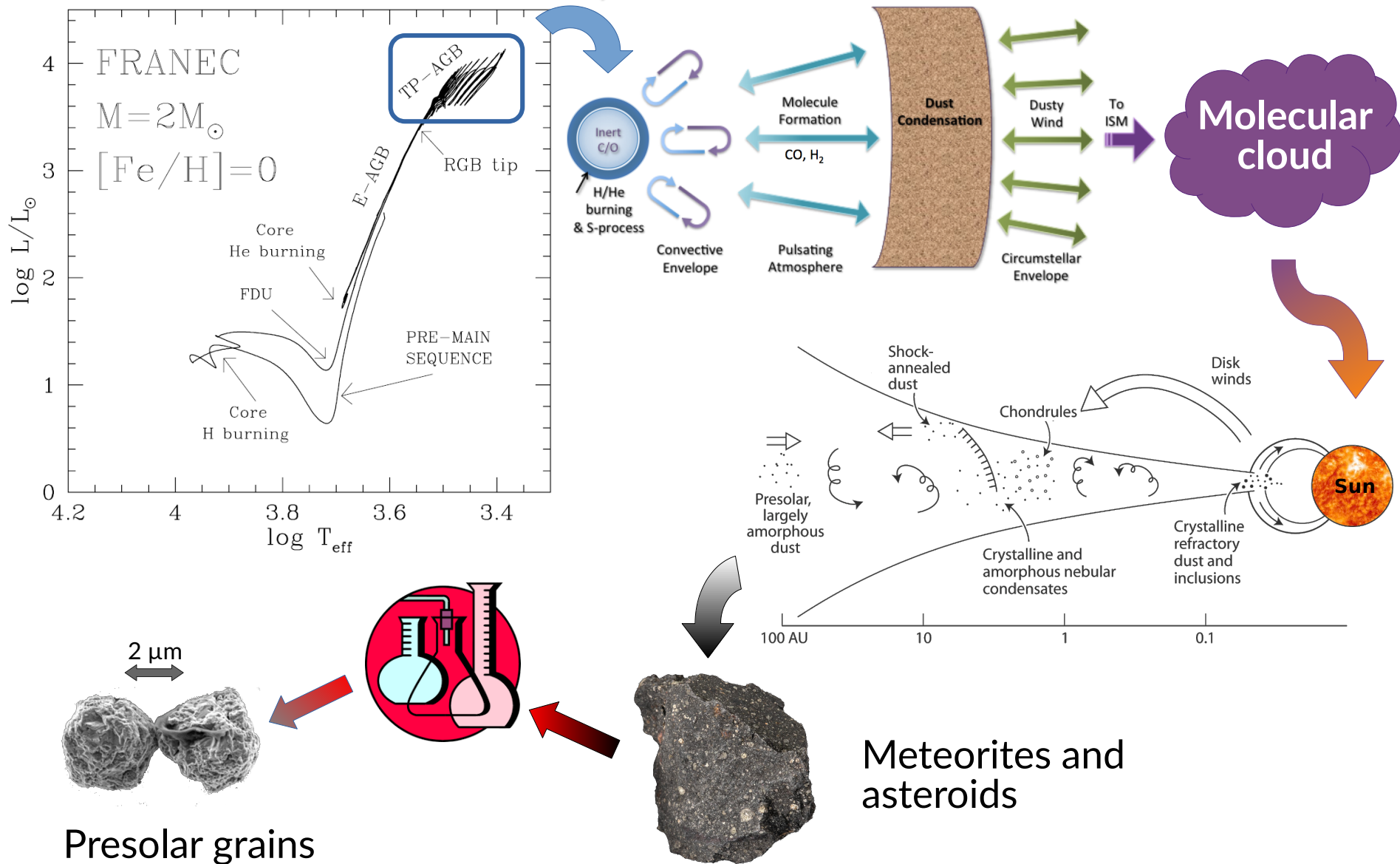
Many recent physical approaches:

- Opacity-induced overshoot (Cristallo+ 2009, 2011, 2015)
 - Convective Boundary Mixing (Battino+ 2016)
 - Magnetic fields (Trippella+ 2016; Palmerini+ 2018)
- ➔ bottom-up mechanism through
magnetic buoyancy

- 1) Rotational shears promote magnetic fields
- 2) Magnetic structures reach the envelope
- 3) Protons are injected into the He-rich region



AGB stars and presolar SiC grains



FRUITY models with convective overshooting

- We considered **convective overshooting only** to the partial mixing of hydrogen.

- **Exponential decay** of the convective velocity



$$v = v_{\text{CE}} \exp\left(-\frac{\Delta r}{\beta H_P}\right)$$

(Straniero+ 2006, Cristallo+ 2009)

- We considered **isotopic data** including Ni, Sr, Zr, Mo and Ba isotope ratios in **presolar SiC grains** → 10% uncertainty

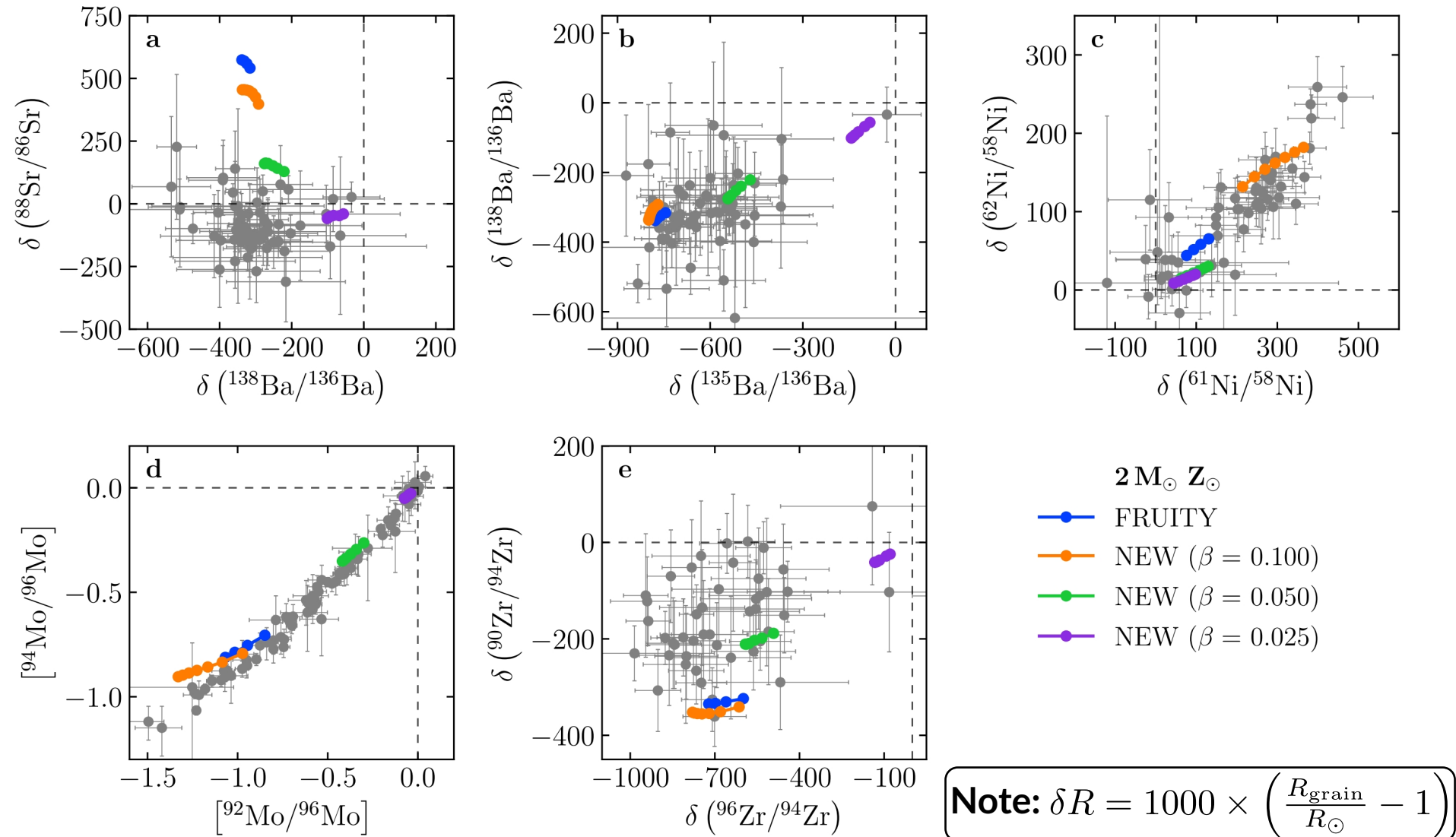
- **One stellar model:** $2 M_{\odot}$ and $Z = Z_{\odot}$

- **Updated** solar-scaled mixture, mass-loss, EOS, nuclear reaction rates

- **Different** values of β

SiC Grains I

- Isotopic data including Ni, Sr, Zr, Mo, and Ba isotope ratios in presolar SiC grains
- Stellar models with same initial mass ($2 M_{\odot}$) and solar metallicity



Magnetic buoyancy

- MagnetoHydroDynamics (**MHD**) solutions (Nucci & Busso 2014):
 - No numerical approximations (exact analytic solution)
 - Simple geometry: **toroidal magnetic field**

Equations:

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{v}) = 0$$

$$\frac{\partial \mathbf{B}}{\partial t} - \nabla \times (\mathbf{v} \times \mathbf{B}) - \nu_m \Delta \mathbf{B} = 0$$

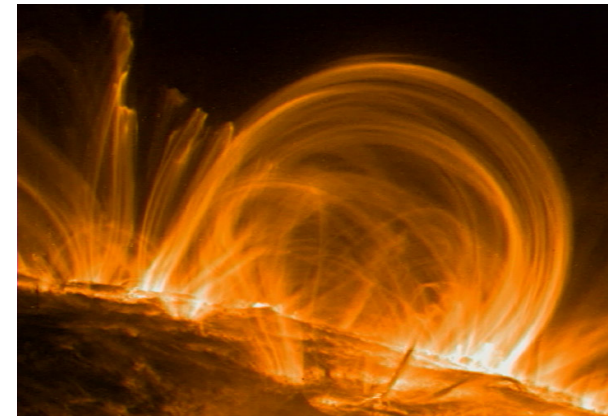
$$\rho \left[\frac{\partial \mathbf{v}}{\partial t} + (\mathbf{v} \cdot \nabla) \mathbf{v} - c_d \mathbf{v} + \nabla \Psi \right] - \mu \Delta \mathbf{v} + \nabla P + \frac{1}{4\pi} \mathbf{B} \times (\nabla \times \mathbf{B}) = 0$$

$$\rho \left[\frac{\partial \epsilon}{\partial t} + (\mathbf{v} \cdot \nabla) \epsilon \right] + P \nabla \cdot \mathbf{v} - \nabla \cdot (\kappa \nabla T) + \frac{\nu_m}{4\pi} (\nabla \times \mathbf{B})^2 = 0$$

Solutions:

$$v_r = v_p \left(\frac{r_p}{r} \right)^{k+1}$$

$$B_\varphi = B_{\varphi,p} \left(\frac{r}{r_p} \right)^{k+1}$$




where k is the exponent of the density distribution:

$$\rho(r) = \frac{\rho_p}{r_p^k} r^k$$

Magnetic-buoyancy-induced mixing


→ **Magnetic** contribution (Vescovi+ 2020) to the dowflow velocity \mathbf{v}_d , acting when the density distribution is $\rho \propto r^k$:


$$v_d(r) = u_p \left(\frac{r_p}{r} \right)^{k+2}$$

Parameters:

- Layer “p” at the deepest coordinate from which buoyancy starts

(can be identified from the corresponding **critical toroidal B_φ** value)


$$B_\varphi \gtrsim \left(4\pi \rho r N^2 H_p \frac{\eta}{K} \right)^{1/2}$$

- Starting velocity u_p of the buoyant material

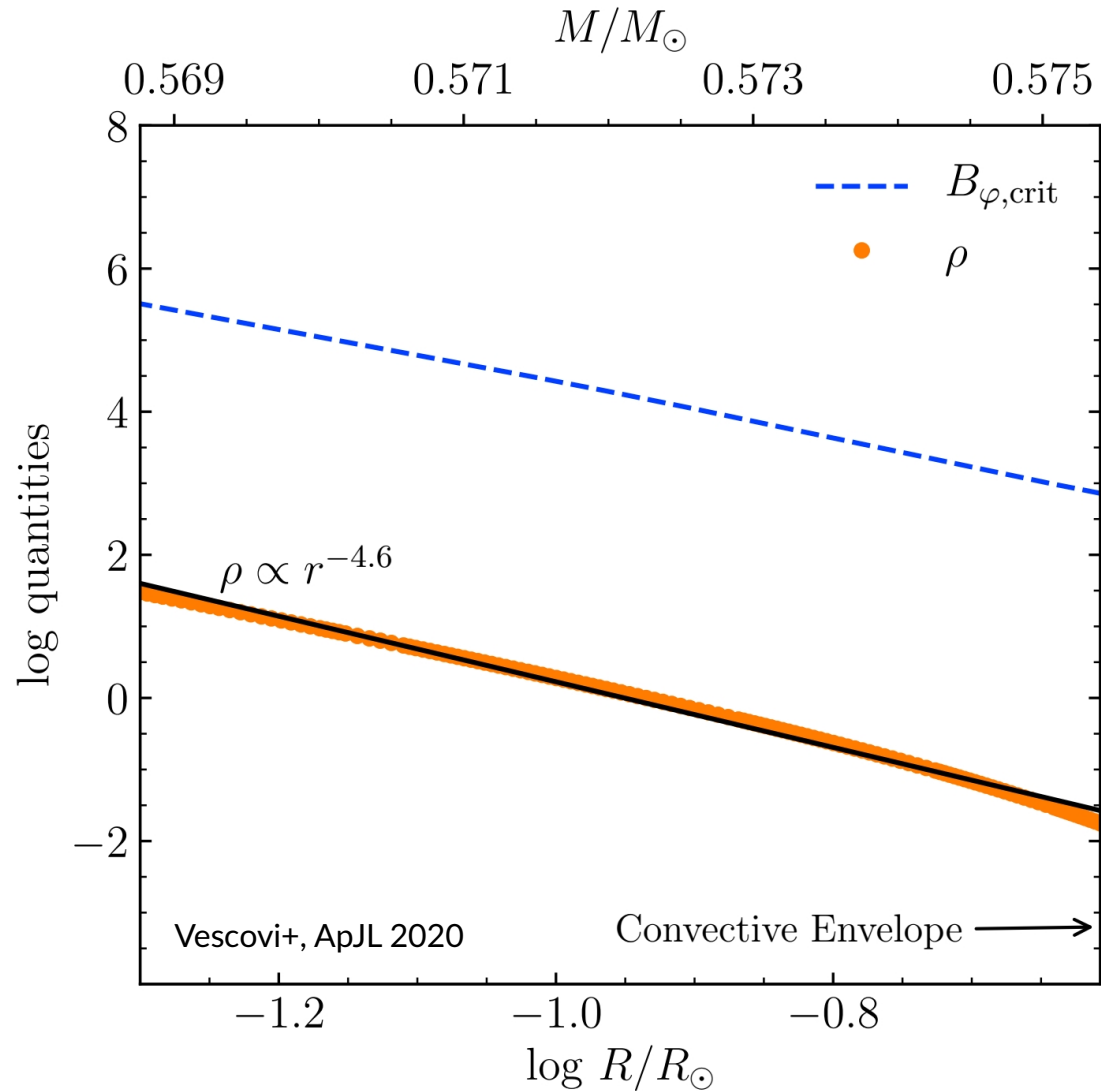
→ Calibration is needed!

→ We ran various tests with different parameter values:

- $u_p = 1, 3, 5, 8, 12 \times 10^{-5}$ cm/s
- $B_\varphi = 2, 5, 10, 15 \times 10^4$ G

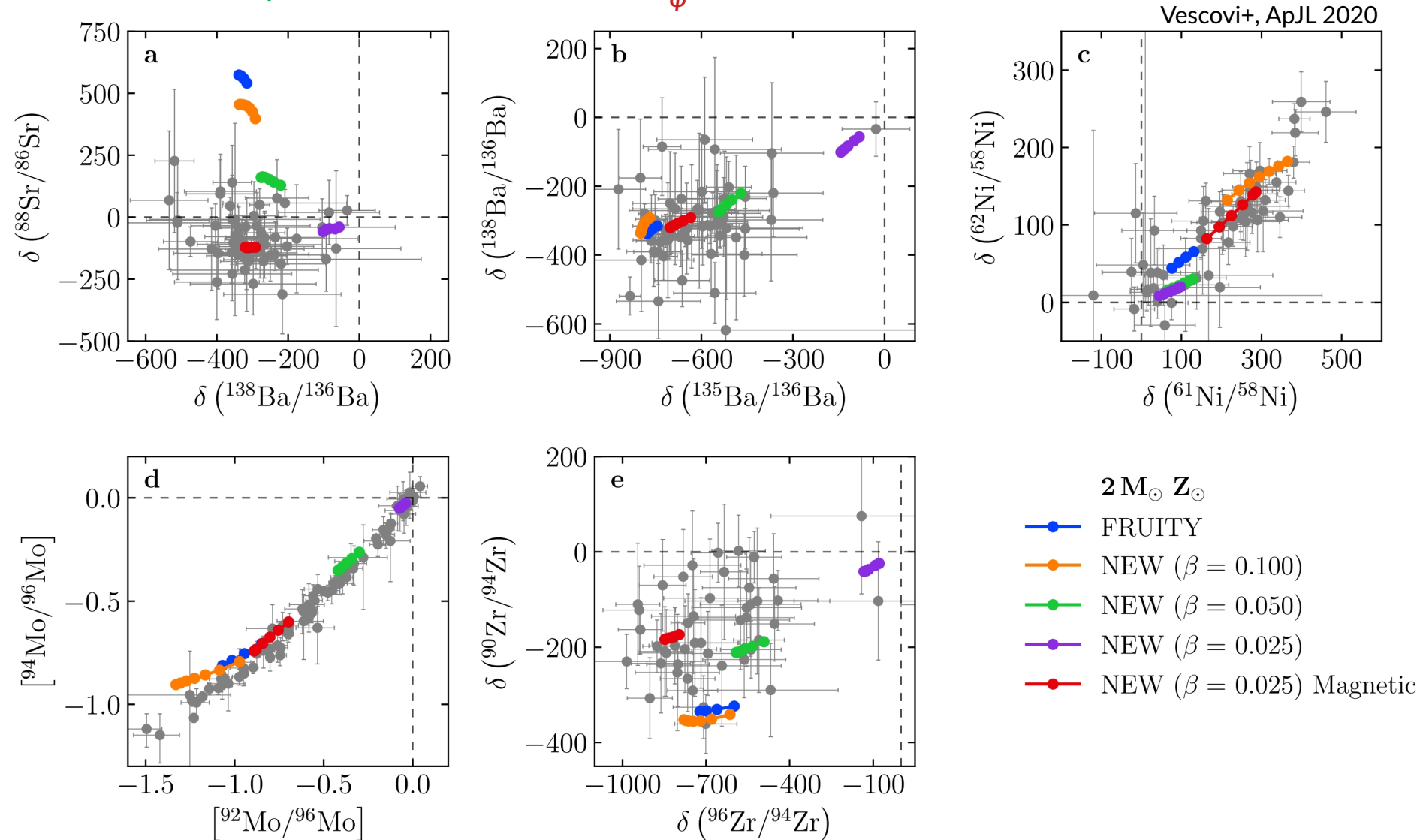
Critical toroidal B -field

- Stellar model: $2 M_{\odot}$ $Z = Z_{\odot}$
- The critical B_{φ} necessary for the onset of magnetic buoyancy instabilities, in radiative zone below the convective envelope **varies from $\sim 10^4$ G to $\sim 10^6$ G**
- Different values of B_{φ} correspond to different values of r_p
- The strength of B_{φ} **determines the extension of the mixed zone and, in turn, of the ^{13}C -pocket**



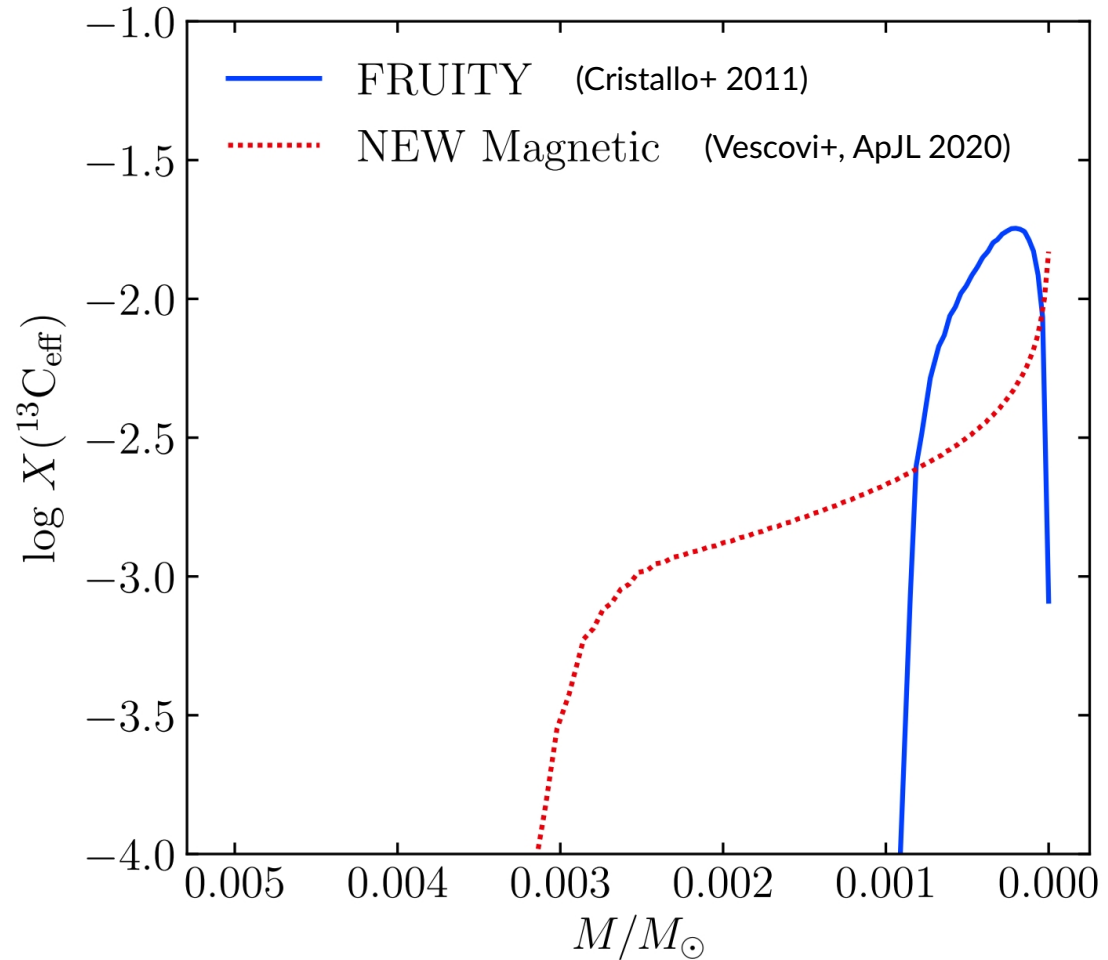
SiC Grains II

- Magnetic contribution accounts for SiC data!!
- Best fit for $u_p = 5 \times 10^{-5}$ cm/s and $B_\phi = 5 \times 10^4$ G



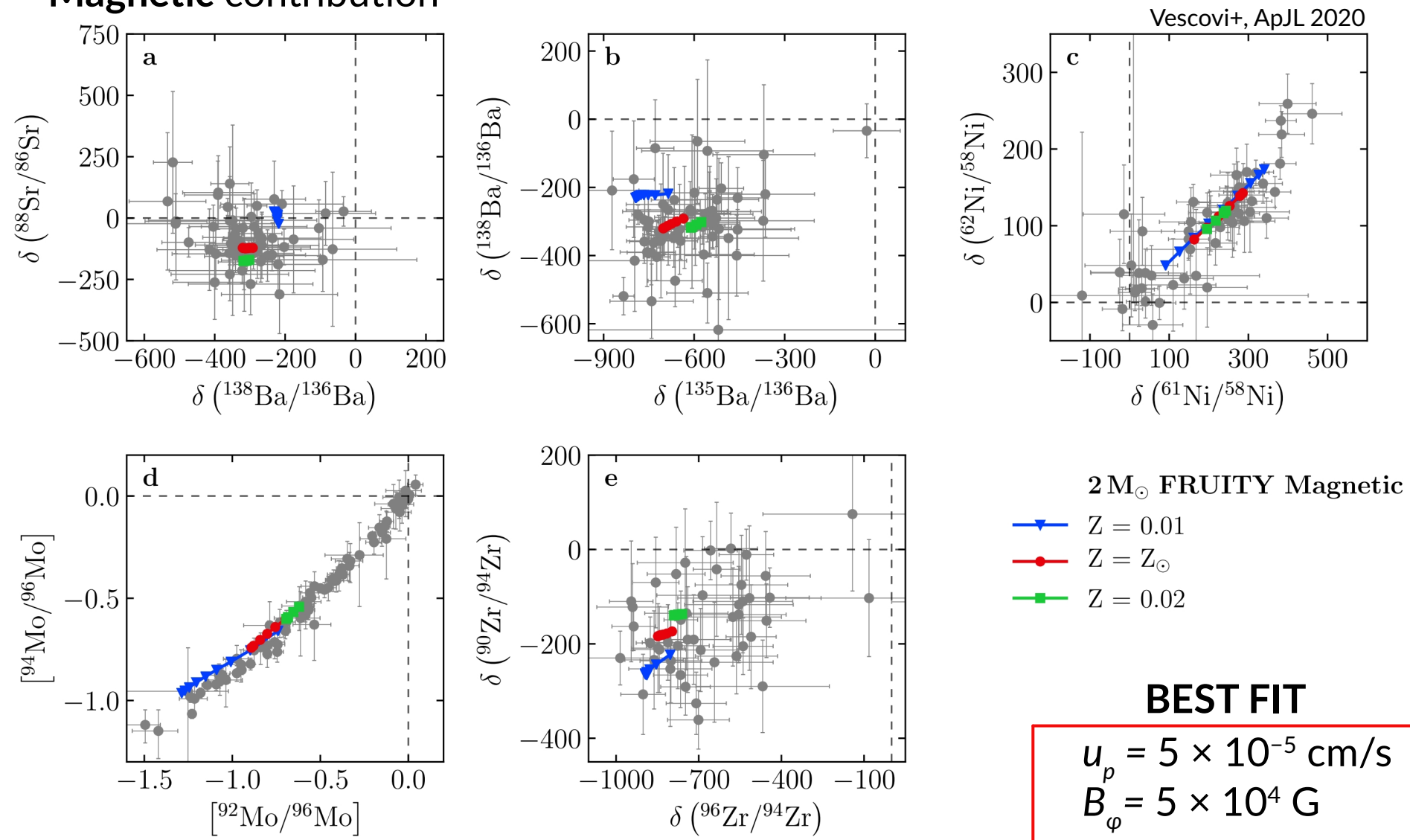
The ^{13}C -pocket: shape

- Effective ^{13}C in the ^{13}C -pocket region → i.e. the difference between the number fractions of ^{13}C and ^{14}N in the pocket
- New “Magnetic” pocket presents are **more extended and flatter**



SiC Grains III

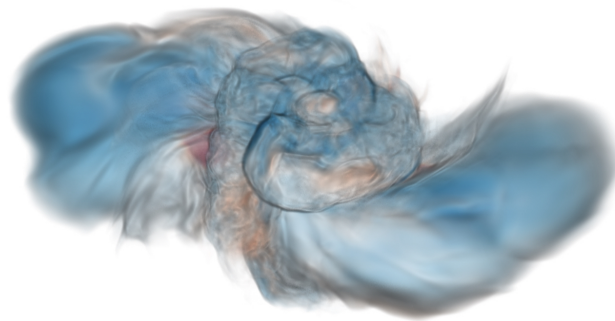
- Stellar models with same initial mass ($2 M_{\odot}$) and close-to-solar metallicity
- Magnetic contribution



Summary II

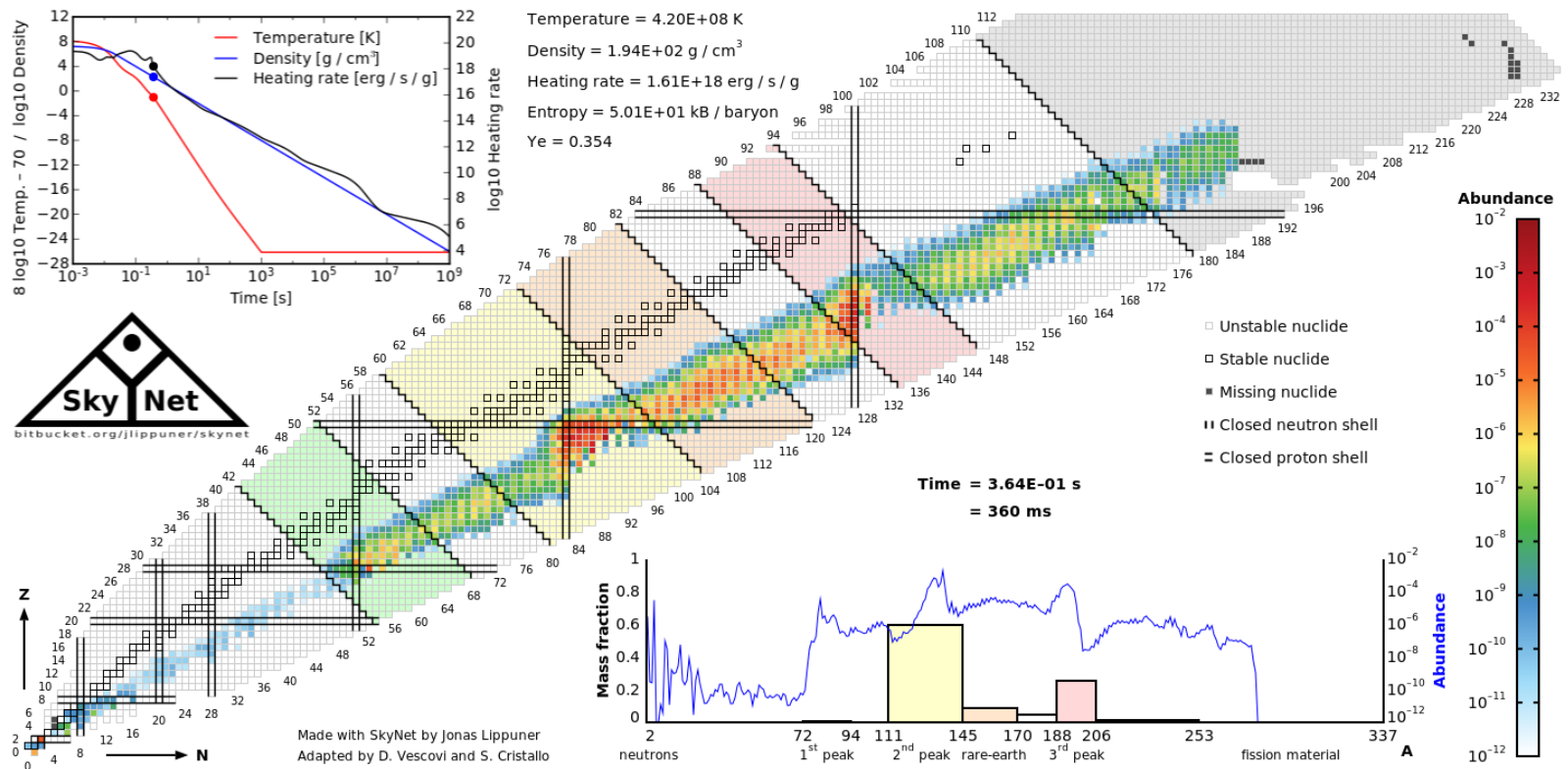
- **First numerical simulations** of the formation of a magnetically induced ^{13}C -pocket in a stellar evolutionary code with fully coupled nucleosynthesis
- **Magnetic fields of the order of 10^5 G** (like in the solar tachocline) can induce the formation and buoyant rise of magnetic flux tubes in the He-intershell of AGB stars.
- Such tubes are fast enough to guarantee, by mass conservation, the downward penetration of sufficient protons to form a sizable ^{13}C -pocket
- **Unique choice** of the field strength and initial buoyant velocity
- New magnetic models provide a consistent explanation to the **majority of the heavy-element isotope data** detected in presolar SiC grains from AGB stars

Kilonovae and production of very light elements in Neutron Star Mergers



r-process: basic ideas

- key reactions: $(A, Z) + n \leftrightarrow (A + 1, Z) + \gamma$
- r-process requires initial high n_n and T
 - high n_n : $\tau_{(n,\gamma)} \ll \tau_{\beta\text{-decay}}$
- equilibrium freeze-out: n_n drops and β -decays take over



Neutron star mergers as *r*-process site

r-process nucleosynthesis in depends mainly on three physical quantities:

1) entropy $s \sim T^3/\rho$

2) Electron fraction $Y_e \sim n_p/(n_n+n_p)$

3) Dynamical expansion timescale τ_{dyn}

Possible scenarios	high entropy <i>r</i> -process	low entropy <i>r</i> -process
	hot CCSN winds	BNS and BHNS mergers MHD supernovae

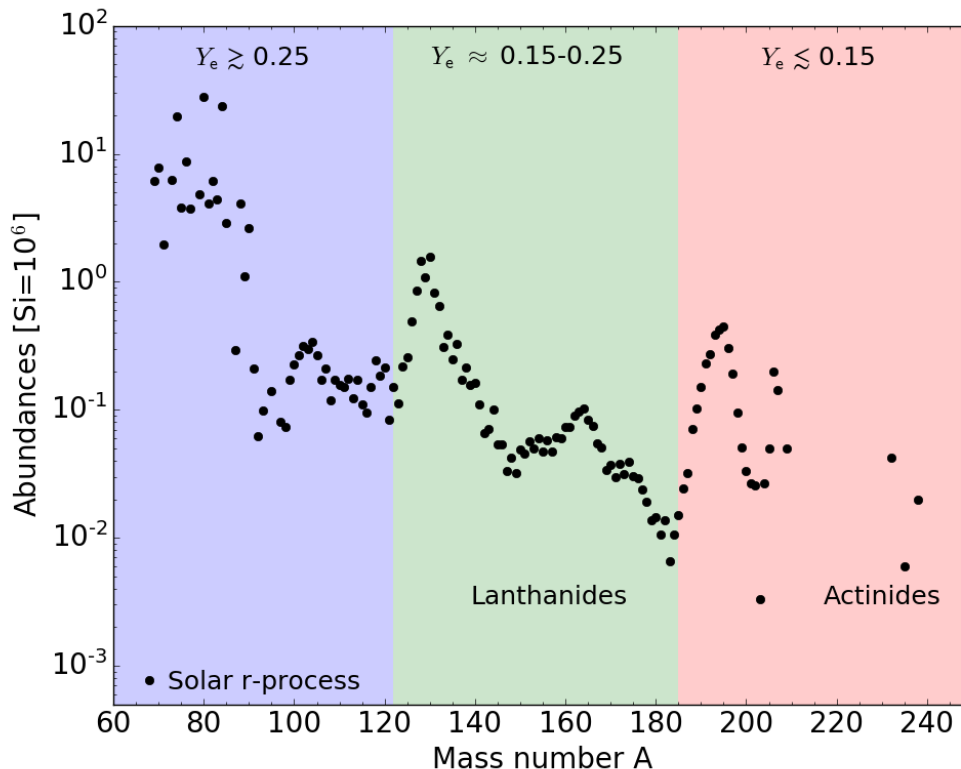


First evidences of *r*-process
nucleosynthesis in kilonova
from GW170817

r-process nucleosynthesis in BNS mergers

Y_e dominant parameter

- $Y_e < 0.15$: robust r -process, due to several fission cycles
- $Y_e \lesssim 0.25$: 2nd and 3rd r -process peaks, but no first
- $Y_e \gtrsim 0.25$: up to 2nd r -process peak

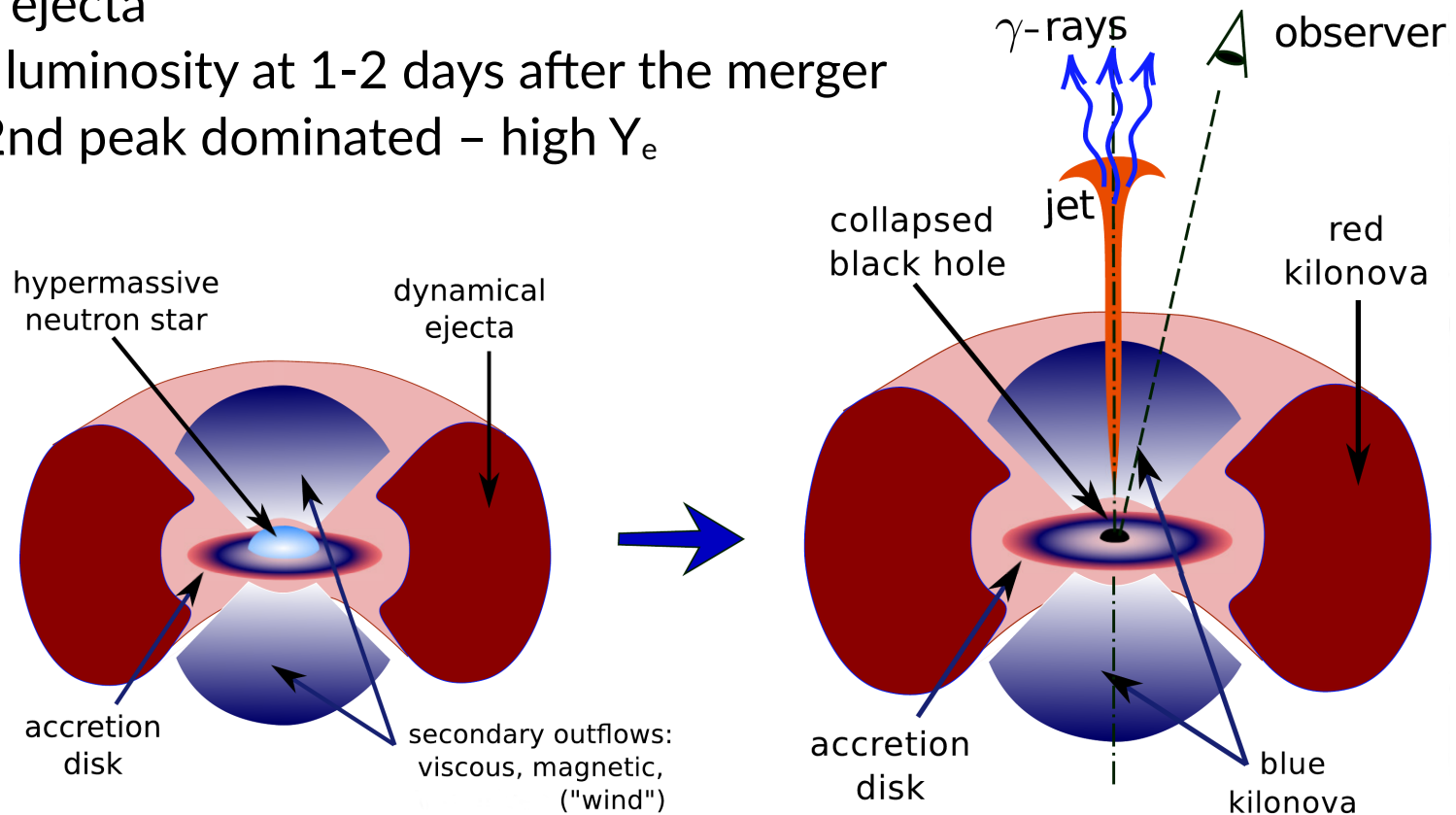


Production of lanthanides dramatically changes photon opacity κ_γ

- **no lanthanides:**
low opacity ($\kappa_\gamma \lesssim 1 \text{ cm}^2/\text{g}$)
- **presence of lanthanides:**
increased opacity ($\kappa_\gamma \gtrsim 10 \text{ cm}^2/\text{g}$)

BNS merger + kilonova

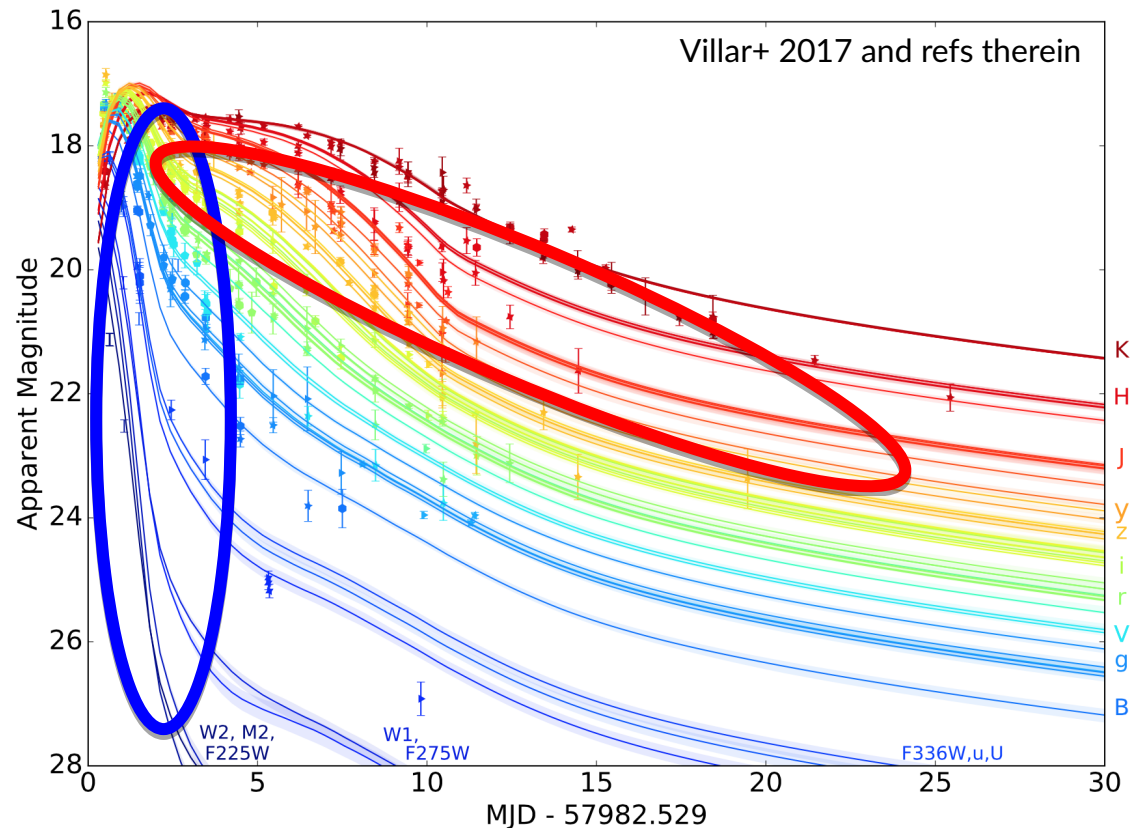
- **Red emission:**
 - Tidal ejecta
 - Peak luminosity at days - 1 week after the merger
 - Lanthanide dominated – low Y_e
- **Blue emission:**
 - Polar ejecta
 - Peak luminosity at 1-2 days after the merger
 - 1st/2nd peak dominated – high Y_e



Courtesy of
O. Korobkin

Properties of GW170817/AT2017gfo

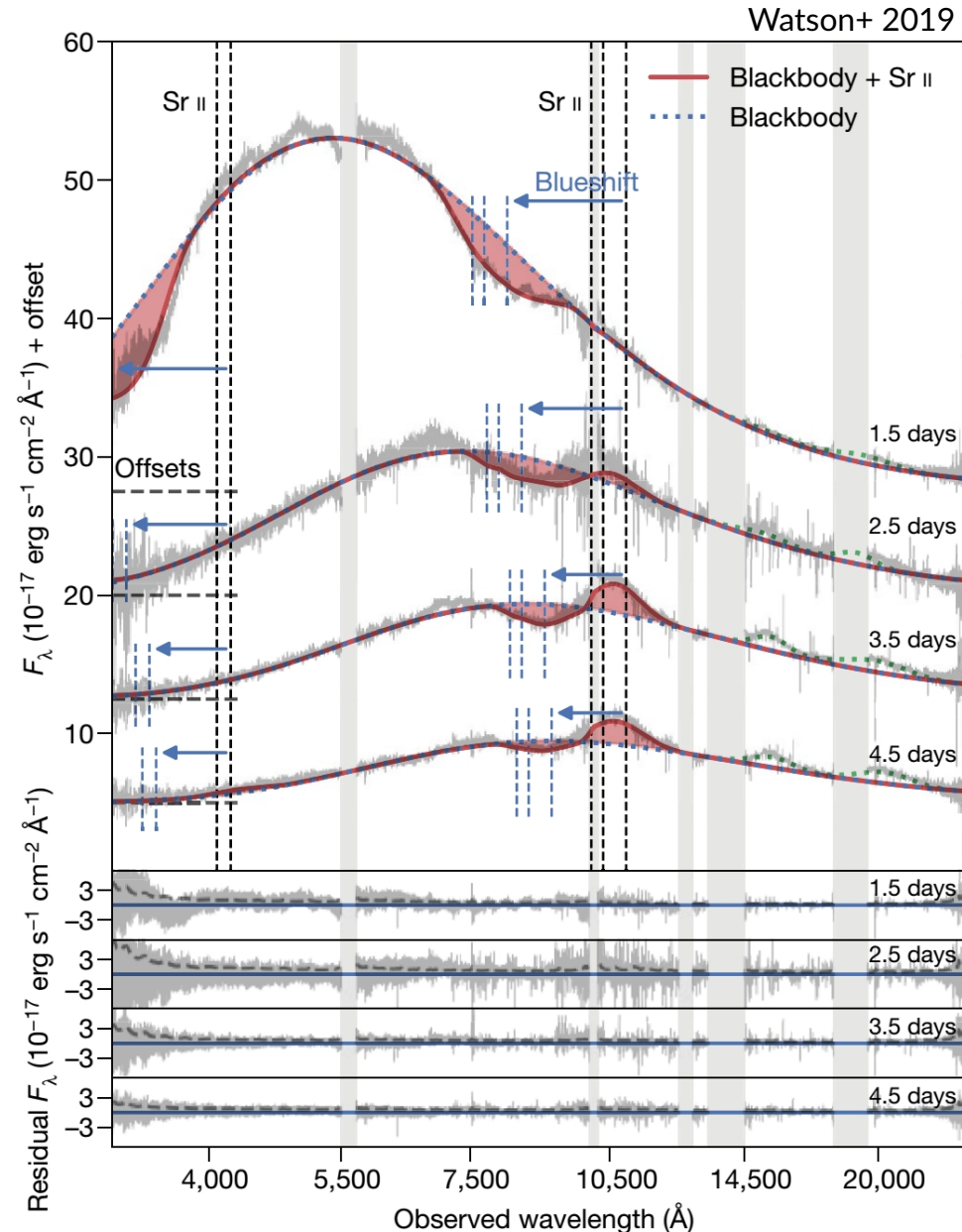
- 17/08/17, GW+EM detection of an event compatible with BNS merger (LVC PRL 2017)
- Blue component
- Red component
- Thermal emission by radiocative decay of heavy elements synthesized in multicomponent (2-3) ejecta



Properties of GW170817/AT2017gfo

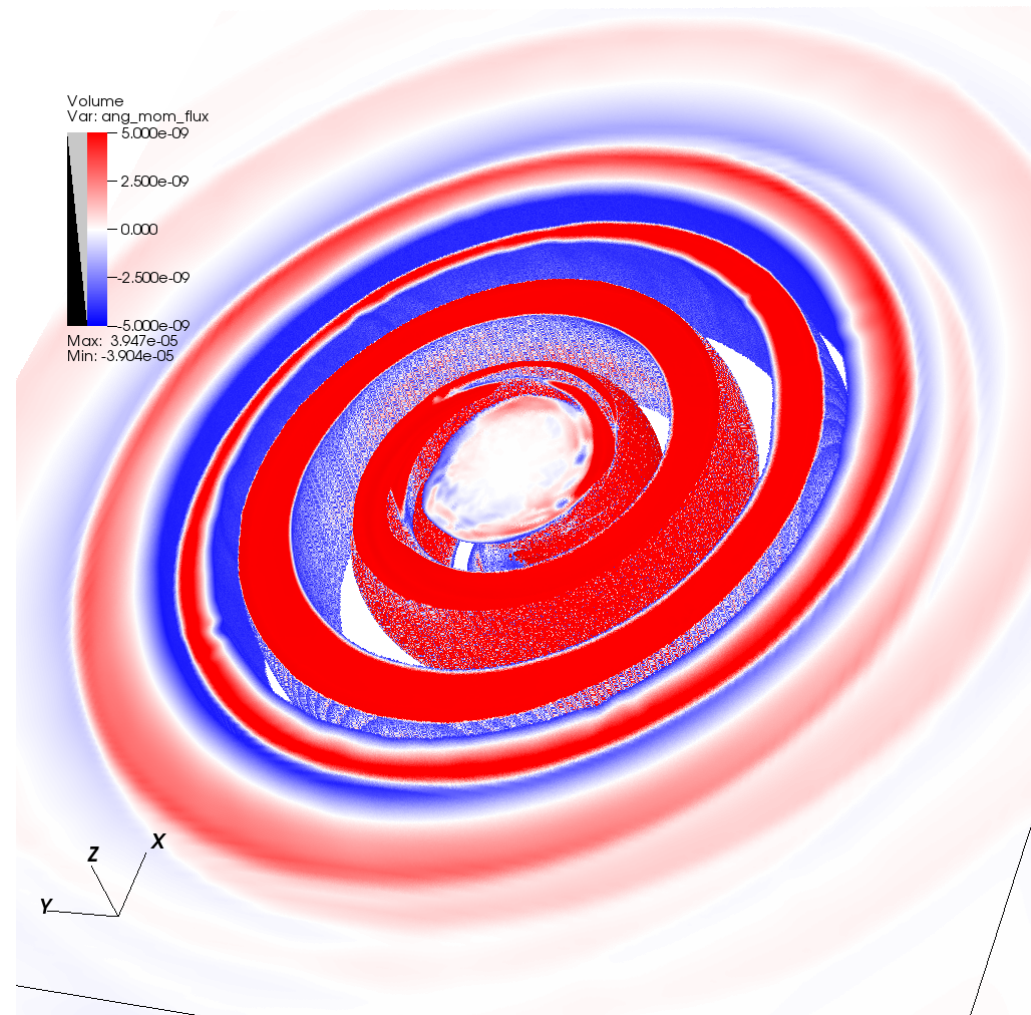
Spectral analysis hampered due to:

- Heavy elements have **forest of lines** hence strong blending
 - **Relativistic velocity** makes for extremely broad lines (multi-components and different velocities)
 - Atomic data are incomplete and uncertain
- The analysis of the spectrum at 1.5 days suggested the presence of **strontium** (Watson +2019)



Production of very light elements in kilonovae

- What about very light elements?
- The dynamical ejecta and spiral-wave wind are the earliest and fastest ejecta
 - transparent within the very first days and possibly providing key spectral features
- we investigated the production of light elements ($Z < 20$)
- connecting the thermodynamics conditions for their production to the binary properties (mass ratio and EOS)
- study their early detectability



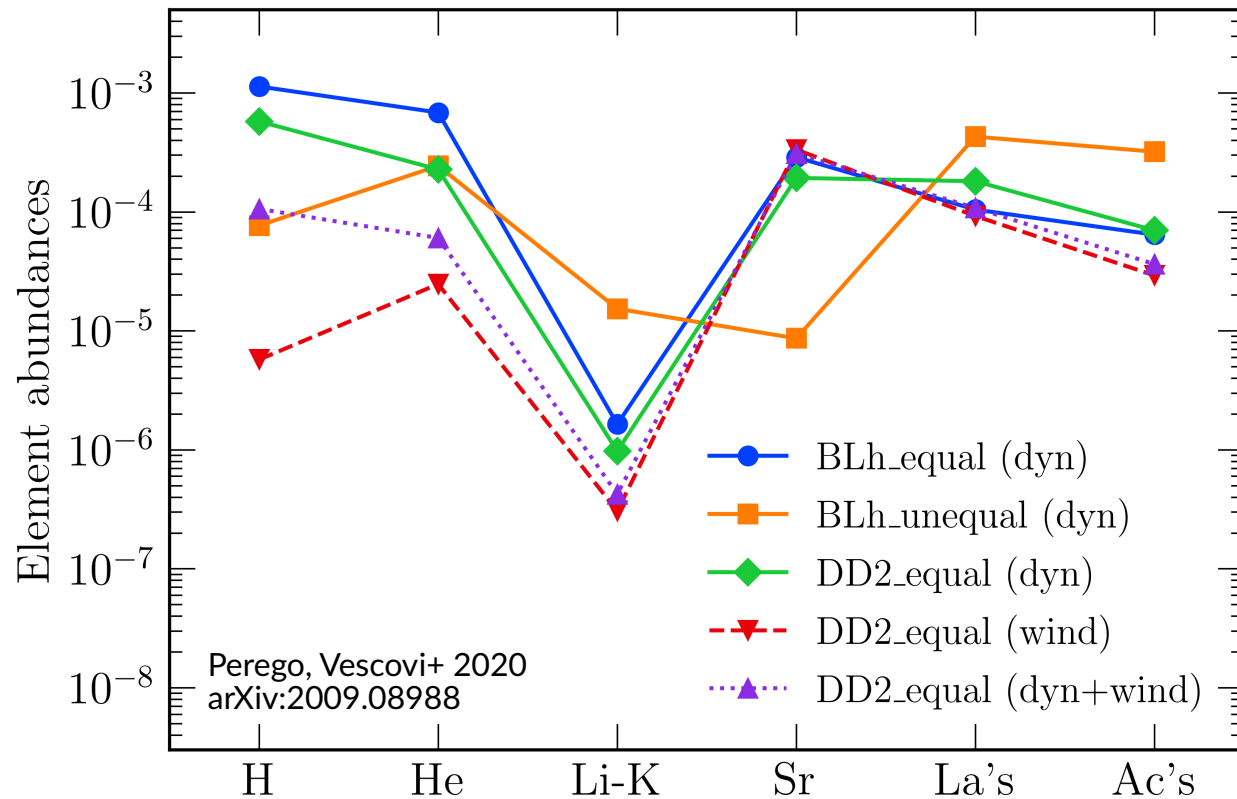
Spiral-wave wind (Nedora+ 2019, 2020)

Production of very light elements in kilonovae

- Three simulations:
 - 1) $M_1 = M_2 = 1.364 M_{\odot}$
Soft EOS (BLh)
 - 2) $M_1 = 1.856 M_{\odot}, M_2 = 1.020 M_{\odot}$
Soft EOS (BLh)
 - 3) $M_1 = M_2 = 1.364 M_{\odot}$
Stiff EOS (DD2)
- from each BNS simulations we extract mass distributions of the ejecta in the s , Y_e , τ_{dyn} space
- **time-dependent abundances** from their convolution with the yields tabulated with *SkyNet* (Lippuner & Roberts 2017)

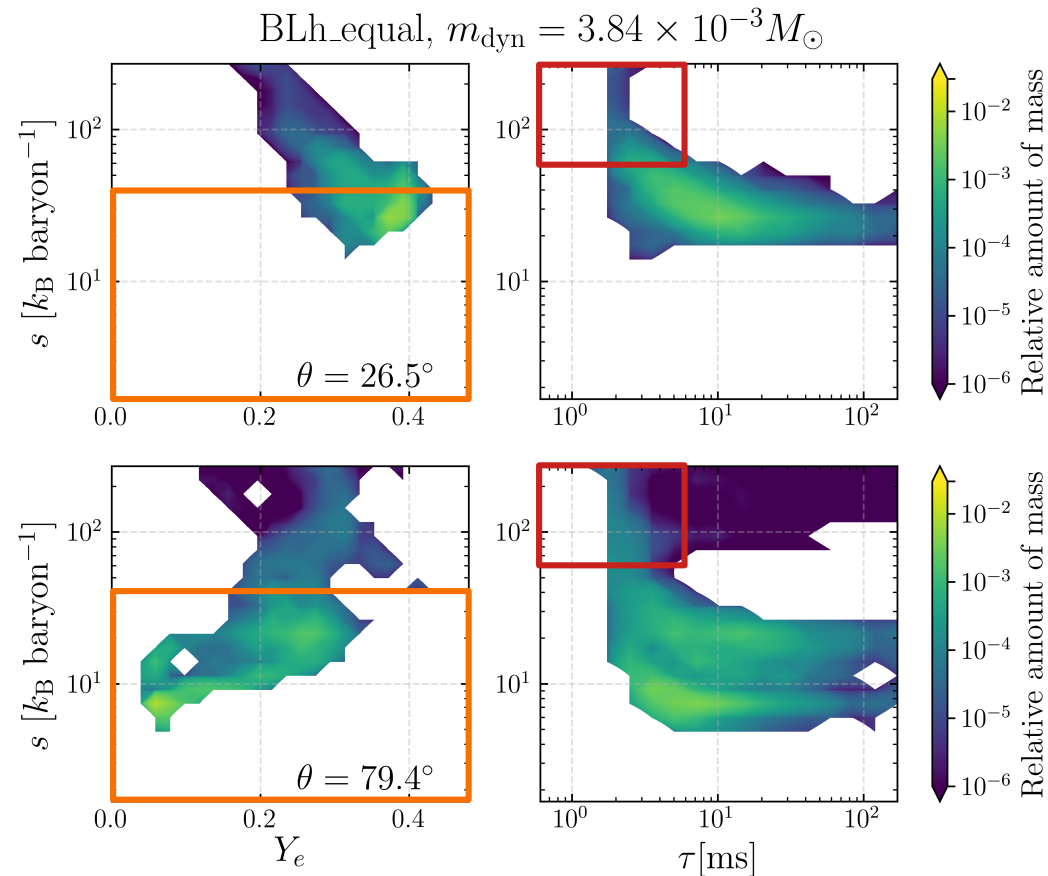
Production of very light elements in kilonovae

- **H and He are the most abundant species, comparable to Sr, lanthanides, and actinides**
- **elements between lithium and potassium are usually several orders of magnitudes less abundant**



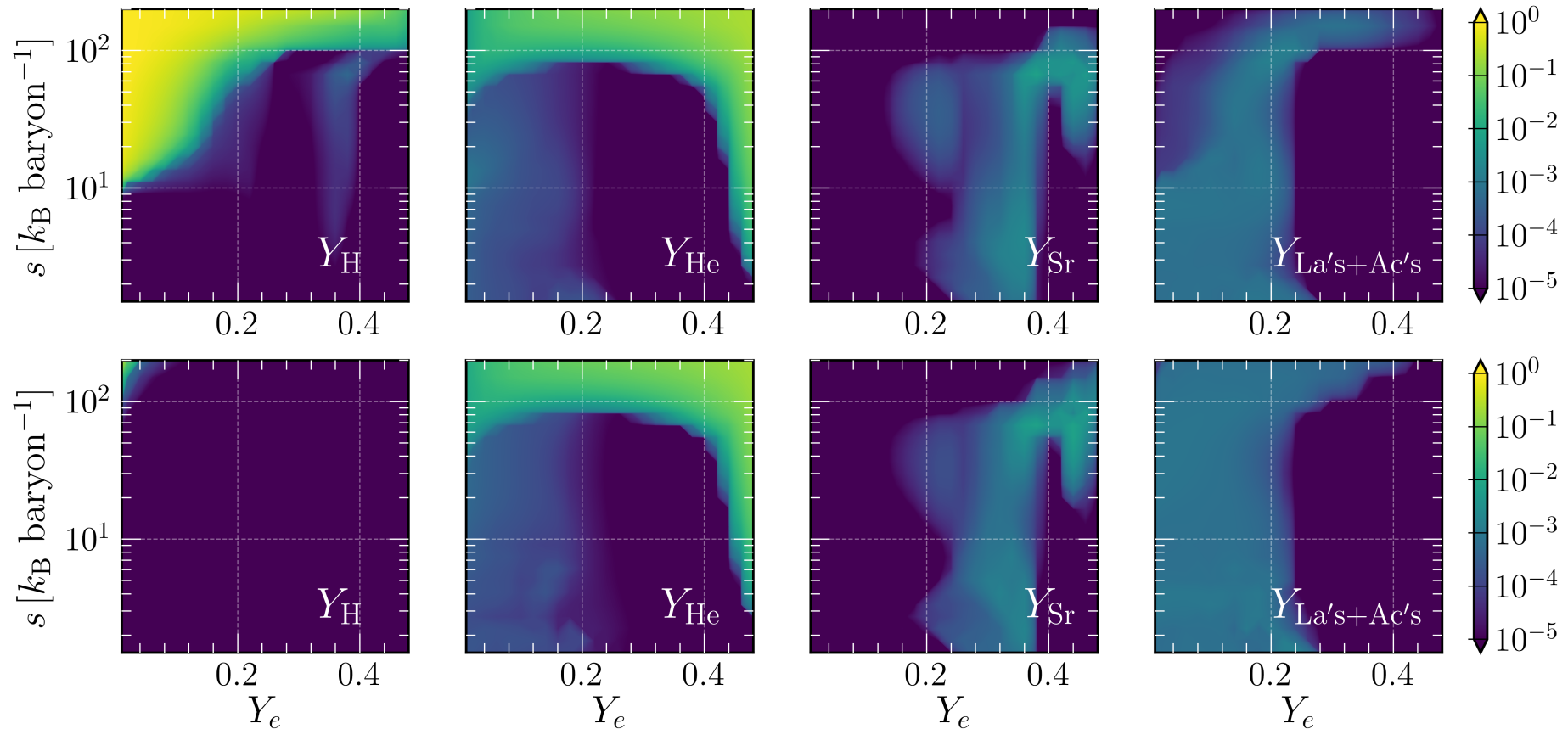
Conditions of the ejecta from BNS merger simulations

- The **bulk** of the ejecta has low entropy ($s < 40 \text{ k}_\text{B} \text{ baryon}^{-1}$) and is neutron rich
- Equatorial ejecta are usually characterized by lower Y_e and lower entropy
- However, at both angles a high-entropy tail (with $s > 60 \text{ k}_\text{B} \text{ baryon}^{-1}$) expanding at high speeds ($\tau < \sim 5 \text{ ms}$) is visible



Origin of H, He, and Sr

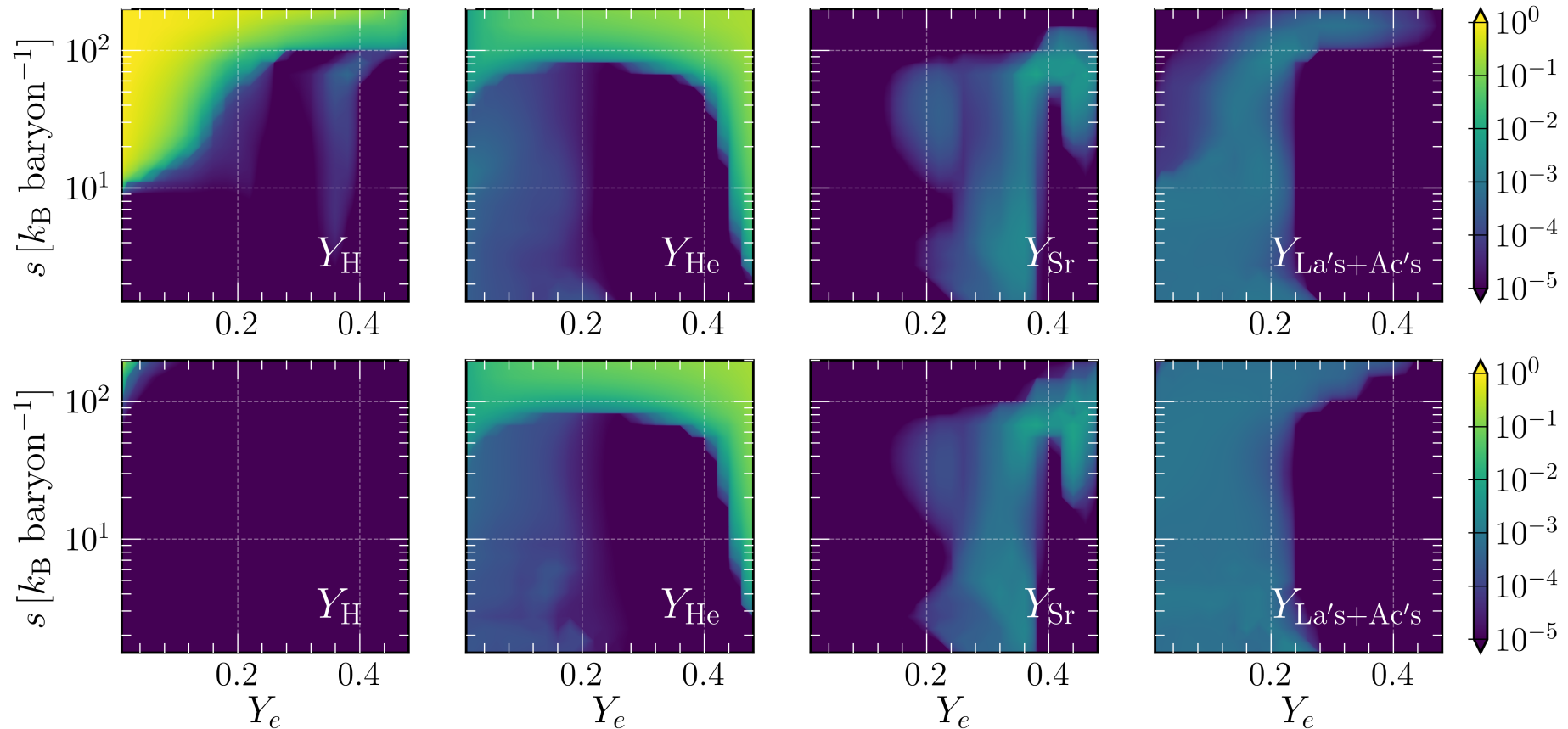
Abundances at 2 days for $\tau = 1.0$ ms (top) and $\tau = 11.4$ ms (bottom) trajectories



- Abundances for individual trajectories characterized by different (s, Y_e, τ) sets
- For $Y_e \gtrsim 0.22$ Sr is robustly produced for all entropies

Origin of H, He, and Sr

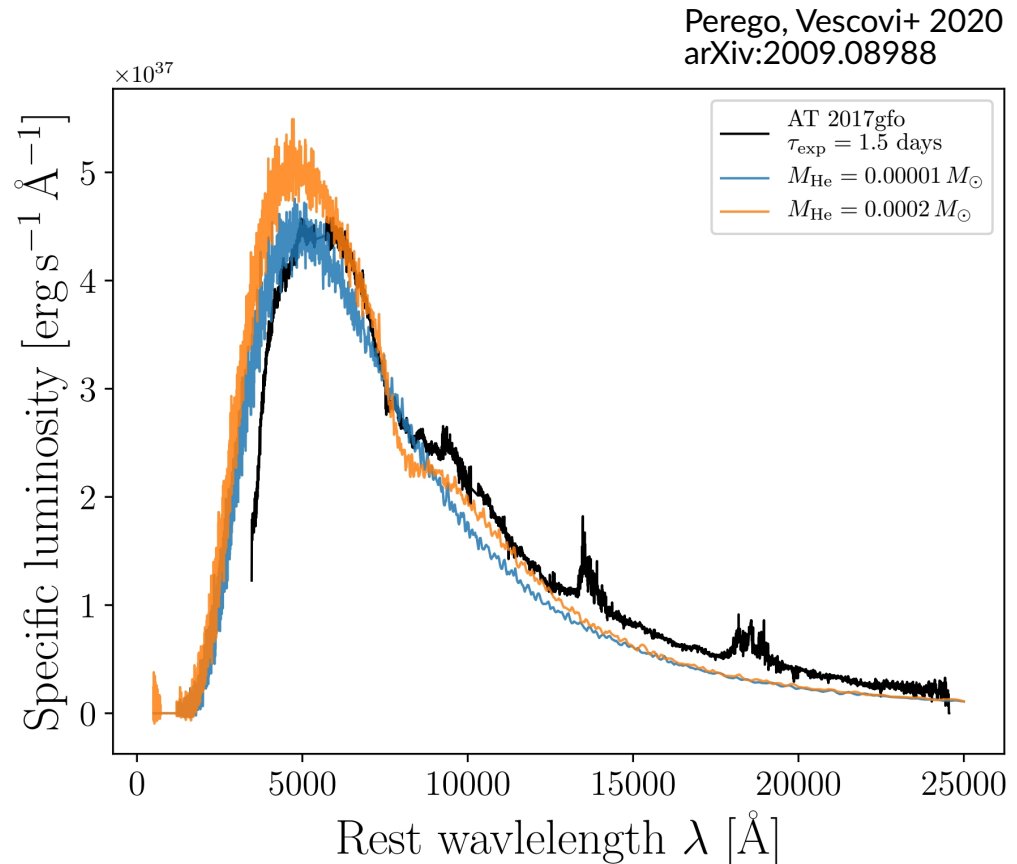
Abundances at 2 days for $\tau = 1.0$ ms (top) and $\tau = 11.4$ ms (bottom) trajectories



- The presence of **H** in the ejecta is related with **high- s** and **low- Y_e**
- He production can happen both in association or in the absence of heavy elements

Detecting H, He, and Sr in kilonova spectra

- The amount of Sr predicted by ab-initio BNS models is **consistent** with the one required by the analysis reported in Watson+ 19
- He and then H could **recombine** in atomic form after a **few hours**
- However, they probably **never contribute** to the kilonova spectrum
- Presence of H/He lines
→ Supernovae



Summary III

- We considered results of Numerical Relativity (NR) simulations of BNS assuming different mass-ratio and EOS
- In BNS mergers H, He, and Sr can be synthesized
- The amount of Sr is **consistent** with the one required to explain early spectral features in the kilonova of GW170817
- H and He probably **never contribute** to the kilonova spectrum formation unless strong non-LTE effects appear or a dramatic EOS softening boosts the presence of fast expanding, high- s matter
- Key result to organize and prioritize future observational campaigns for the electromagnetic counterparts of GW events

Backup Slides

Standard Solar Model (SSM)

- Stellar model obtained by numerical integration of the equations describing the physical and chemical structure of the Sun as well as its time evolution

$$\begin{aligned}\frac{\partial r}{\partial m} &= \frac{1}{4\pi r^2 \rho} \\ \frac{\partial P}{\partial m} &= -\frac{Gm}{4\pi r^4} \\ \frac{\partial l}{\partial m} &= \varepsilon_n - \varepsilon_\nu - \varepsilon_g \\ \frac{\partial T}{\partial m} &= -\frac{GmT}{4\pi r^4 P} \nabla\end{aligned}$$

$$\frac{\partial X_i}{\partial t} = R_i + M_i + DG_i$$

Nuclear reactions

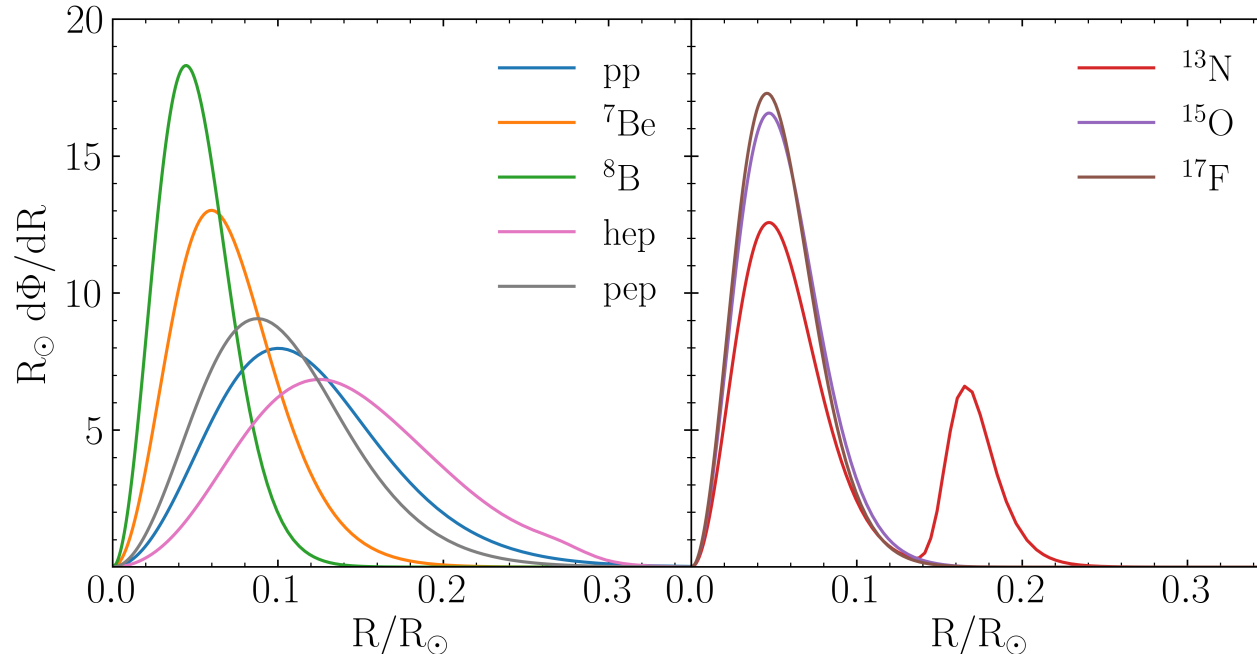
Mixing (convection)

Diffusion
Gravitational settling

- Evolve a model with $1 M_\odot$ starting from a chemically homogeneous model to present solar age with:
 - 1) good microphysics (reaction rates, equation of state (EOS), opacity)
 - 2) assumed mixing length (α_{ml}), initial helium (Y_{ini}) and metal (Z_{ini}) abundances
- Match R_\odot , L_\odot , and $(Z/X)_\odot$ to better than one part in 10^{-5}

SSM: predictions

- Physical quantities: temperature, pressure, density, luminosity, mass...
- Chemical profiles: $X(r)$, $Y(r)$, $Z_i(r) \rightarrow$ electron density profiles
- Helioseismic quantities: surface helium abundance, depth of the convective envelope, sound speed
- Neutrino fluxes: production profiles and integrated values



Sun's core metallicity

$$Z_{\odot}^c = 0.400 \times \frac{\Phi_{\text{CNO}}}{10^{10} \text{cm}^{-2} \text{s}^{-1}} \quad (\text{Gough 19})$$

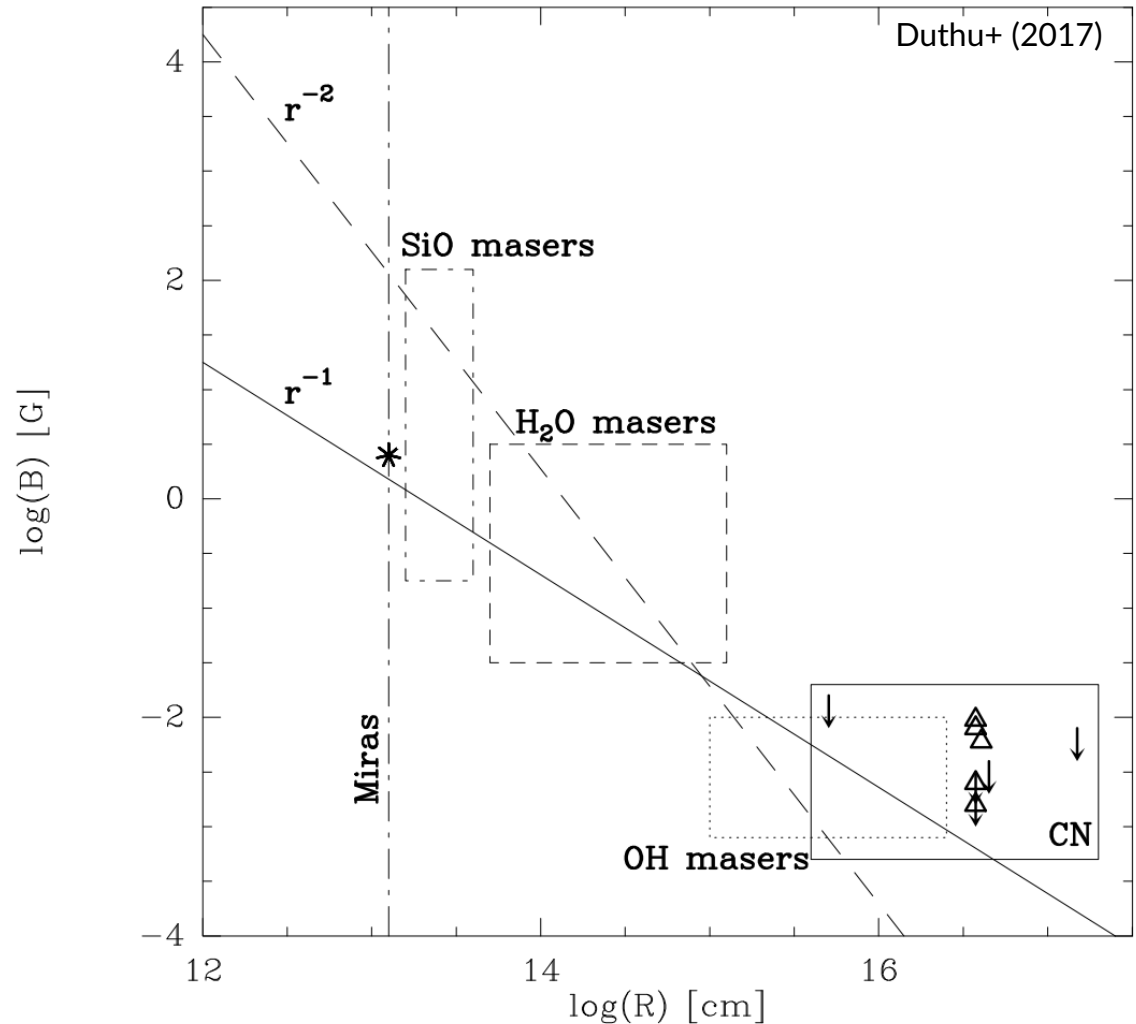


$$Z_{\odot}^c (\Phi_{\text{CNO}}^{\text{BX}}) = 0.028^{+0.012}_{-0.008}$$

Source	Z_c
GS98	0.0203 ± 0.0026
PLJ14	0.0179 ± 0.0021

Magnetic field in O-rich and C-rich AGB stars

- Generally, AGB magnetic field measurements come from maser polarization observations (SiO, H₂O and OH) (e.g. Vlemmings+ 2012)
- These have revealed a strong magnetic field throughout the circumstellar envelope
- **B-field at surface ~ few G**
- Although the maser observations trace only oxygen-rich AGB stars, recent CN Zeeman splitting observations (Duthu+ 2017) indicate that **similar strength fields are found around C-rich stars**

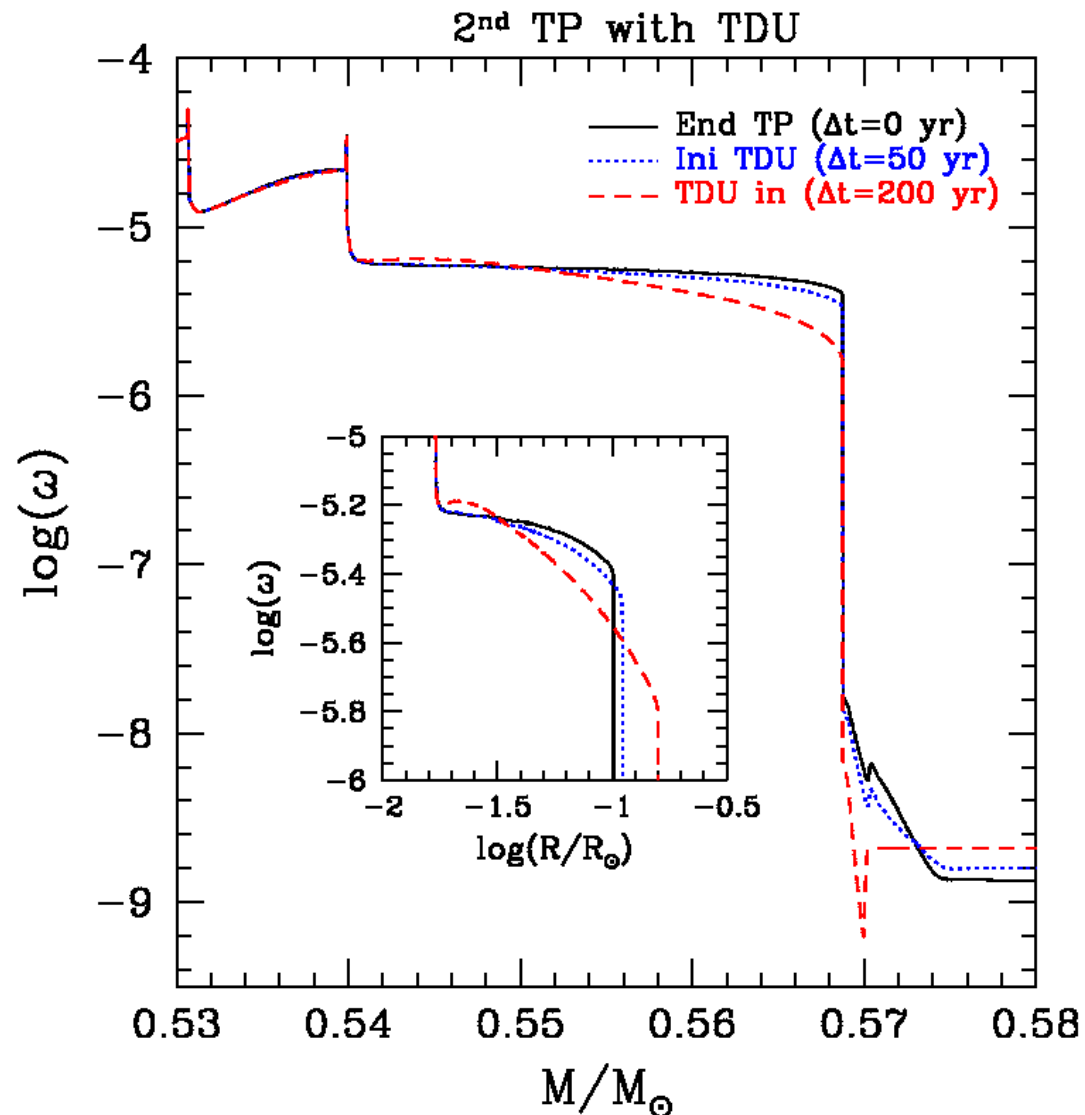


Generation of a toroidal B-field in the He-intershell

- Stellar model: $2.5M_{\odot}$ $Z=Z_{\odot}$
- Stretching of a preexisting **poloidal field** can generate a toroidal field

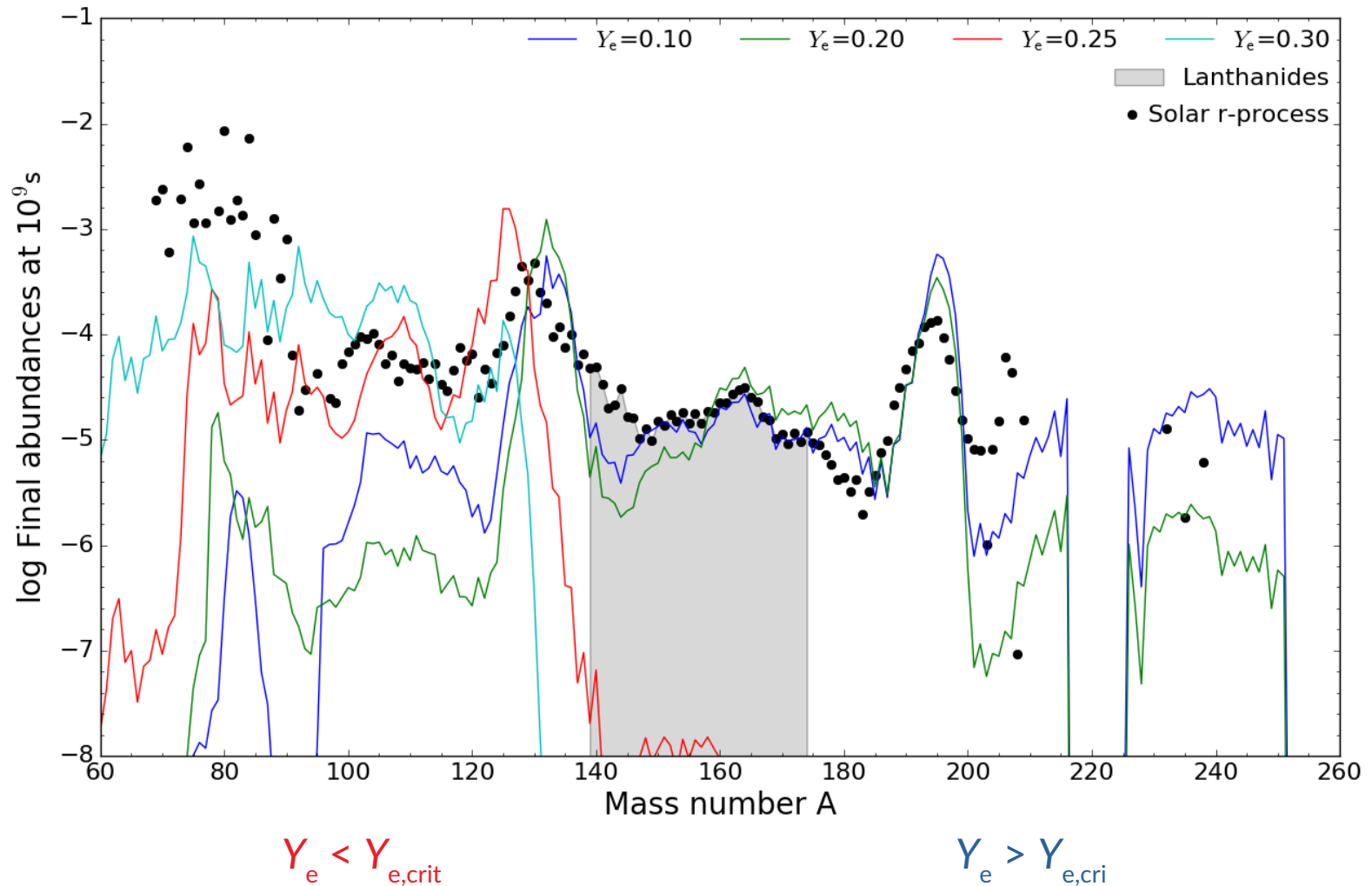
$$\Rightarrow \frac{\partial B_{\varphi}}{\partial t} = \frac{1}{r} \frac{\partial}{\partial r} (\Omega r^2 B_p) = \Omega q B_p$$
- Differential rotation in the He-intershell?
- An additional artificial viscosity of around $10^7 \text{cm}^2 \text{s}^{-1}$ provides a sufficient transport of angular momentum to match the core and envelope rotation rates for core He-burning stars (den Hartogh + 2019a,b)
- The **critical poloidal B_p** would be

$$\Rightarrow B_p \sim B_{\varphi} (\Omega q \Delta t)^{-1}$$
- A rough (preliminary) estimate gives a **B_p few hundreds times lower than B_{φ}** $\Rightarrow B_p \lesssim 1 \text{kG}$ Not implausible!!



Final abundances vs. electron fraction Y_e

→ Threshold value $Y_{e,\text{crit}} \approx 0.25$



“robust” r-process $A \gtrsim 130$

“weak” r-process $A \lesssim 130$

insensitive to details of trajectory

sensitive to details of trajectory

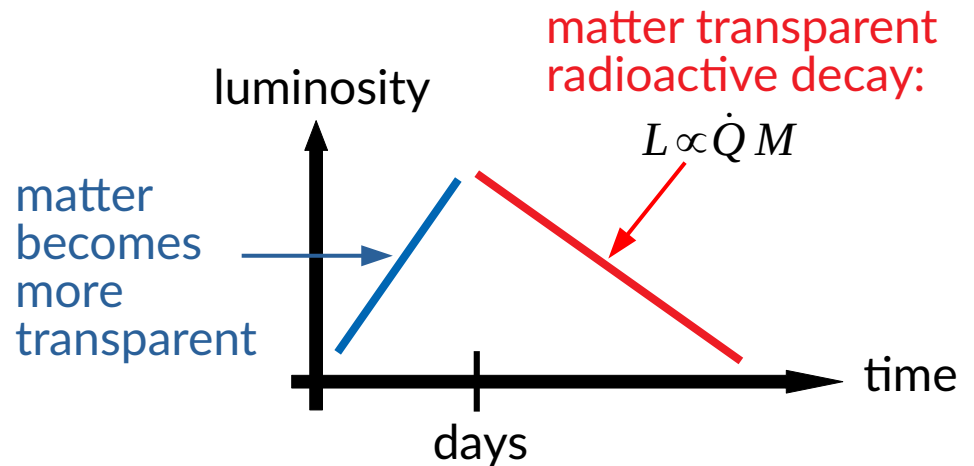
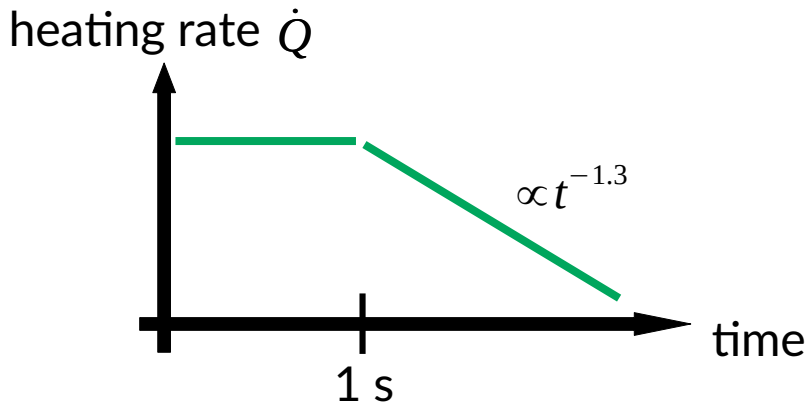
Nuclear heating rate

- Radioactive decays of *r*-process elements release nuclear energy

$$\dot{Q}_{r\text{-process}} = \sum_{i \in \text{reactions}} Q_i \lambda_i$$

with $Q = M_{\text{initial}} - M_{\text{final}}$
and $\lambda = \text{decay rate}$

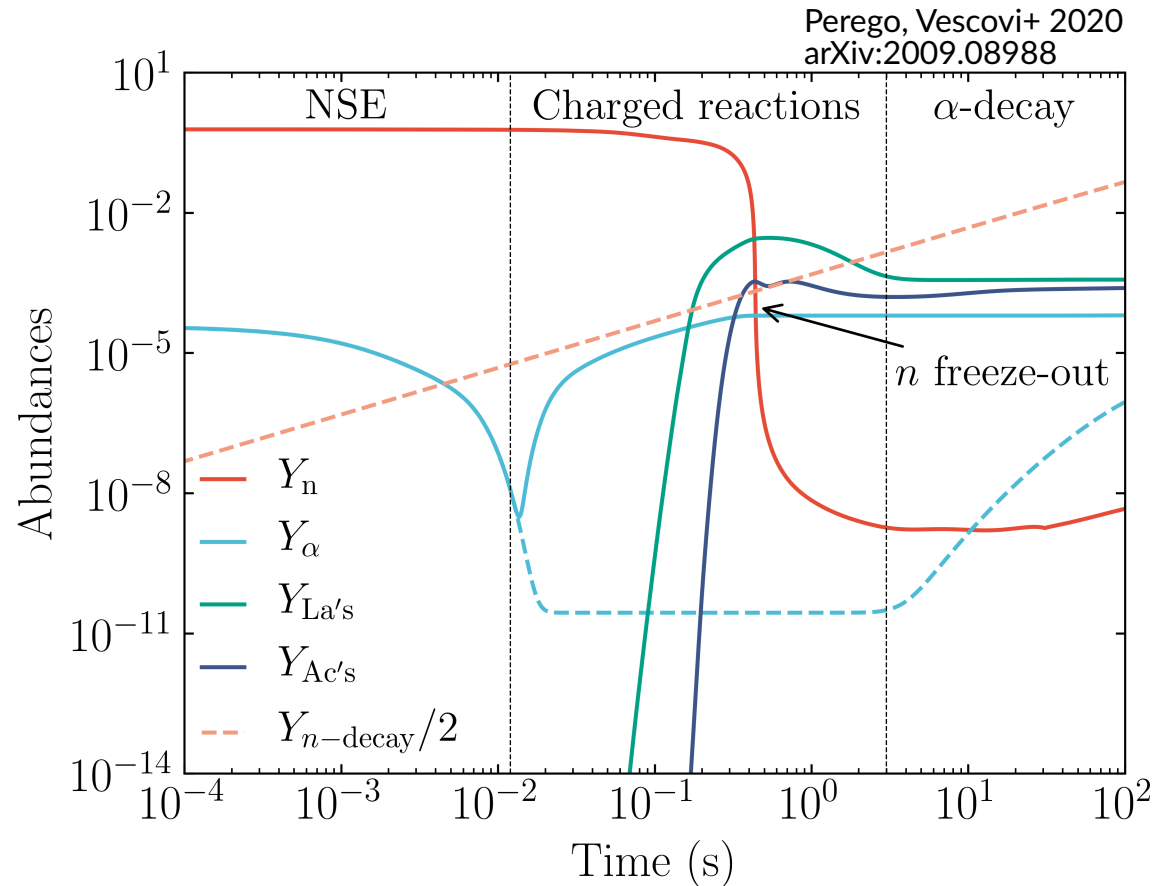
$Y_e \gtrsim 0.25$	$Y_e \lesssim 0.25$
weak <i>r</i> -process ($A < 130$)	robust <i>r</i> -process ($A > 130$)
“blue transients” peaking after ~ 1 day	“red transients” peaking after ~ 1 week



- key physics ingredients:
 - 1) ejecta mass, velocity, $Y_e \longrightarrow$ astrophysics
 - 2) opacity $\kappa_\gamma \longrightarrow$ atomic physics
 - 3) radioactive heating rate $\dot{Q} \longrightarrow$ nuclear physics

Origin of He

- **Free neutrons** are abundant and provide an almost steady supply of free protons (through *n*-decay) and the efficient formation of deuterium (d) and tritium (t).
- Y_α increases through charge reactions such as $t + t \rightarrow 2n + {}^4\text{He}$ and $d + t \rightarrow n + {}^4\text{He}$
- At later times ($t > \sim 2$ s), α -decay of translead nuclei becomes significant and Y_α increases further



Trajectory with $s = 10 \text{ k}_B \text{ baryon}^{-1}$, $\tau = 10 \text{ ms}$ and $Y_e = 0.15$