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# The TeV gamma-ray population of the Milky-Way

the contribution of H.E.S.S. unresolved sources to VHE diffuse emission

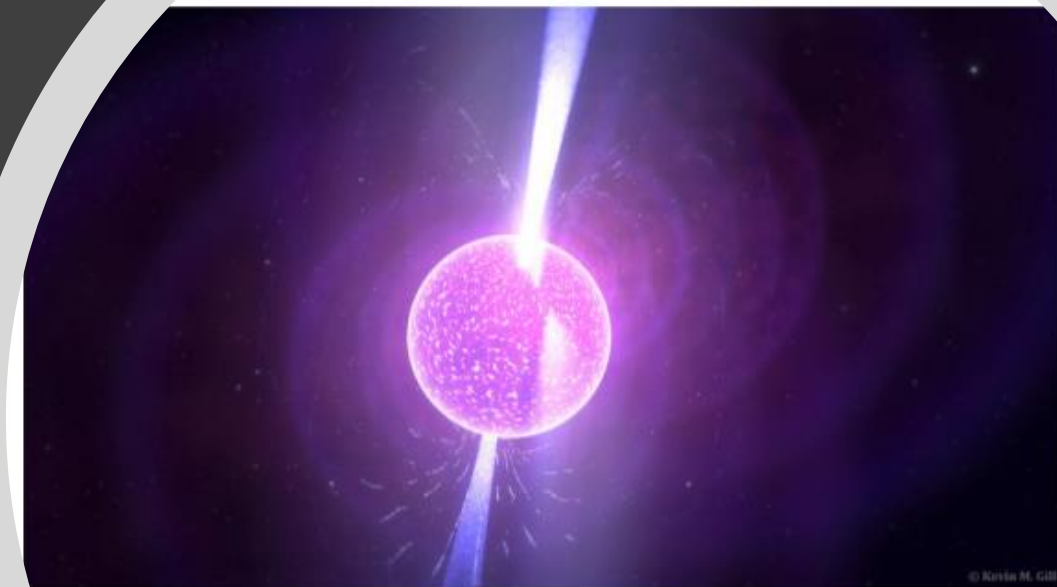
Presented by: Vittoria Vecchiotti

Based on a work done in collaboration with: M. Cataldo, G. Pagliaroli, F. L. Villante

# The TeV gamma-ray luminosity of the Milky-Way: and the contribution of H.E.S.S. unresolved sources to VHE diffuse emission

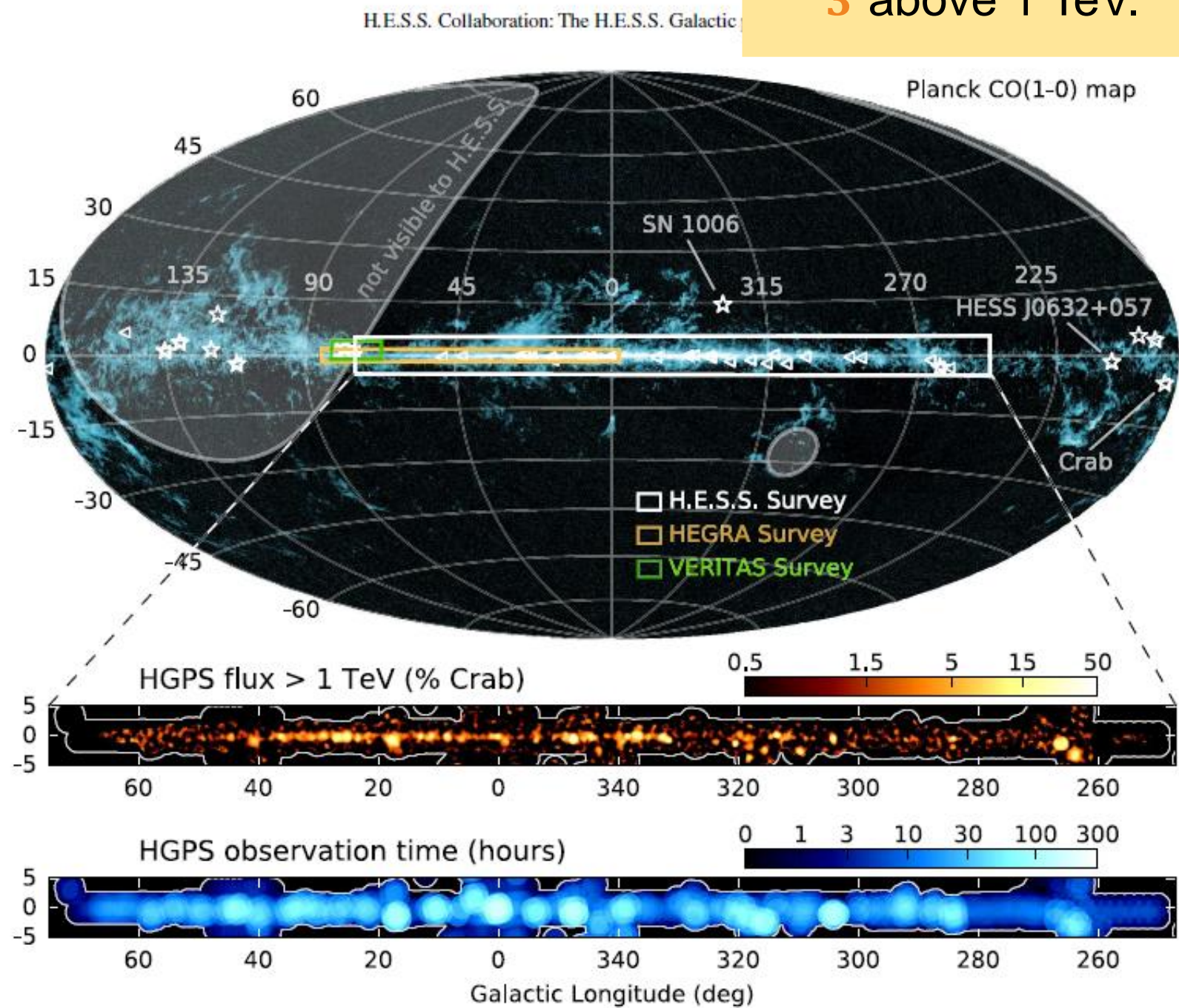
<https://inspirehep.net/literature/1799863>

- Population study of the H.E.S.S. Galactic Plane Survey in order to estimate the **total luminosity of the Milky-Way** and **total source flux** and the contribution of H.E.S.S. **unresolved sources** to VHE diffuse emission;
- **Fading-sources interpretation:** In the hypothesis that the signal is dominated by pulsar-powered sources (TeV-Halos, PWNe) we inferred general properties of the pulsar population.

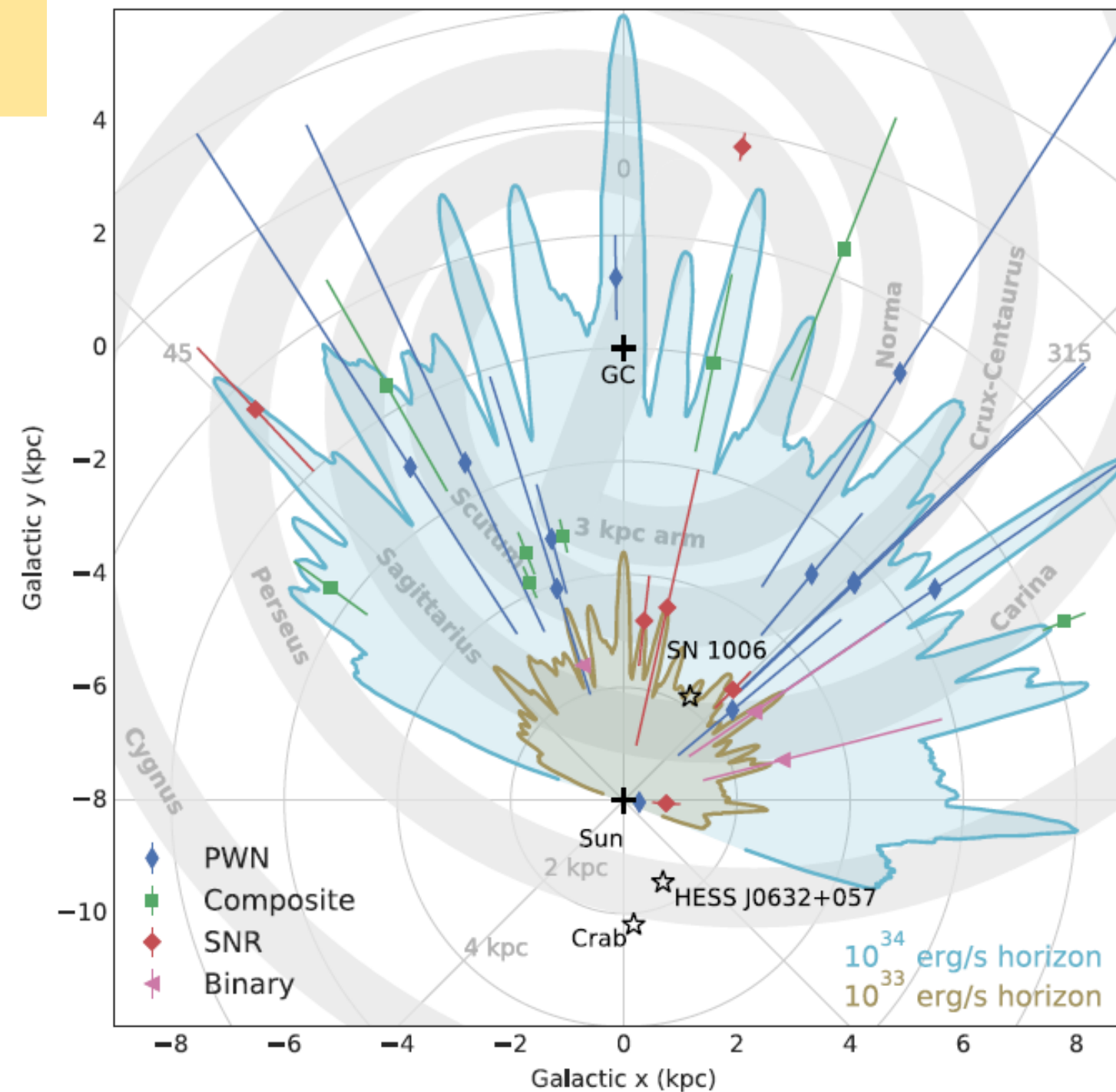


# H.E.S.S.:

H.E.S.S. provides observation of the  $\gamma$ -ray sky in the window:  
 $-110^\circ < l < 60^\circ$  and  $|b| < 3^\circ$  above 1 TeV.



H.E.S.S. sensitivity detection limit:



Concerning point-like sources, H.E.S.S. probes a small fraction of the Galaxy up to a median distance of 7.3 kpc for bright ( $10^{34} \text{ erg s}^{-1}$ ) sources.



Unresolved sources that contribute to the total diffuse signal.

# H.G.P.S catalogue:

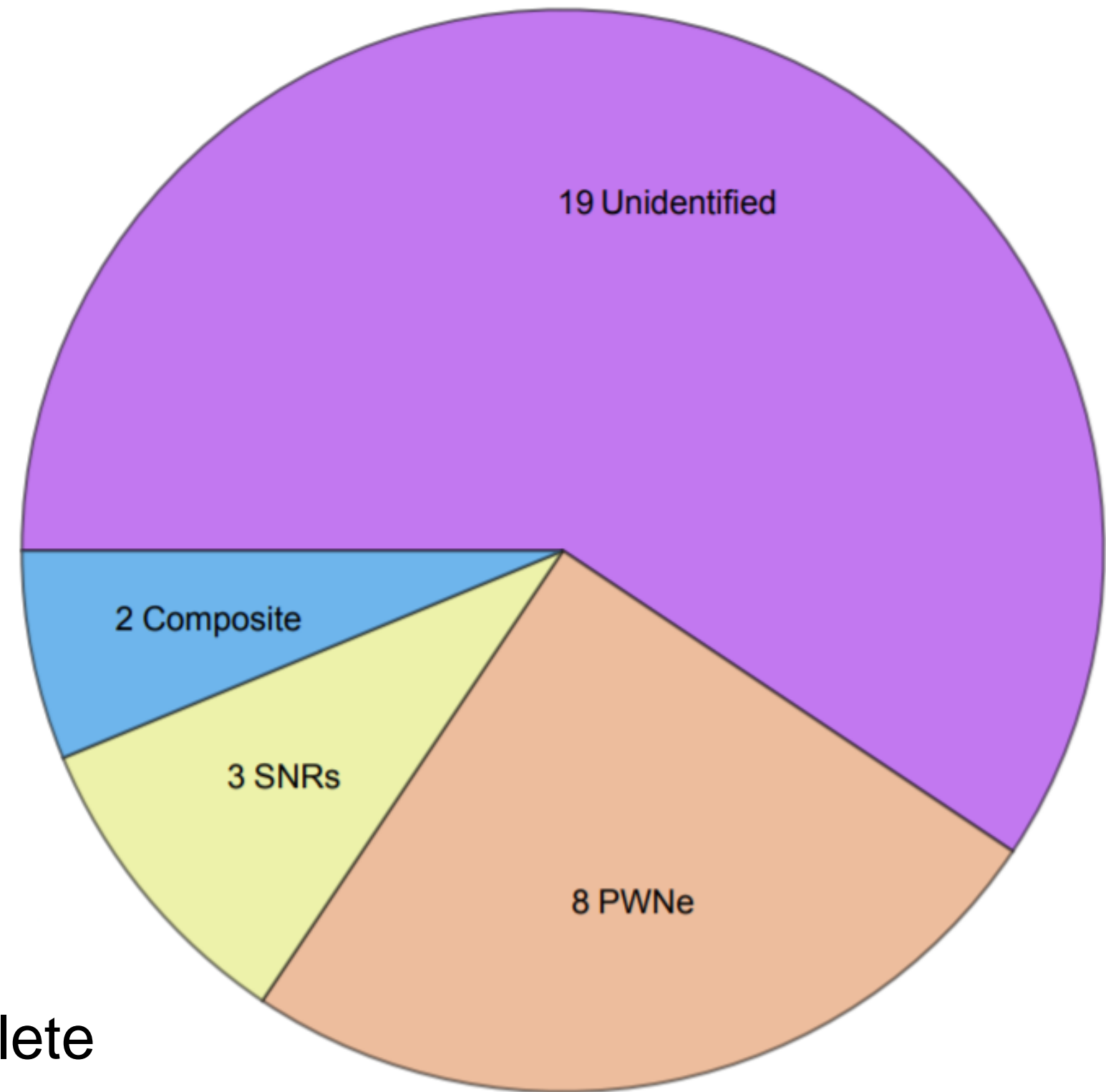
- It includes **78 VHE** sources in the H.E.S.S. observational window;
- It provides the integrated flux above 1 TeV of each sources  $\phi$ .

We focus on the brightest sources with flux:

$$\phi > 0.1\phi_{Crab} = 0.1 (2.26 \times 10^{-11} \text{cm}^{-2} \text{s}^{-1})$$

The catalogue above this threshold is considered complete (no unresolved sources): **32 sources**.

We assumed a **power-law** energy spectrum with index  $\beta = 2.3$  that is the average index of the catalogue for all the sources ;



**Model:** We postulate the **spatial** and intrinsic **luminosity** distribution of the TeV sources:

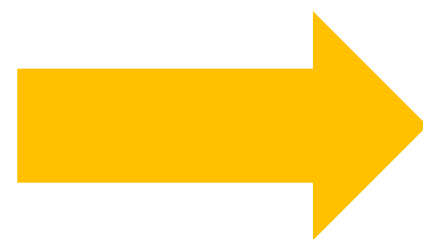
$$\frac{dN}{dr^3 dL} = \rho(r) Y(L)$$

- The **spatial distribution** of sources in the Galaxy is assumed to be proportional to the pulsar distribution as in [Lormier et Al \(2006\)](#).;
- The **luminosity distribution** of sources in the Galaxy is assumed to be a **power law**:

$$Y(L) = \frac{\mathcal{N}}{L_{max}} \left( \frac{L}{L_{max}} \right)^{-\alpha}$$

Reference case:  
 $\alpha = 1.5$

We have two  
free parameters:

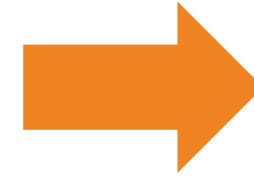


- the normalization  $\mathcal{N}$  number of high-luminosity sources
- the maximum luminosity of the population  $L_{max}$

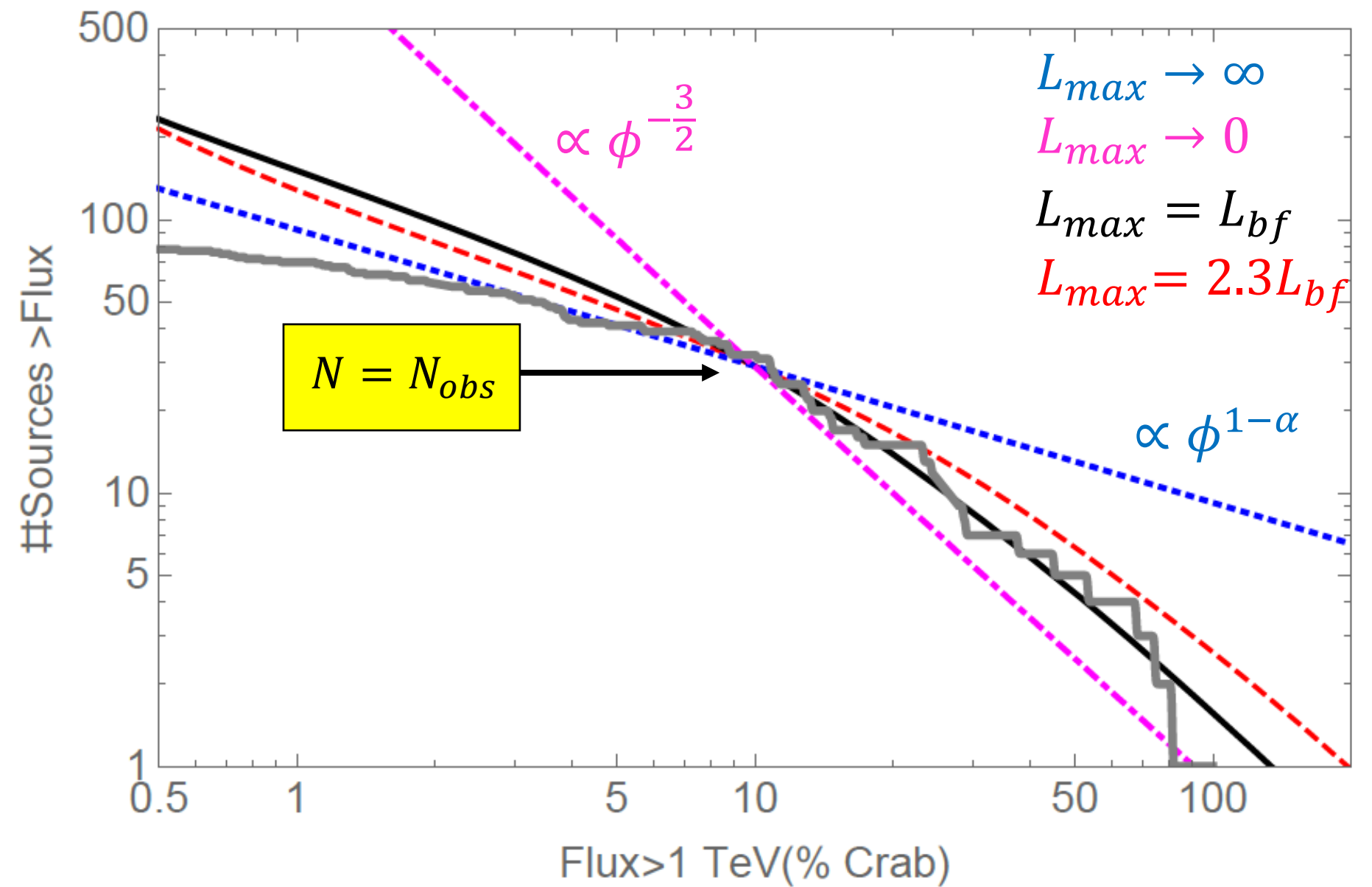
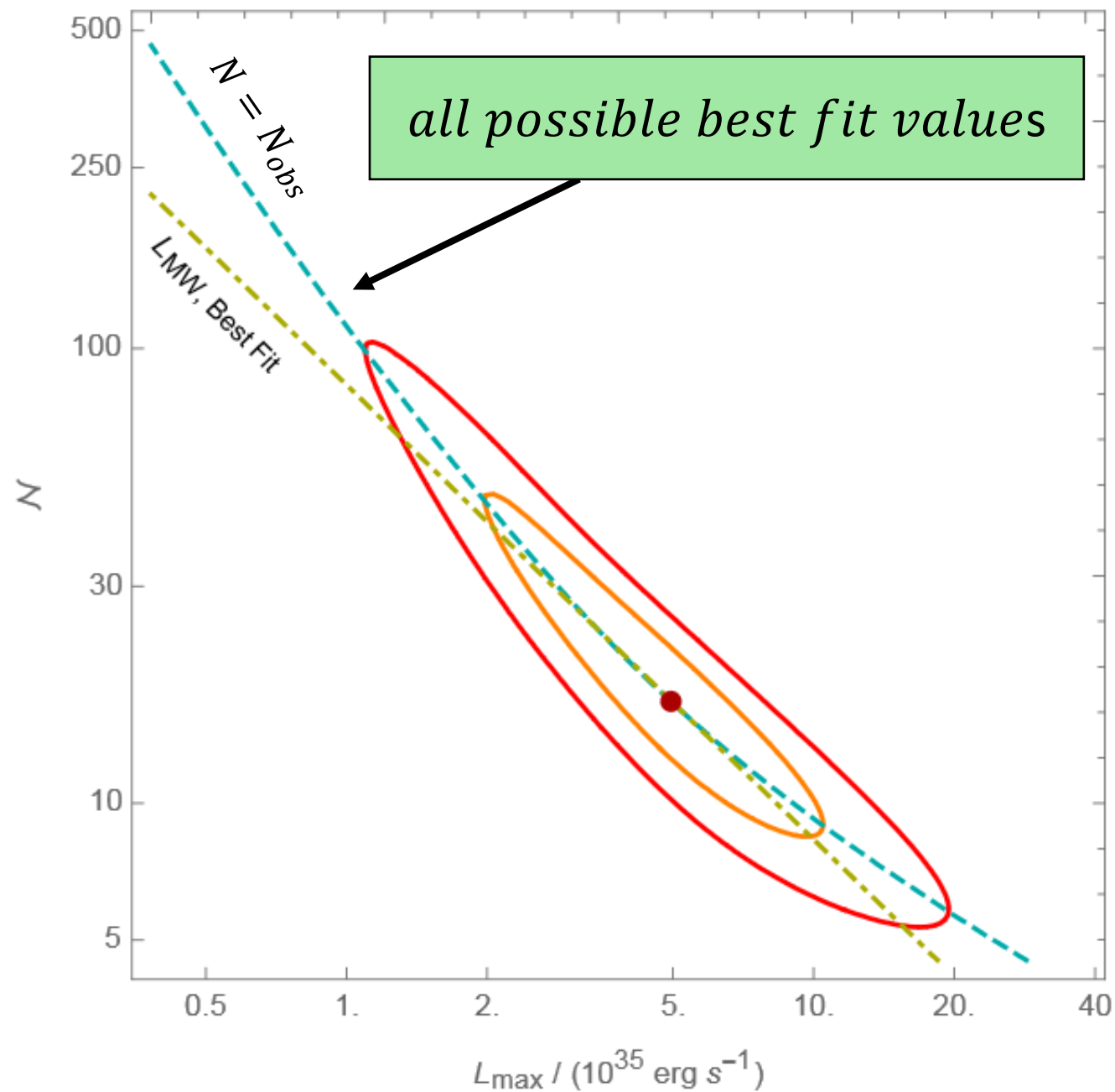
**Goal:** Estimation of the free parameters of our model by fitting H.E.S.S. observational results with an unbinned likelihood

# Results:

Best fit values for the reference case:

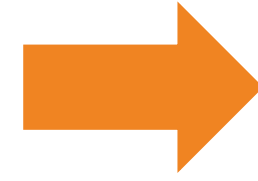


$$L_{\max} = 4.9_{-2.1}^{+3.0} \times 10^{35} \text{ ergs/s}$$
$$\mathcal{N} = 17_{-6}^{+14}$$

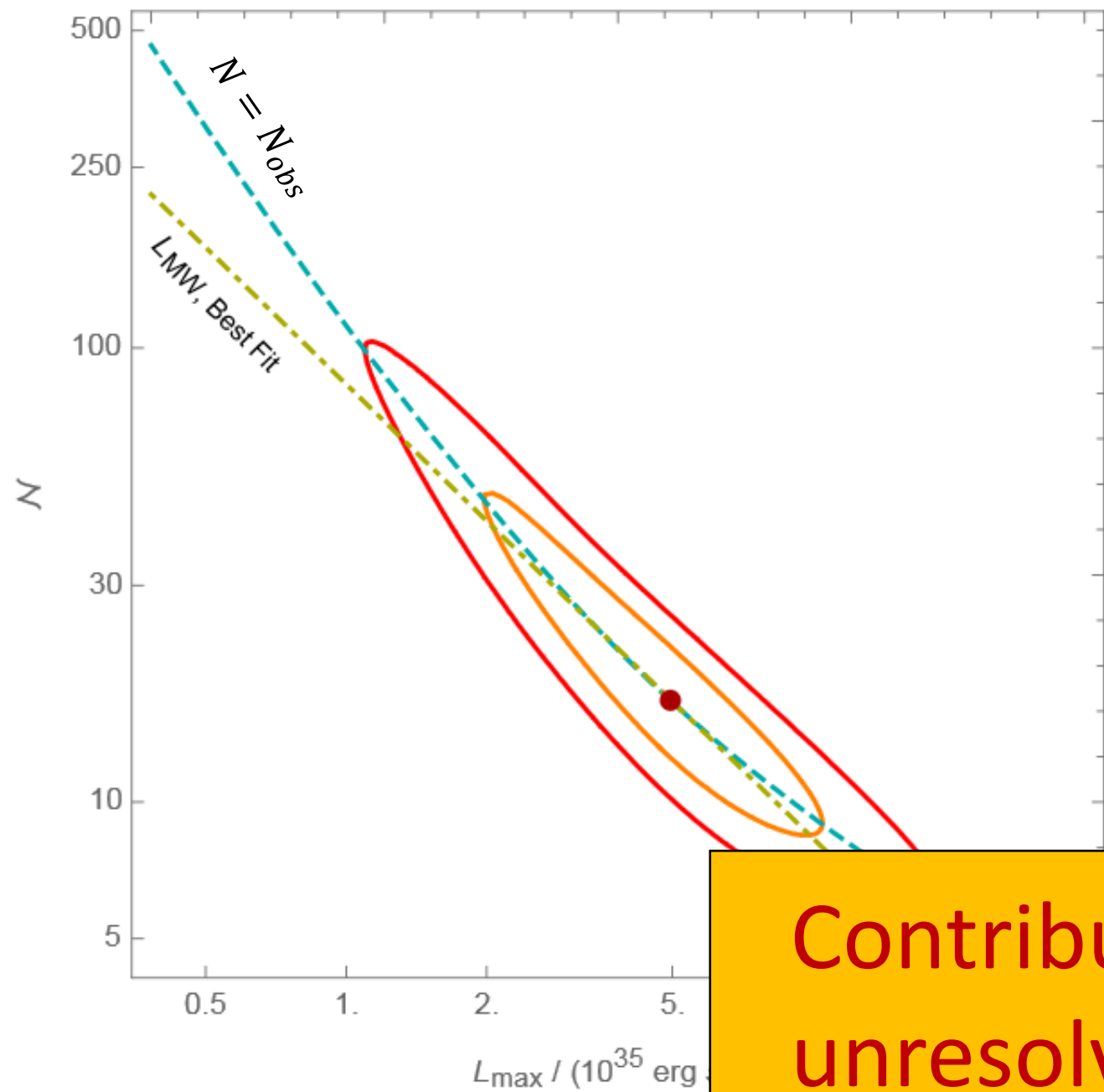


# Results:

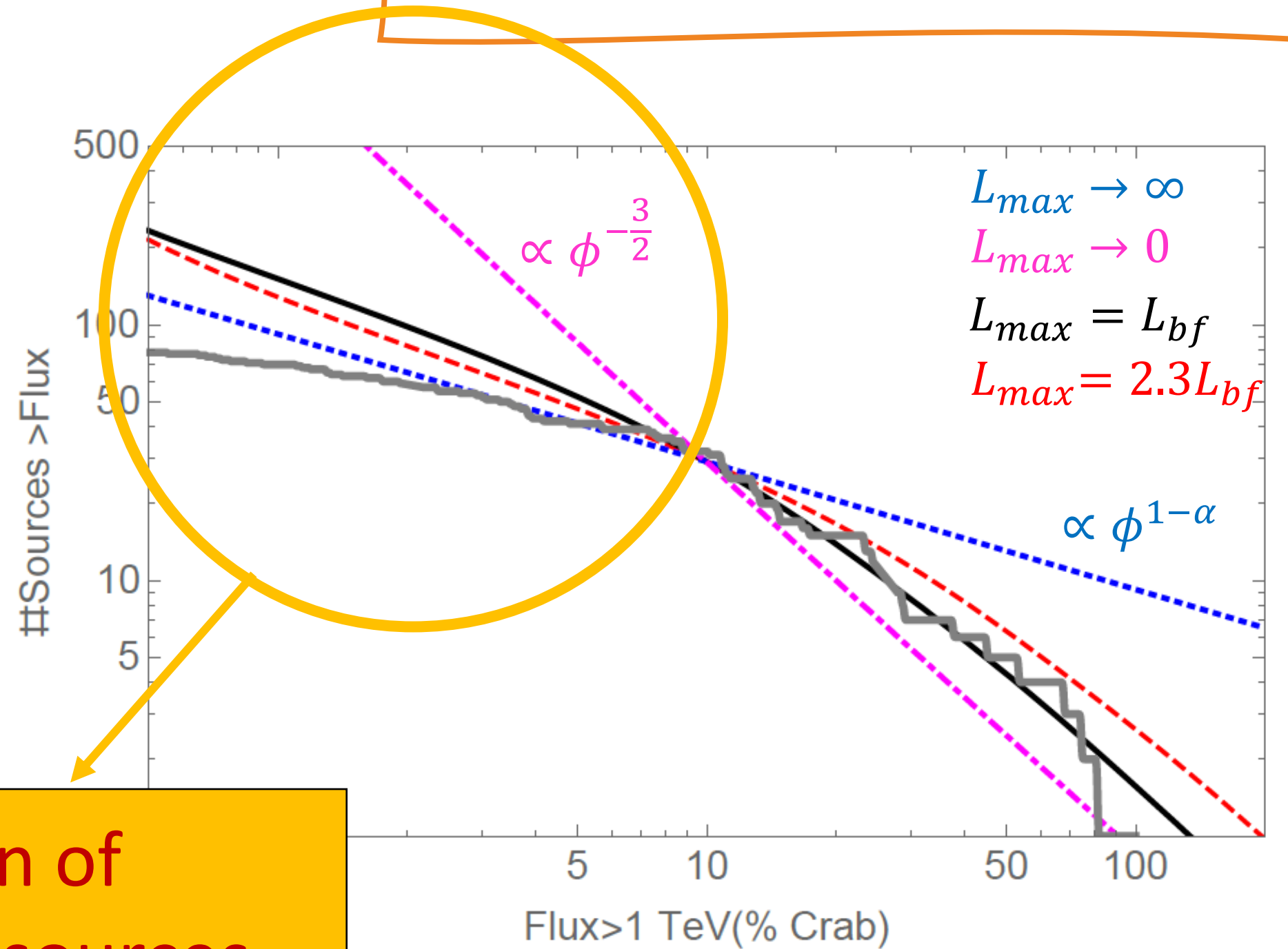
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Contribution of unresolved sources



# Results:

- The total **TeV luminosity (1-100 TeV)** of the Galaxy:

$$L_{MW} = \frac{N L_{max}}{(2-\alpha)} \left[ 1 - \left( \frac{L_{min}}{L_{max}} \right)^{\alpha-2} \right] = 1.7^{+0.5}_{-0.4} \times 10^{37} \text{ erg s}^{-1}$$

- The **flux at Earth produced by all sources (1-100 TeV)** (resolved and unresolved) in the H.E.S.S. OW:

$$\phi_{tot} = \frac{L_{MW}}{4\pi \langle E \rangle} \int_{OW} d^3r \rho(r) r^{-2} = 3.8^{+1.0}_{-1.0} \times 10^{-10} \text{ cm}^{-2} \text{ s}^{-1}$$

3.25 TeV

- By subtraction we can obtain the contribution of **unresolved sources** in the H.E.S.S. observational window knowing that:  $\phi_{S,res} = 2.3 \times 10^{-10} \text{ cm}^{-2} \text{ s}^{-1}$  (cumulative flux due to all 78 sources):

$$\phi_{S,unres} = \phi_{tot} - \phi_{S,res} = 1.4^{+1.0}_{-0.8} \times 10^{-10} \text{ cm}^{-2} \text{ s}^{-1} \sim 60\% \phi_{S,res}$$



# Robustness of the results:

	$\log_{10} \frac{L_{\max}}{\text{erg s}^{-1}}$	$\mathcal{N}$	$\log_{10} \frac{L_{\text{MW}}}{\text{erg s}^{-1}}$	$\Phi_{\text{tot}}$	$\tau$	$\Delta\chi^2$
Ref.	$35.69^{+0.21}_{-0.28}$	$17^{+14}_{-6}$	$37.22^{+0.12}_{-0.13}$	$3.8^{+1.0}_{-1.0}$	$1.8^{+1.5}_{-0.6}$	—
SNR	$35.69^{+0.22}_{-0.25}$	$18^{+15}_{-7}$	$37.23^{+0.12}_{-0.13}$	$3.8^{+1.0}_{-1.0}$	$1.8^{+1.6}_{-0.7}$	1.4
$H = 0.1$ kpc	$35.65^{+0.22}_{-0.27}$	$15^{+14.5}_{-6}$	$37.13^{+0.12}_{-0.13}$	$5.0^{+0.4}_{-2.0}$	$1.6^{+1.5}_{-0.6}$	-7.3
$H = 0.05$ kpc	$35.34^{+0.26}_{-0.19}$	$28^{+19}_{-13}$	$37.08^{+0.12}_{-0.13}$	$4.4^{+1.3}_{-0.9}$	$2.9^{+2.0}_{-1.4}$	-10.5
$d = 20$ pc	$35.69^{+0.20}_{-0.26}$	$17^{+16}_{-6}$	$37.23^{+0.12}_{-0.13}$	$3.9^{+0.8}_{-1.0}$	$1.9^{+1.9}_{-0.7}$	-0.2
$d = 40$ pc	$35.67^{+0.20}_{-0.25}$	$20^{+20}_{-8}$	$37.28^{+0.12}_{-0.13}$	$4.4^{+1.2}_{-1.1}$	$2.2^{+2.0}_{-0.8}$	-1.8
$\alpha = 1.3$	$35.61^{+0.18}_{-0.27}$	$25^{+24}_{-8.5}$	$37.17^{+0.12}_{-0.13}$	$3.5^{+1.1}_{-0.9}$	$4.3^{+4.3}_{-1.5}$	0.0
$\alpha = 1.8$	$35.83^{+0.29}_{-0.24}$	$7^{+6}_{-4}$	$37.39^{+0.11}_{-0.13}$	$5.9^{+1.8}_{-0.1}$	$0.5^{+0.4}_{-0.2}$	0.5

# Robustness of the results:

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The quality of the fit improves by reducing the thickness of the disk.

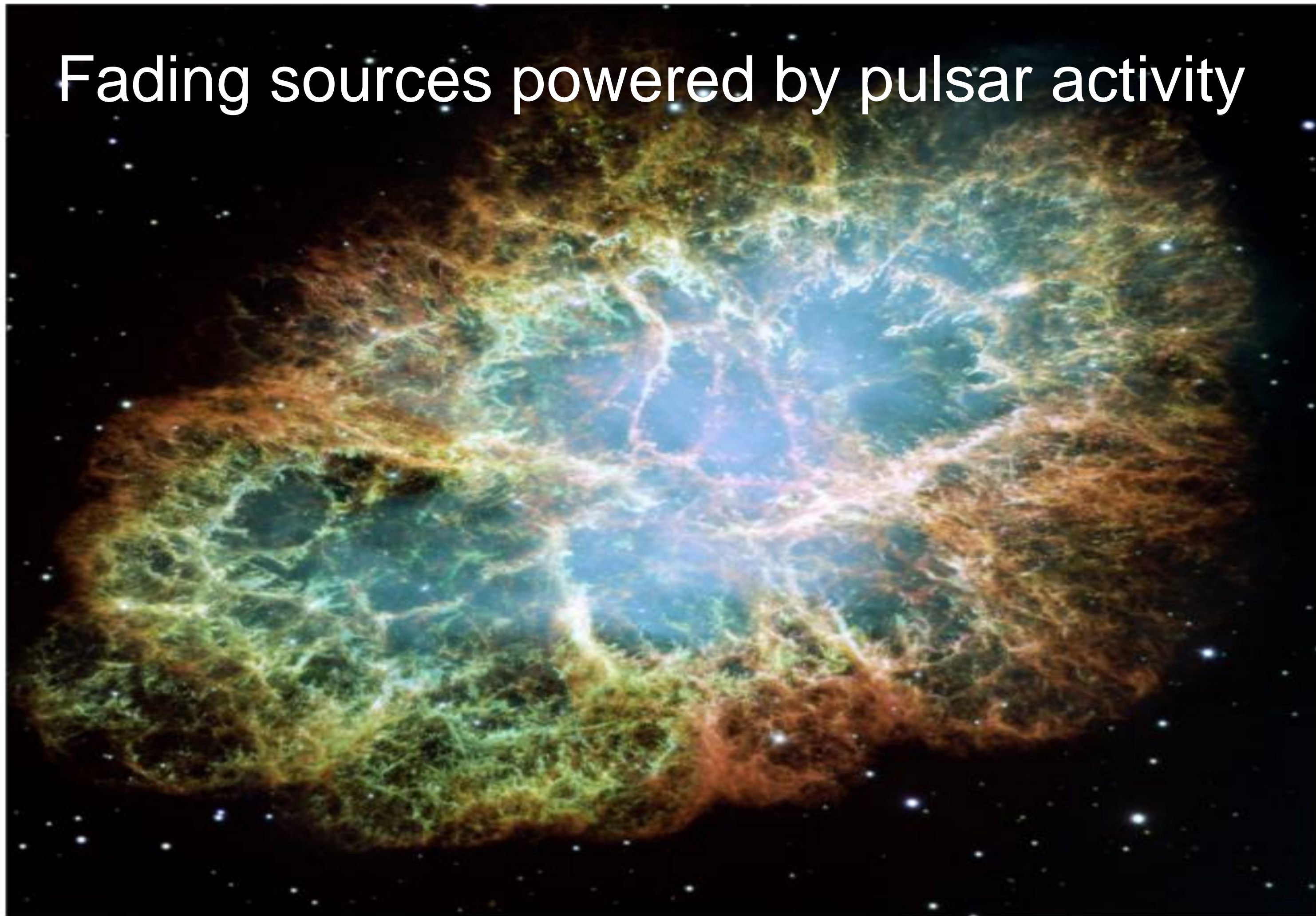
# Robustness of the results:

	$\log_{10} \frac{L_{\max}}{\text{erg s}^{-1}}$	$\mathcal{N}$	$\log_{10} \frac{L_{MW}}{\text{erg s}^{-1}}$	$\Phi_{\text{tot}}$	$\tau$	$\Delta\chi^2$
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$$L_{MW} = (1.2 - 2.5) \times 10^{37} \text{ erg s}^{-1}$$

$$\Phi_{\text{tot}} = (3.5 - 5.9) 10^{-10} \text{ cm}^{-2} \text{ s}^{-1}$$

# Fading sources powered by pulsar activity



## Model:

$$\frac{dN}{d^3r dL} = \rho(\mathbf{r}) Y(L)$$

Assuming a fading source population (like PWNe, TeV Halos), the spin-down power is described by:

$$\dot{E}(t) = \dot{E}_0 \left(1 + \frac{t}{\tau_{sd}}\right)^{-2}$$

Considering that a fraction  $\lambda(t)$  of the spin-down power is converted into gamma-rays then the intrinsic luminosity decreases according to:

$$L(t) = \lambda(t) \dot{E}(t) = \lambda \dot{E}_0 \left(1 + \frac{t}{\tau_{sd}}\right)^{-\gamma} \text{ where } \gamma = 2(\delta + 1);$$

$$\lambda(t) = \lambda \left(\frac{\dot{E}(t)}{\dot{E}_0}\right)^\delta$$

## Model:

$$\frac{dN}{d^3r dL} = \rho(\mathbf{r}) Y(L)$$

We automatically obtain a **power law** for the luminosity distribution:

$$Y(L) = \frac{\bar{r} \tau (\alpha - 1)}{L_{\max}} \left( \frac{L}{L_{\max}} \right)^{-\alpha}$$

Where  $\bar{r} = 0.019 \text{ yr}^{-1}$  is the SN's rate and  $\alpha = \left( \frac{1}{\gamma} + 1 \right)$  therefore for  $\gamma = 2$  we have  $\alpha = 1.5$ .

In conclusion the new free parameters are:



- the spin-down timescale  $\tau$
- the maximum luminosity of the population  $L_{\max}$

# Model:

The best fit parameters  $L_{max}$  and  $\tau_{sd}$  are linked to the magnetic field  $B_0$  and the initial spin-down period  $P_0$  of the pulsar through this relations:

$$L_{max} = \lambda \dot{E}_0 = \lambda \frac{8\pi^4 B_0^2 R^6}{3c^3 P_0^4}$$

$$\tau_{sd} = \frac{3Ic^3 P_0^2}{4\pi^2 B_0^2 R^6}$$

For the firmly identified pulsar from the HGPS catalogue we obtained that the parameter  $\lambda$  is in the range:

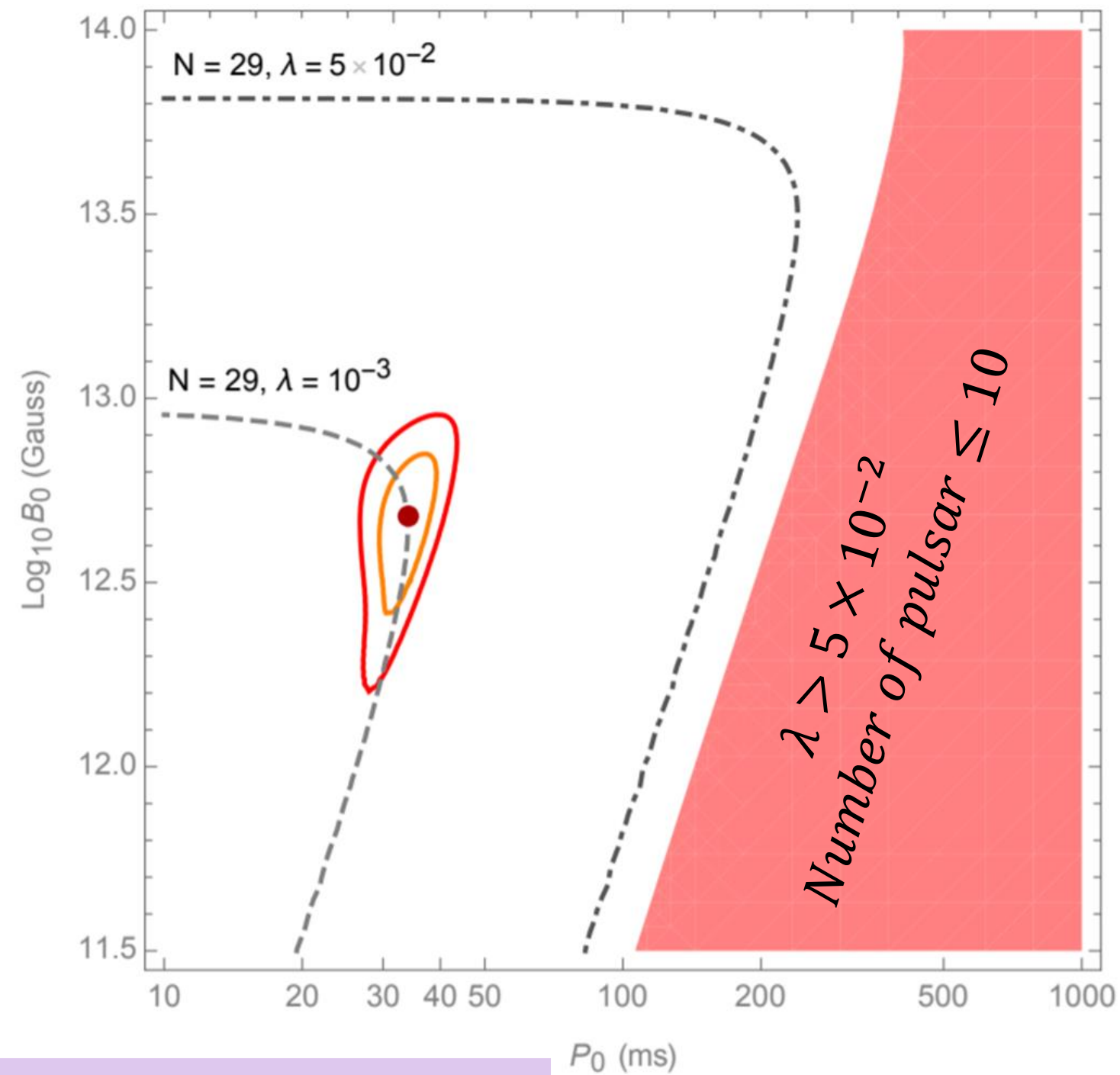
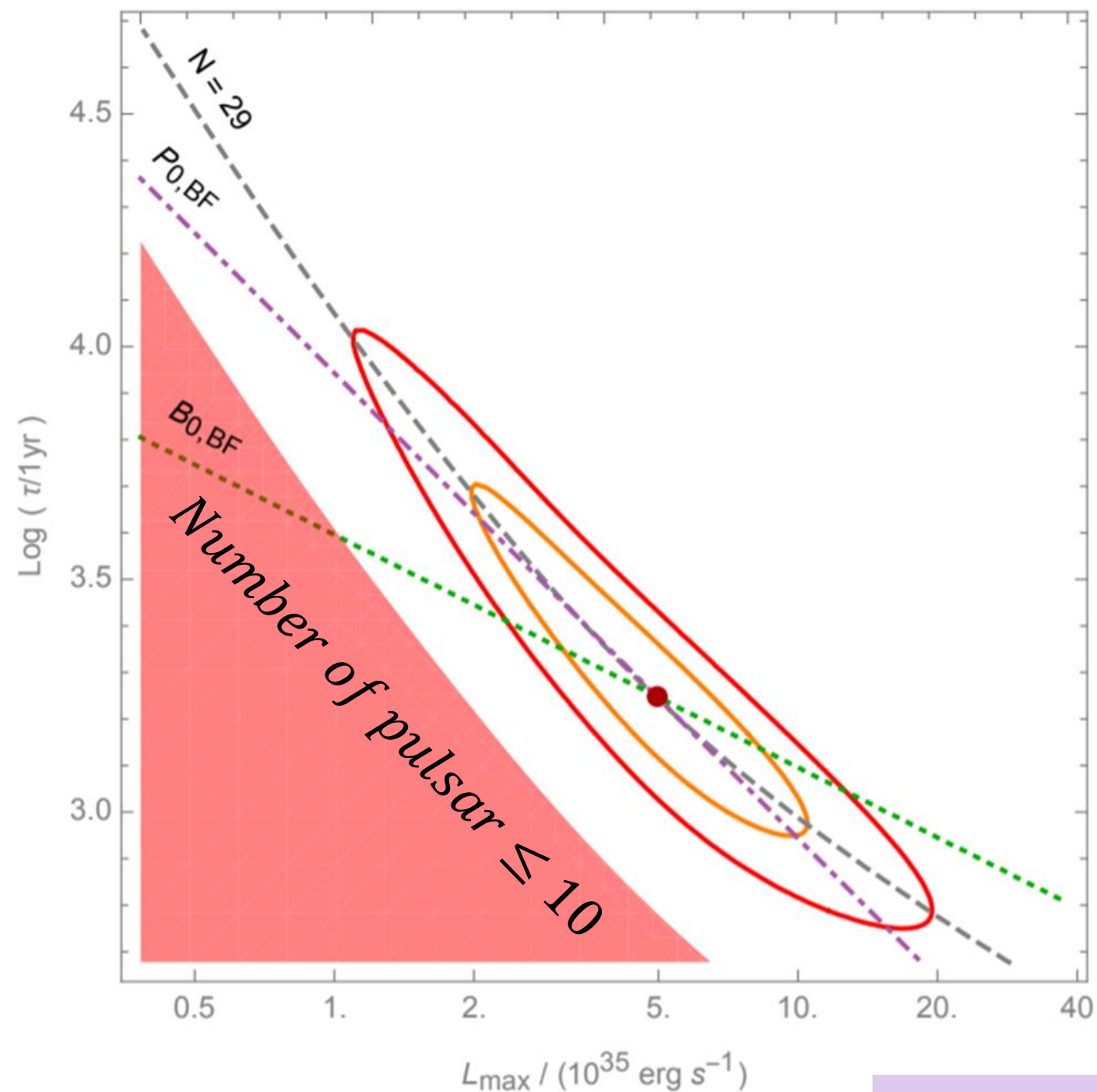
$$5 \times 10^{-5} \leq \lambda \leq 5 \times 10^{-2}$$

As a reference value we take  $\lambda = 10^{-3}$

$$\frac{P_0}{1 \text{ ms}} = 94 \left( \frac{\lambda}{10^{-3}} \right)^{\frac{1}{2}} \left( \frac{\tau}{10^4 \text{ yr}} \right)^{-\frac{1}{2}} \left( \frac{L_{max}}{10^{34} \text{ erg s}^{-1}} \right)^{-\frac{1}{2}}$$

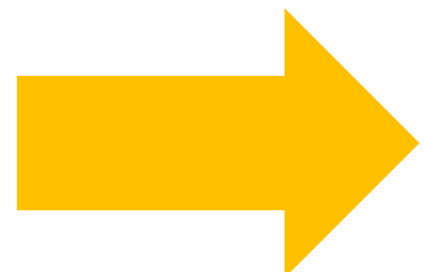
$$\frac{B_0}{10^{12} \text{ G}} = 5.2 \left( \frac{\lambda}{10^{-3}} \right)^{\frac{1}{2}} \left( \frac{\tau}{10^4 \text{ yr}} \right)^{-\frac{1}{2}} \left( \frac{L_{max}}{10^{34} \text{ erg s}^{-1}} \right)^{-\frac{1}{2}}$$

# Results:



$$\tau_{sd} = 1.8_{-0.6}^{+1.5} \times 10^3 \text{ yr}$$

$$L_{\text{max}} = 4.9_{-2.1}^{+3.0} \times 10^{35} \text{ ergs s}^{-1}$$



$$P_0 = 33_{-4.3}^{+5.4} \text{ ms} \times \left( \frac{\lambda}{10^{-3}} \right)^{\frac{1}{2}}$$

$$B_0 = 4.32(1 \pm 0.45) 10^{12} \text{ G} \times \left( \frac{\lambda}{10^{-3}} \right)^{\frac{1}{2}}$$





# Conclusions:

- Using the H.G.P.S. we are able to calculate the total Milky Way luminosity in the energy range 1 -100 TeV and the total flux in the H.E.S.S. observational window in the energy range 1 -100 TeV;
- The contribution of unresolved sources is not negligible being  $\sim 60\%$  of the resolved signal measured by H.E.S.S.;
- In the hypothesis of a fading-source population powered by pulsar activity we are able to predict the general parameters of the pulsar  $P_0$  and  $B_0$ . Our predictions are in agreement with values obtained from TeV pulsars but the period is 1 order of magnitude lower than the value observed for radio pulsars.

# Future Plans:

- Study of the contribution of unresolved sources for present (Milagro, FermiLAT) and future experiments (CTA);
- Implication of unresolved contribution for the determination of the diffuse component due to cosmic ray interactions.



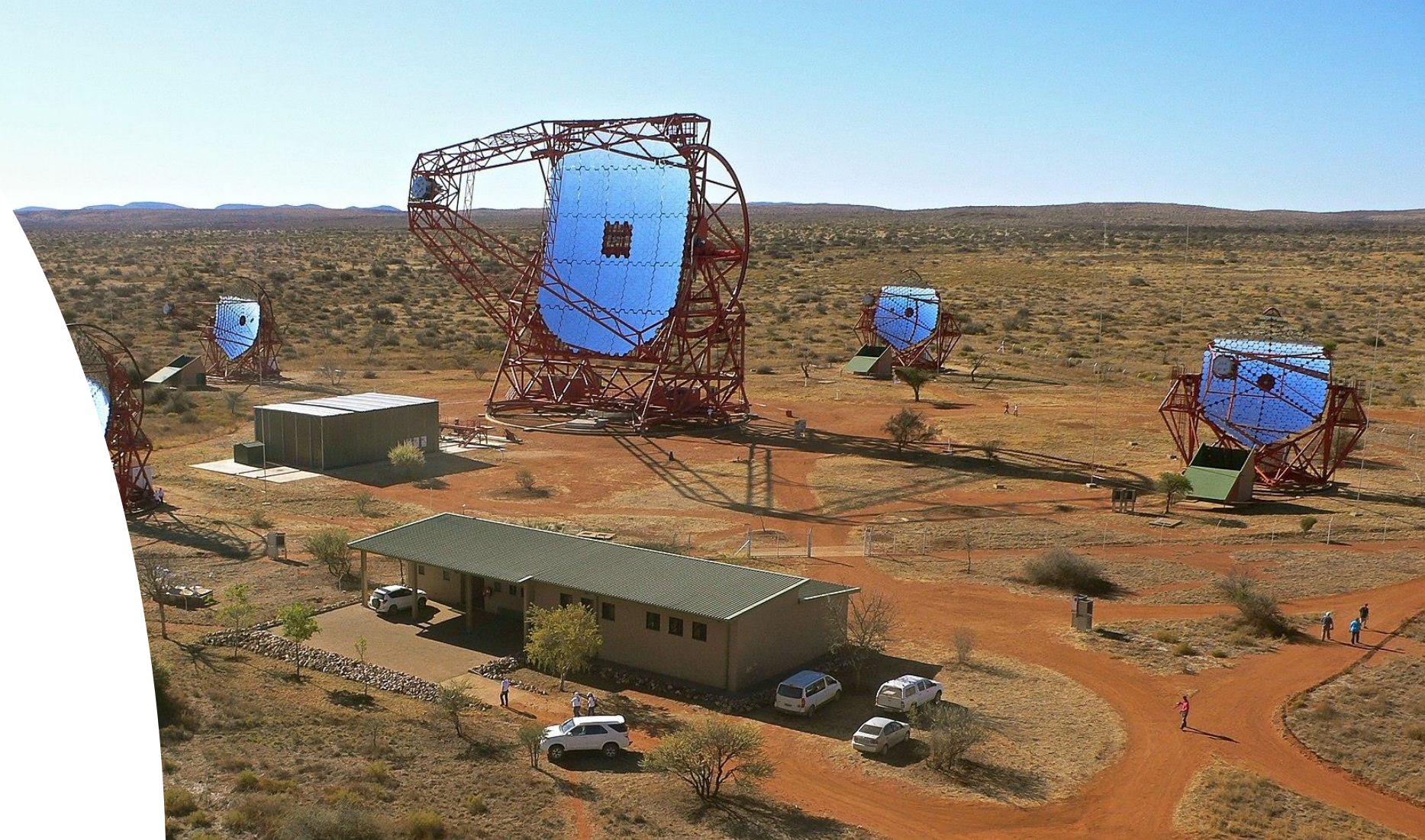
Thank you for the attention!

# Why H.E.S.S.?

The fraction of sources of the considered population which are included respectively in the H.E.S.S. ( $-110^\circ < l < 60^\circ$  and  $|b| < 3^\circ$ ) and H.A.W.C. ( $0^\circ < l < 180^\circ$  and  $|b| < 2^\circ$ ) observation window:

$$\text{H.E.S.S. } \int d^3r \rho(\mathbf{r}) = 0.816$$

$$\text{H.A.W.C. } \int d^3r \rho(\mathbf{r}) = 0.389$$



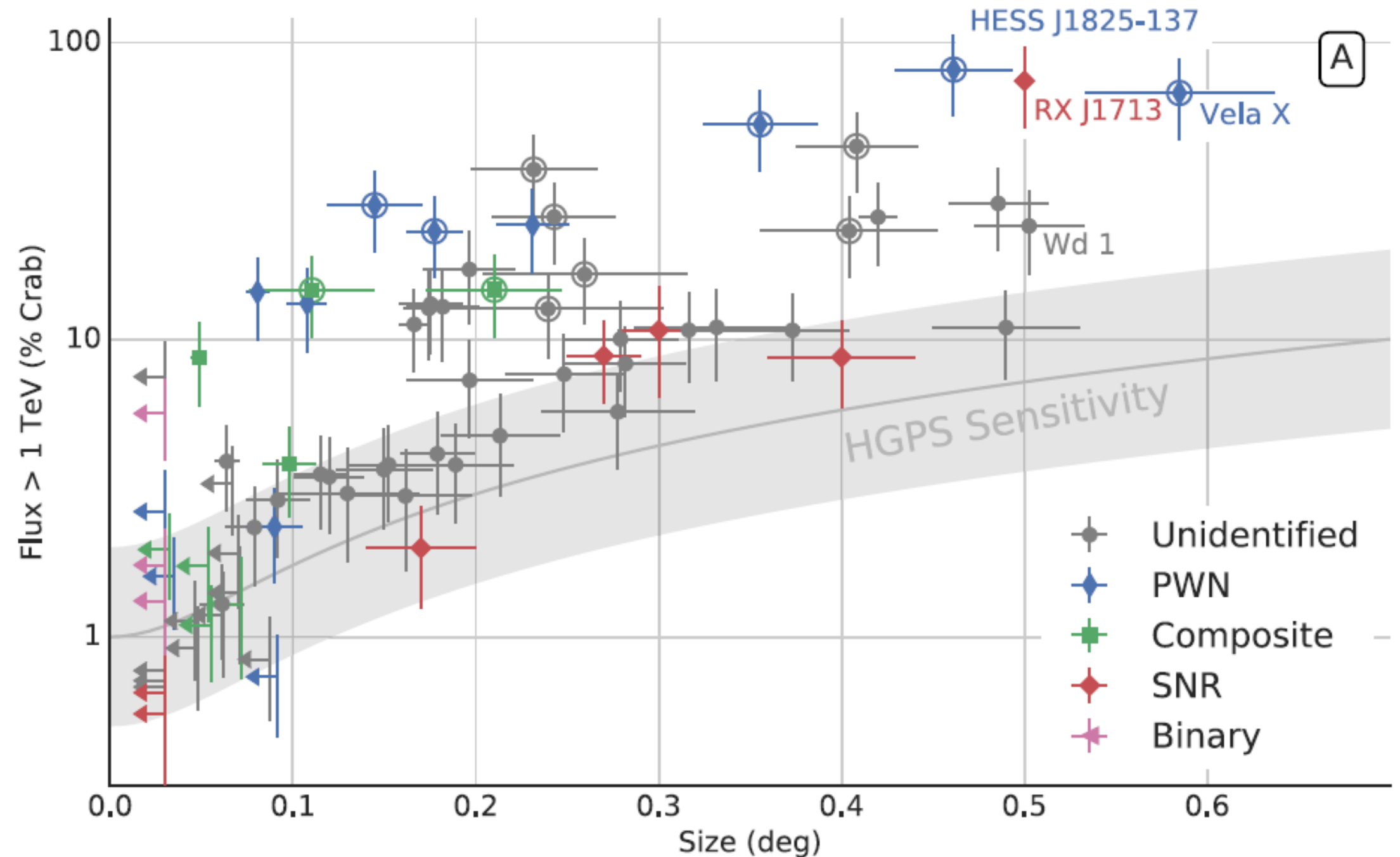
*The HAWC Observatory (J. Goodman, Nov. 2016)*



# H.E.S.S. sensitivity:

- For  $0.01\phi_{Crab} \leq \phi \leq 0.1\phi_{Crab}$  the H.E.S.S. sensitivity depends on the angular size of the sources.
- For  $\phi \geq 0.1\phi_{Crab}$  all the sources are resolved independently of their angular size. Above this threshold the catalogue is complete.

H.E.S.S. Collaboration: The H.E.S.S. Galactic plane survey



# Cumulative distribution:

The flux distribution can be calculated as:

$$\frac{dN}{d\Phi} = \int dr 4\pi r^4 \langle E \rangle Y(4\pi r^2 \langle E \rangle \Phi) \bar{\rho}(r)$$

- $\bar{\rho}(r)$  is the sources spatial distribution integrated over the longitude and latitude intervals probed by H.E.S.S.;
- The above integral is performed in the range  $d/\theta_{max} \leq r \leq D(L, \phi)$  = where  $\theta_{max} = 0.7^\circ$  is the maximal angular dimension that can be probed by H.E.S.S. and the  $d$  is the physical dimension of the source. While  $D(L, \phi) = (L/4\pi \langle E \rangle \phi)^{\frac{1}{2}}$ ;
- We calculate analytically the flux distribution for the 2 limits cases  $L_{max} \rightarrow \infty$  and  $L_{max} \rightarrow 0$ :

$$\frac{dN}{d\Phi} = R \tau (\alpha - 1) L_{max}^{\alpha-1} \Phi^{-\alpha} \int_0^\infty dr (4\pi \langle E \rangle)^{1-\alpha} r^{4-2\alpha} \bar{\rho}(r)$$

$$\frac{dN}{d\Phi} \simeq (4\pi \langle E \rangle)^{1-\alpha} \bar{\rho}(0) R \tau (\alpha - 1) L_{max}^{\alpha-1} \Phi^{-\alpha} \int_0^{D(L_{max}, \Phi)} dr r^{4-2\alpha} = \bar{\rho}(0) R \tau \left( \frac{\alpha - 1}{5 - 2\alpha} \right) \left( \frac{L_{max}}{4\pi \langle E \rangle} \right)^{\frac{3}{2}} \Phi^{-\frac{5}{2}}$$

# Effect of dispersion in our Model:

We also consider the effects of dispersion of initial period  $P_0$  and magnetic field  $B_0$  around the reference values  $\tilde{P}_0$  and  $\tilde{B}_0$ . This turns into a dispersion in  $L_{max}(P_0, B_0)$  and  $\tau(P_0, B_0)$ .

We obtain the following luminosity distribution after integrating on  $P_0$  and  $B_0$  distribution:

$$Y(L) = \frac{R \tilde{\tau} (\alpha - 1)}{\tilde{L}} \left( \frac{L}{\tilde{L}} \right)^{-\alpha} G \left( \frac{L}{\tilde{L}} \right)$$

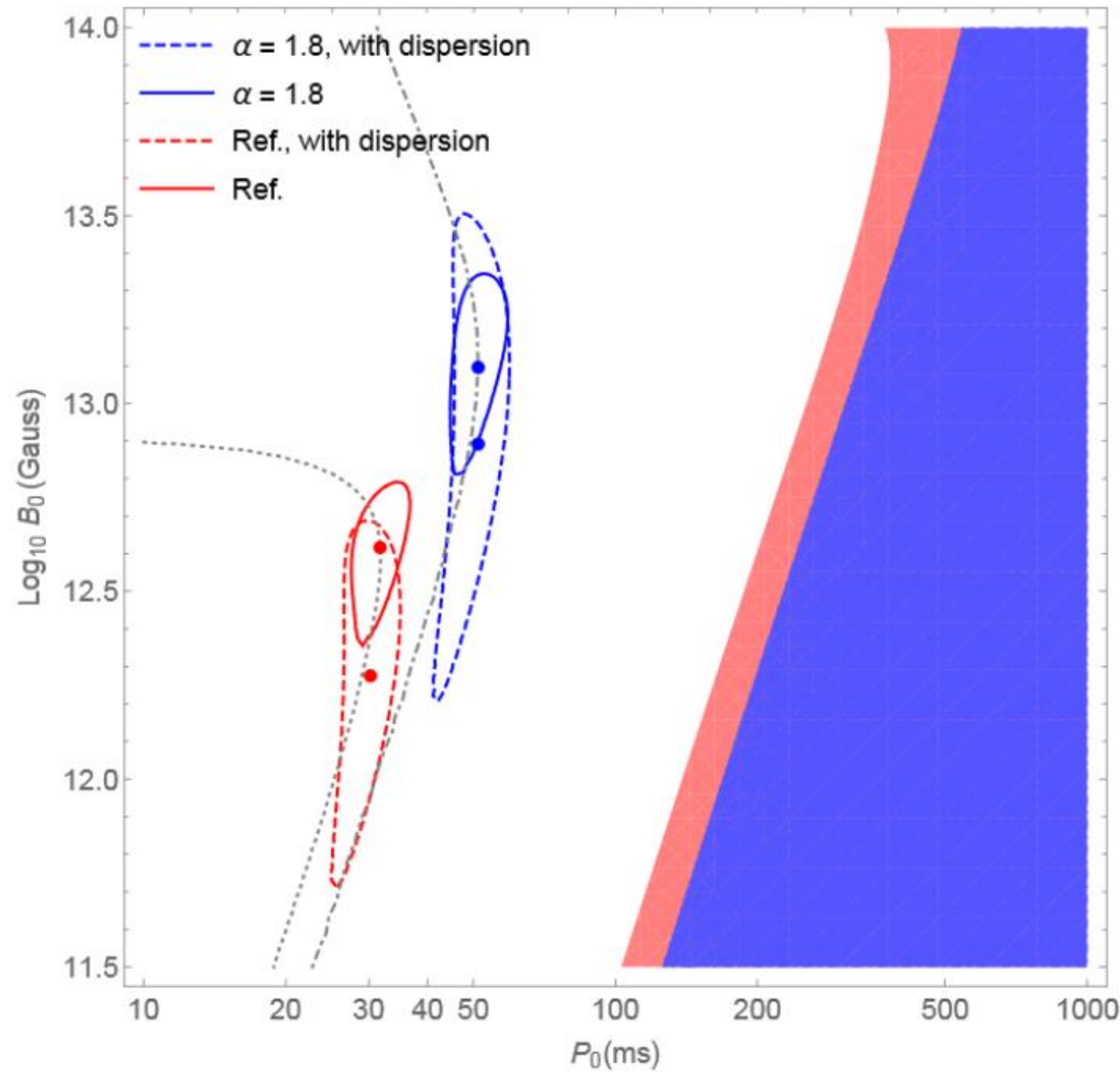
Where  $\tilde{L}(\tilde{P}_0, \tilde{B}_0)$  and  $\tilde{\tau}(\tilde{P}_0, \tilde{B}_0)$  are the spin down time scale and maximum luminosity for the reference values  $\tilde{P}_0$  and  $\tilde{B}_0$  and  $G(x)$  is:

$$G(x) \equiv \int dp \, h(p) p^{6-4\alpha} \int db \, g(b) b^{2\alpha-4} \theta(p^{-4} b^2 - x)$$

Probability distribution for the initial period and it is assumed to be a gaussian distribution in  $\text{Log}_{10}(p)$  where  $p = P/\tilde{P}_0$

Probability distribution for the magnetic field and it is assumed to be a gaussian distribution in  $\text{Log}_{10}(b)$  where  $b = B_0/\tilde{B}_0$

# Results:



The best fit value of  $P_0$  does not change, while  $B_0$  is slightly reduced as a consequence of the high-luminosity tail of the new source luminosity.

$$\alpha = 1.8$$

$$B_0 = 12.7_{-5.8}^{+9.6} 10^{12} G \times \left( \frac{\lambda}{10^{-3}} \right)^{\frac{1}{2}}$$

$$P_0 = 51_{-6.4}^{+8.1} ms \times \left( \frac{\lambda}{10^{-3}} \right)^{\frac{1}{2}}$$



# Milagro excess:

The total flux measured by Milagro at 15 TeV is consistent (within uncertainties) with the total flux produced by the HGPS source population in the same observation window ( $-30^\circ < l < 65^\circ$  and  $|b| < 2^\circ$ ):

$$\frac{d\phi_{\text{Milagro}}}{dE} \sim 2.9 \times 10^{-12} \text{cm}^{-2} \text{s}^{-1} \text{sr}^{-1} \text{TeV}^{-1}$$

$$\frac{d\phi_{\text{HGPS}}}{dE} \sim 3.6_{-0.9}^{+1.1} \times 10^{-12} \text{cm}^{-2} \text{s}^{-1} \text{sr}^{-1} \text{TeV}^{-1}$$

# TeV Halo

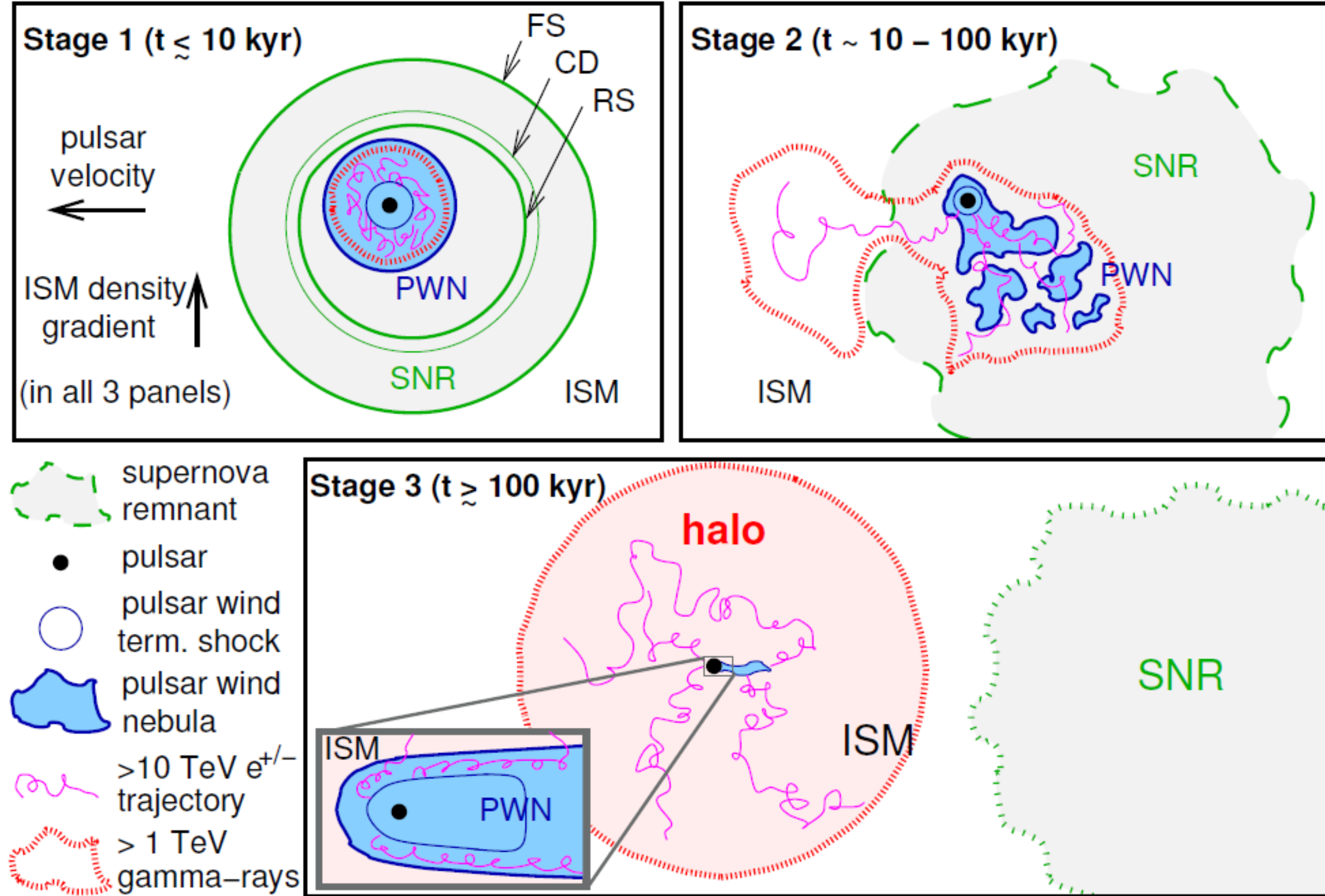
**Stage 1 :** The PWN is contained inside the SNR and before the reverse shock (RS) interacts with it. The electrons that are responsible for the TeV gamma-ray emission of the nebula are thought to be confined within the nebula at this stage

Green line : The SNR forward shock (FS) and contact discontinuity (CD)

**Stage 2 :** The PWN is disrupted by the reverse shock, but before the pulsar escapes its SNR. At this stage, TeV gamma-ray emitting electrons start to escape from the PWN, into the SNR and possibly into the ISM.

**Stage 3 :** The pulsar has escaped from its —now fading— parent SNR. At this stage, high-energy electrons escape into the surrounding ISM, and may, only then, form a halo.

Sketch of the main evolutionary stages of a PWN



[arXiv:1907.12121v1 \[astro-ph.HE\] 28 Jul 2019](https://arxiv.org/abs/1907.12121v1)